Light Element Standard Cross Sections for ENDF/B

Version IV

by

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ABSTRACT

Several light-element standard cross-section evaluations in the ENDF/B-IV file are described and compared with experimental measurements. The hydrogen scattering cross section has long been accepted as a standard since it is essentially equal to the total cross section which is well known and varies smoothly with incident neutron energy. The ^{3}He(n,p)T, ^{6}Li(n,t)α, ^{10}B(n,α_0)^{7}Li, and ^{10}B(n,α_1)^{7}Li*(478-keV γ) reactions have positive Q values and large thermal cross sections which make them ideal to use in neutron flux monitors. The Yale phase shifts were used to generate the hydrogen elastic scattering cross section and angular distributions while comprehensive R-matrix analyses were performed to determine the ^{6}Li and ^{10}B cross sections.

I.   INTRODUCTION

This report describes several of the light element standard cross-section evaluations that are included in Version IV of ENDF/B.[1] It is limited to those reactions for which the Los Alamos Scientific Laboratory has the primary responsibility and is intended as a supplement to an earlier but less detailed report by Magurno[2] which includes all of the Version IV standards.

The main criteria for the choice of a standard cross section are that it be a smooth function of energy and well determined experimentally; in addition, the response function of the detector in which the cross section is employed assumes great importance. While positive Q reactions enhance detector response functions, they also produce very large low-energy backgrounds. Therefore, neutron sources and geometry must be chosen with great care.

Elastic neutron scattering from hydrogen, for which the cross section is essentially equal to the total cross section above a few eV, is the only reaction which satisfies the criterion of smoothness over the entire energy range to 20 MeV. Unfortunately, however, the hydrogen recoil does not have enough energy to produce a useful response[*] at low-incident neutron energies in most detector configurations, and positive Q reactions must be employed in flux monitors below a few keV. The light-element standard evaluations for ENDF/B-IV described in this report are listed in Table I along with a few of their important properties.

TABLE I

Reaction	Mat#	Standard	Q-Value (MeV)	Recommended Energy Range
^{1}H(n,n)^{1}H	1269	$\begin{cases} \sigma_{elas}(E_n) \\ \sigma_{elas}(E_n,\theta_n) \end{cases}$	0	1 keV–20 MeV
^{3}He(n,p)T	1146	$\sigma_{n,p}(E_n)$	+ 0.7645	thr. – 1 MeV
^{6}Li(n,t)^{4}He	1271	$\sigma_{n,t}(E_n)$	+ 4.786	thr. – 100 keV
^{10}B(n,α)^{7}Li	1273	$\sigma_{n,\alpha}(E_n)$	+ 2.790	thr. – 100 keV
^{10}B(n,$\alpha_1\gamma$)^{7}Li	1273	$\sigma_{n,\alpha_1\gamma}(E_n)$	+ 2.312	thr. – 100 keV

II. ^{1}H(n,n)^{1}H ELASTIC SCATTERING CROSS SECTION AND ANGULAR DISTRIBUTION

The elastic and total cross sections for hydrogen are essentially equal above a few eV, and the total cross section is the best known and most often recommended of the standard cross sections. It satisfies the most important requirements for standards in that $\sigma(E_n)$ shows no structure up to 20 MeV, the cross section is well known, the scattering is isotropic in the center-of-mass system (±4%) up to 20 MeV, and hydrogen is relatively easy to incorporate into various counter types.

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[*] The 2.2-MeV γ from the ^{1}H(n,γ)D reaction is sometimes used in a flux monitor instead of the recoil proton thereby taking advantage of a positive Q reaction to employ a hydrogen counter at low energies. A discussion of this reaction, however, is not included in this report.

The extensive theoretical analysis of fast-neutron measurements by Hopkins and Breit[3] was used to generate the scattering cross section and angular distributions of the neutrons for the ENDF/B-IV file.[4] The code and the Yale phase shifts[5] were obtained from Hopkins[6] in order to obtain the data on a fine-energy grid. Pointwise angular distributions were produced to improve the precision over that obtained from the published Legendre coefficients.* The phase shifts were also used to extend the energy range down below 200 keV as represented in the original paper.[3]

At 100 eV, the elastic cross section calculated from the phase shifts is 20.449 barns, in excellent agreement with the thermal value of 20.442 derived by Davis and Barschall.[7] Therefore, for the ENDF/B-IV evaluation, the free-atom scattering cross section is assumed to be constant below 100 eV and equal to the value calculated from the Yale phase shifts at 100 eV giving a thermal cross section of 20.449 b.

Total cross-section measurements are compared with the evaluation in Fig. 1 for the energy range from 10 eV to 0.5 MeV. Similarly, Figs. 2 and 3 compare the evaluation with measured data from 0.5 to 20 MeV. The agreement with the earlier experiments shown in Fig. 2 is quite good over the entire energy range. The 1969 data of Schwartz[42] included in Fig. 3, however, lie slightly below the evaluation over most of the energy range even though agreement with the 1972 results of Clement[43] is quite acceptable.

Unfortunately, few absolute values of the angular dependence of the neutrons (or recoil protons) exist and even the relative measurements are often restricted to less than half of the angular range. The experiment of Oda[24] at 3.1 MeV is not atypical of the earlier distributions which, as shown in Fig. 4, does not agree with the phase-shift predictions. Near 14 MeV, the T(d,n) neutron source has been employed in many experiments to determine the angular distributions. A composite of these measurements is compared with ENDF/B-IV in Fig. 5A. Note that most of the experiments are in reasonable agreement on a relative scale, but 10% discrepancies frequently appear among the data sets. The measurements of Cambou[50] average more than 5% lower than the predicted curve and differences of 5% or more are occasionally apparent among the data of a single set. Figure 5B

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*For E_n = 30 MeV, the difference in the 180° cross section is ~ 1% as calculated from the Legendre coefficients[3] compared to that calculated from the phase shifts.
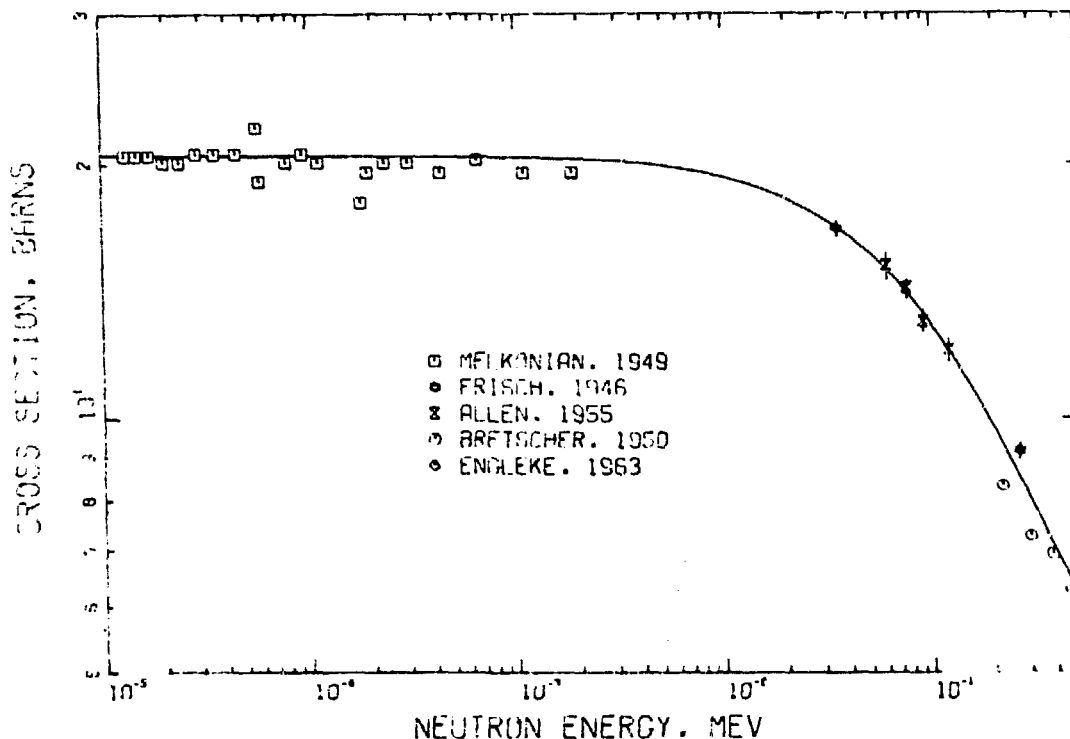
3

Fig. 1.
Total cross section for hydrogen from 1×10^{-5} eV to 500 keV. The
ENDF/B-IV evaluation is compared to the measurements of Refs. 8-12.

shows the measurements of Galonsky[51] at 17.9 MeV compared with the evaluation.
Again, the agreement on an absolute basis is quite poor.

Elastic scattering angular distributions at 0.1, 5, 10, 20, and 30 MeV are
provided in Ref. 1 as Legendre expansion coefficients. Using the Hopkins-Breit
phase-shift program and the Yale phase shifts, additional and intermediate en-
ergy points were calculated for the Version IV evaluation.[4] As shown in Figs.
5-16 of Ref. 4, the angular distributions are neither isotropic below 10 MeV
nor symmetric about 90° above 10 MeV as assumed in earlier evaluations. In this
evaluation, the angular distribution at 100 keV is assumed to be isotropic since
the calculated 180°/0° ratio is very nearly unity, that is, 1.0011. At 500 keV,
this ratio approaches 1.005. Therefore, the pointwise normalized probabilities
as a function of the center-of-mass scattering angle are provided at the follow-
ing energies: 10^{-5} eV (isotropic), 100 keV (isotropic), 500 keV, and at 1-MeV
intervals from 1 to 20 MeV.

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(A)

CROSS SECTION, BARNS

☒ ALLEN, 1955
◊ BRETSCHER, 1950
◆ BAILEY, 1946
✕ LAMPI, 1949
⊠ WAY, 1941
Y HAMERMESH, 1950
✱ FIELDS, 1954
■ ... 1954
△ FOSTER, 1967
▲ FIELDS, 1953
✧ ENGELKE, 1965
⊛ ZINN, 1939
⋈ NERESON, 1954

(B)

CROSS SECTION, BARNS

10²

△ FOSTER, 1967
⋈ OBA, 1950
⊙ BRETSCHER, 1950
⋈ NERESON, 1954
↪ ENGELKE, 1963
◆ BAILEY, 1946
↳ HAMERMESH, 1953
⊙ CLEATOR, 1947
▼ BRATENAHL, 1957
⋉ LASDAY, 1951
➤ GOODMAN, 1952
⋈ POSS, 1951
⊞ TANAKA, 1970
⊙ BATTAT, 1959

◇ ALLRED, 1953
✦ COOK, 1954
✕ POSS, 1952
⊠ BOWEN, 1961
Y PETERSON, 1960
✕ GROCE, 1966
✱ WEST, 1965
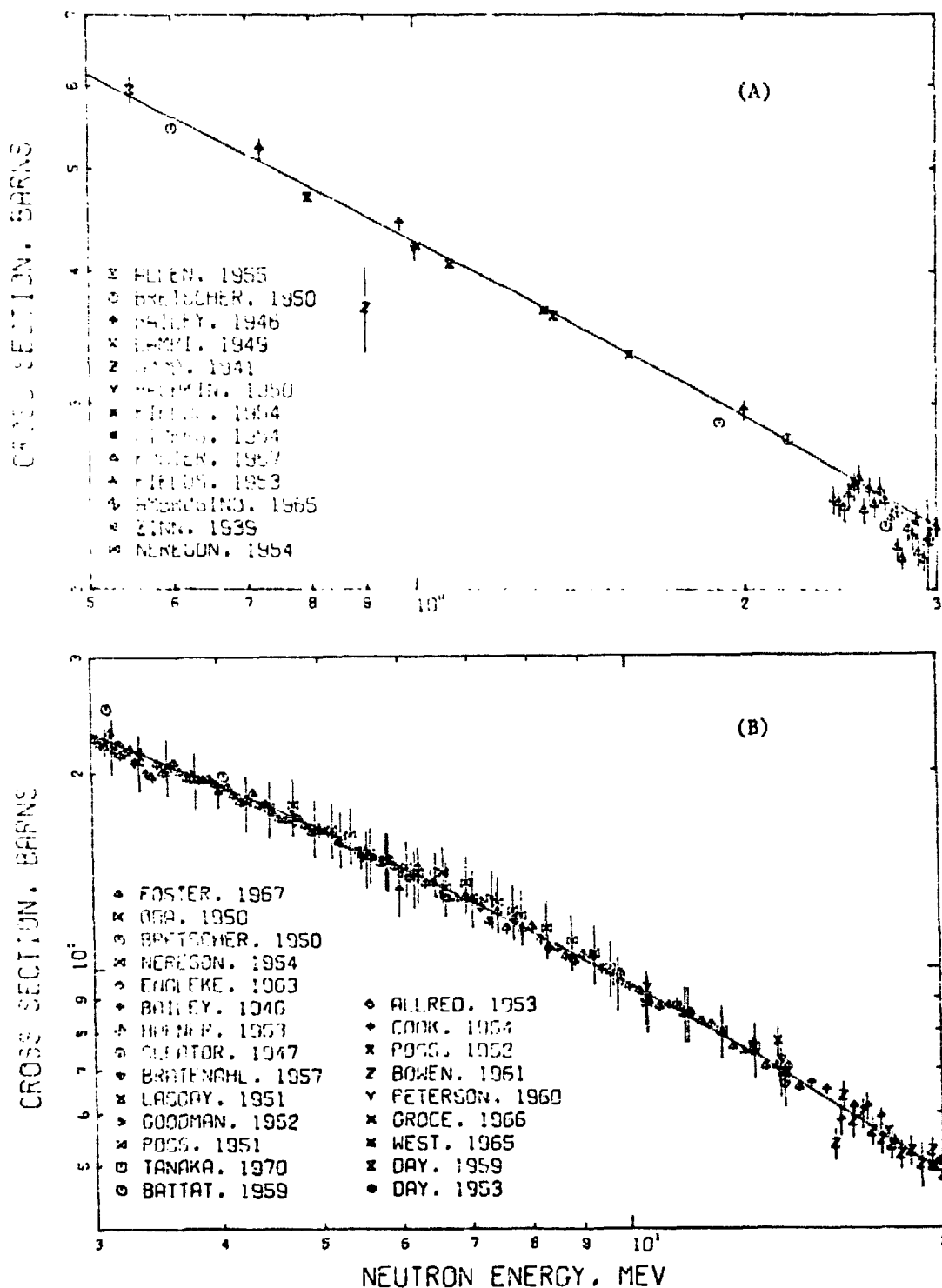⊠ DAY, 1959
● DAY, 1953

NEUTRON ENERGY, MEV

Fig. 2.
Total cross section for hydrogen from 500 keV to 20 MeV. The ENDF/B-IV
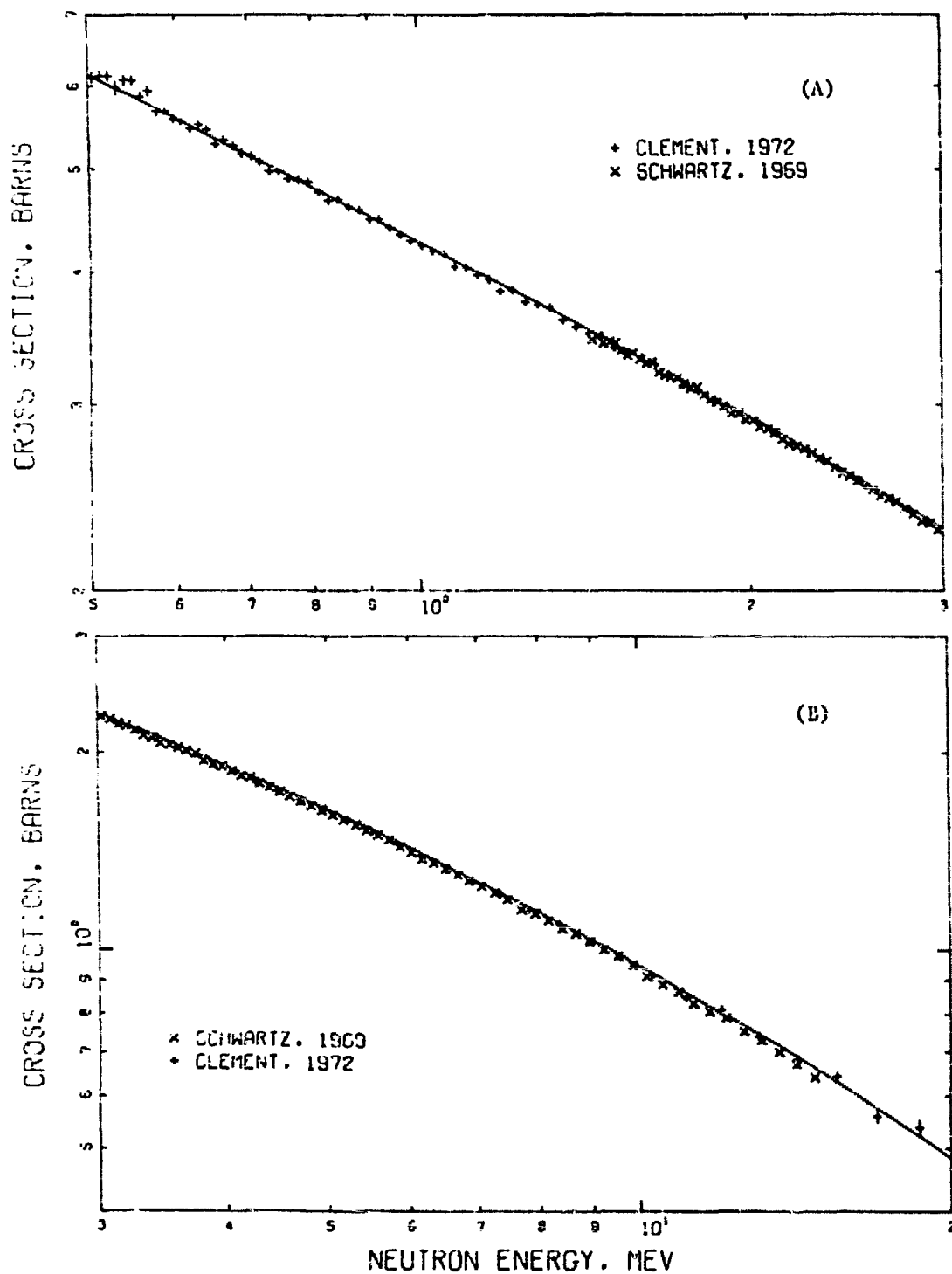evaluation is compared to measurements reported in Refs. 10-41.

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Fig. 3.
Total cross section for hydrogen from 500 keV to 20 MeV. The ENDF/B-IV evaluation is compared to measurements reported in Refs. 42 and 43.
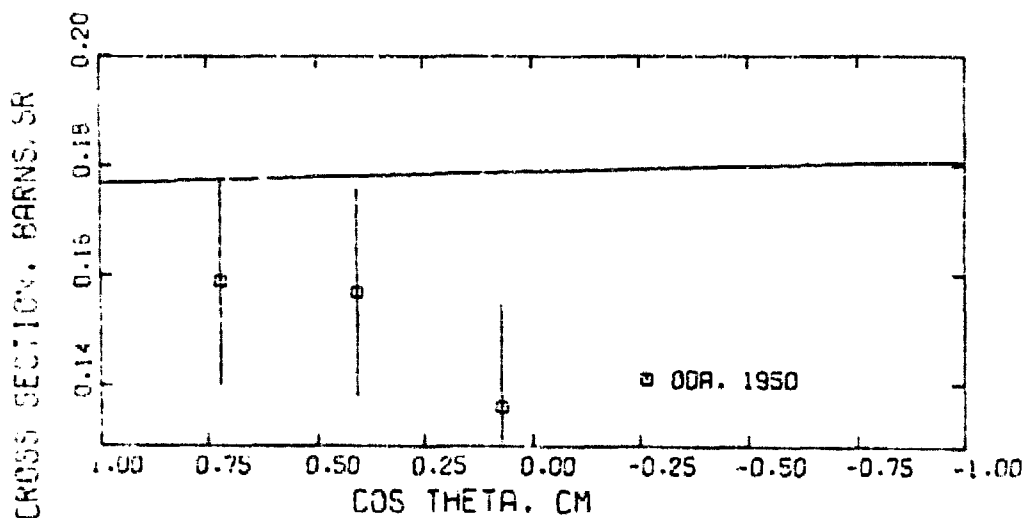
Fig. 4.
Angular distribution of the neutrons elastically scattered
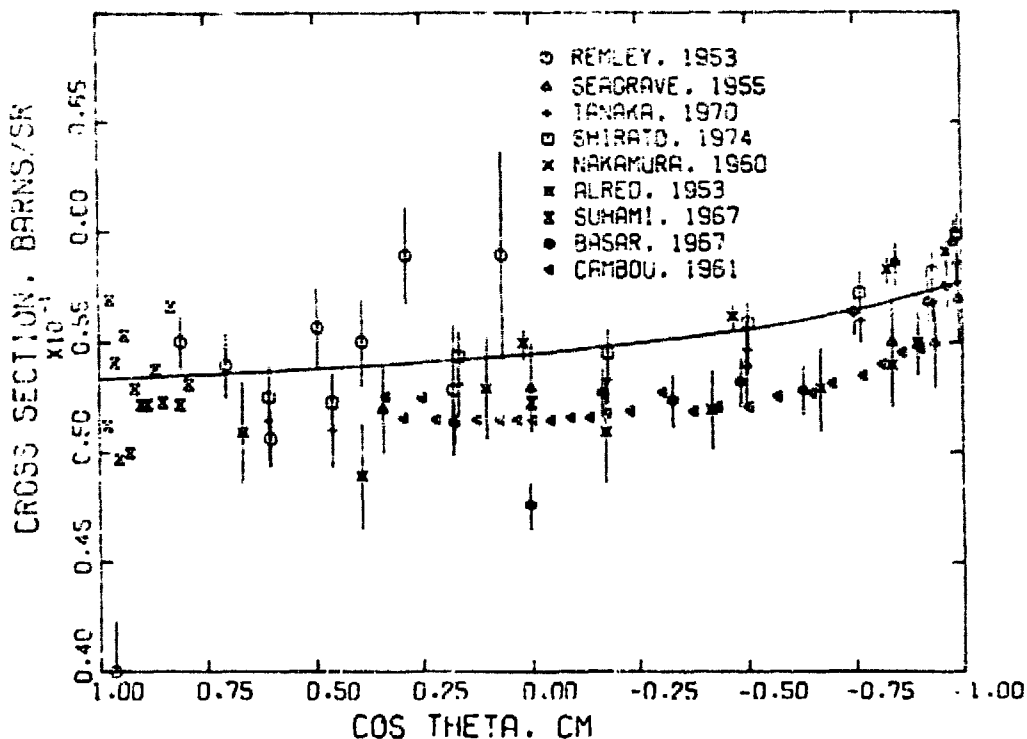from hydrogen at 3.1 MeV. ENDF/B-IV is compared with the
experimental values of Oda.[24]

Fig. 5A.
Angular distribution of the neutrons elastically scattered from
hydrogen at energies near 14 MeV. The experimental data shown
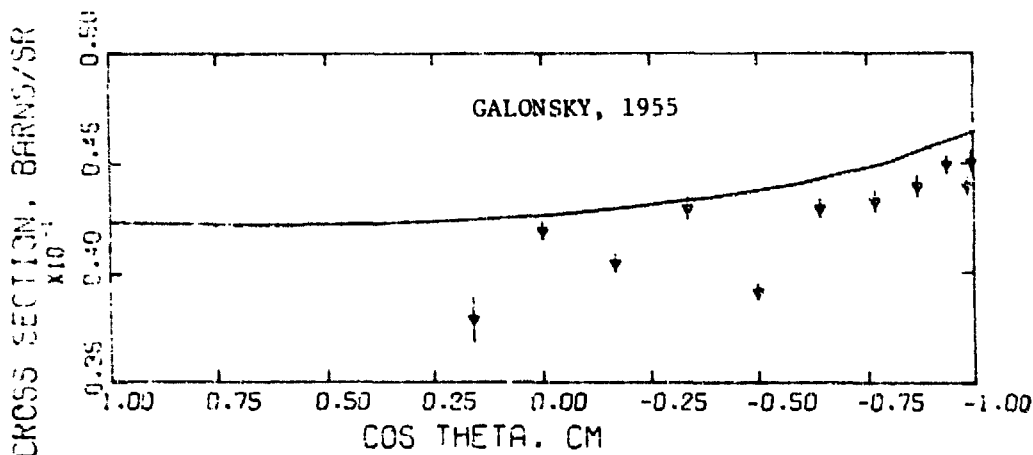were reported in Refs. 31, 33 and 44-50.

7

Fig. 5B.
Angular distribution of the neutrons elastically scattered from
hydrogen at energies near 17.8 MeV. The experimental data shown
were reported in Ref. 51.

Certainly the Hopkins-Breit phase shifts reproduce reasonably well the
measured angular distributions near 14 MeV. It is important, however, that
experiments be made at two or three energies which would, hopefully, further
corroborate this analysis. Near 14 MeV, the energy-dependent total cross sec-
tion is presently assumed to be known to ~ 1% and the angular distribution to
~ 2-3%. At lower energies where the angular distributions approach isotropy,
the error estimate on the angular distribution is less than 1%.

It should be pointed out that errors involved in using hydrogen as a stan-
dard depend upon the experimental techniques employed and therefore may be sig-
nificantly larger than the errors placed on the standard cross section. The
elastic angular distribution measurements of neutrons scattered by hydrogen,
which are available today, seem to indicate that $\sigma(\Theta)$ is difficult to measure
with the precision ascribed to the reference standard. If this is the case,
then the magnitude of the errors in the $\sigma(\Theta)$ measurements might be indicative of
error assignments which should be made on hydrogen flux monitors. That is, it
is difficult to assume that hydrogen scattering can be implemented as a standard

with much higher precision than it can be measured. Even though better agreement with many past measurements can be reached by renormalizing the absolute scales, such action may not always be warranted.

At this time, no attempt has been made to estimate the effect of errors on the energy scale in ENDF/B. It is clear, however, that a small energy shift would produce a large change in the cross section, especially at low energies. For example, a 50-keV shift in energy near 1 MeV would produce a change in the standard cross section of approximately 2½%. Therefore, precise determination of the incident neutron energy and the energy spread could be very important in employing hydrogen as a cross-section standard, depending upon the experimental technique.

III. ^{3}He(n,p)T CROSS SECTION

The ENDF/B-IV evaluation was performed in 1968 and accepted by the CSEWG Standards Subcommittee for the ENDF/B-III file[52] in 1971. No changes have been recommended for this file; therefore ENDF/B-IV was carried over from ENDF/B-III. This standard is recommended for use up to approximately 1 MeV.

The thermal cross section of 5327 b was derived from precise measurements by Als-Nielsen and Dietrich[53] of the total cross section up to an energy of 11 eV. No experimental measurements on the ^{3}He(n,p) reaction are available below ~ 5 keV, and the cross section was assumed to follow 1/v up to 1.7 keV. The evaluation is compared with the available data below 10 keV in Fig. 6. For convenience, the inset includes tabular values of the elastic, (n,p) and total cross sections at a few energies up to 1 keV.

Up to 10 keV, the evaluation is a reasonable representation of the 1966 results of Gibbons and Macklin[54] and an average of their cross sections measured in 1963.[55] These experiments, which extend to 100 keV, are compared with ENDF/B-IV in Fig. 7.

From 100 keV to 1 MeV, additional experiments are available. The evaluation is heavily weighted by the data of Refs. 54 and 55 and the cross sections of Perry et al.[56] as given in Fig. 8. Note that these three measurements are in good agreement among themselves but are higher than the measurements of Batchelor et al.[57] and of Sayres et al.[58] On the other hand, Sayres et al. measure an elastic cross section much higher than reported by Seagrave et al.[59] (noted on the same figure).
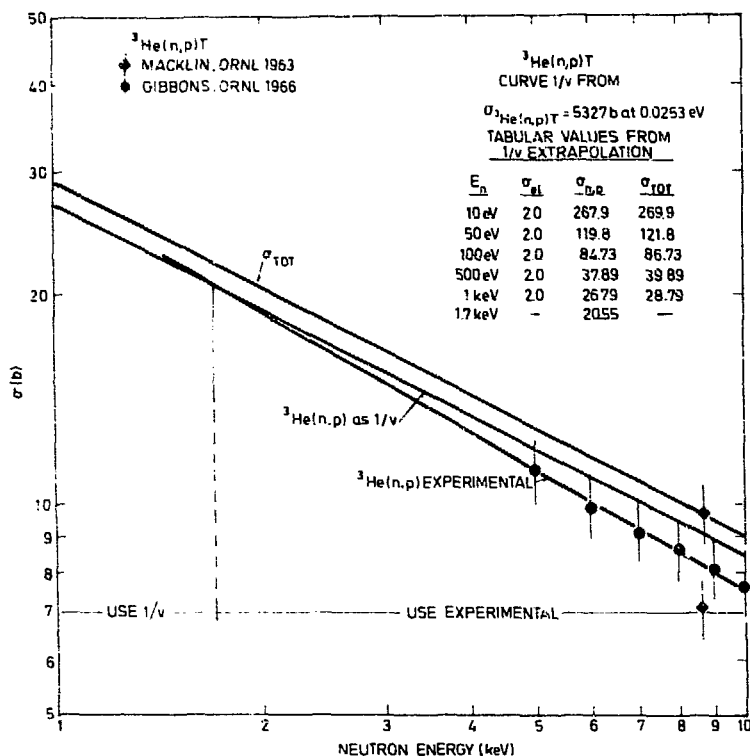
Fig. 6.
The (n,p) and total cross sections for ^{3}He from 1
to 10 keV. The curve drawn through the experimen-
tal points deviates from 1/v at 1.7 keV.

In 1970, Costello et al.[60] measured the (n,p) cross section from 300 keV
to 1 MeV and obtained essentially a constant value of 900 mb over this energy
range. Agreement of the Costello data with this evaluation above 500 keV is
excellent, although from 300 to 400 keV, their measurements are more than 10%
lower than ENDF/B-IV.

Finally, Lopez et al.[61] measured the relative ratio of the counting rates
between ^{3}He and BF_3 proportional counters from 218 eV to 521 keV. To provide a
comparison between these two standard cross sections, the Lopez ratios were
normalized at 218 eV to the Version IV ratios. Then, by using this evaluation
for the ^{3}He(n,p) cross section to convert the Lopez ratio measurements to ^{10}B
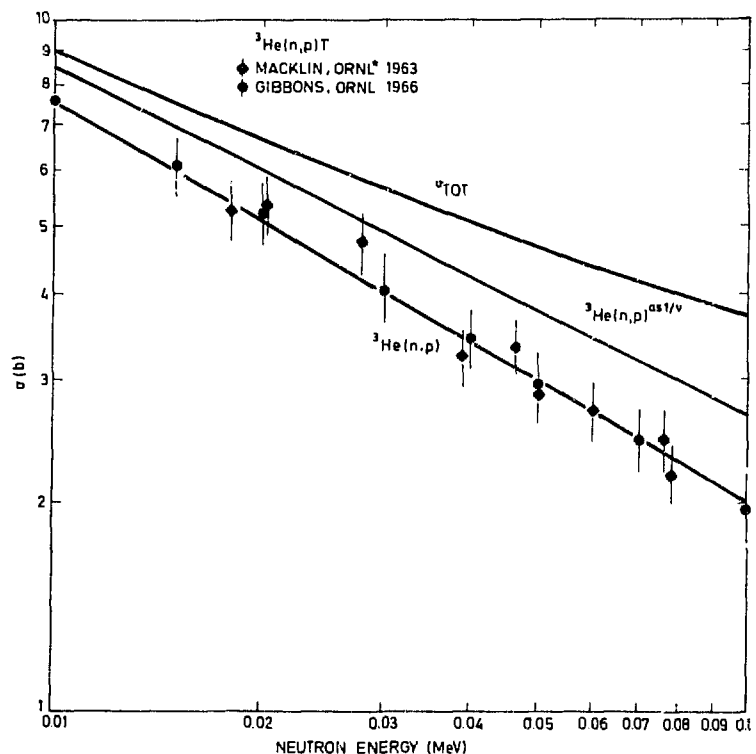cross sections, reasonable agreement with Version IV ^{10}B(n,α) is obtained.

Fig. 7.

The (n,p) and total cross sections for ^{3}He from 10 to 100 keV.
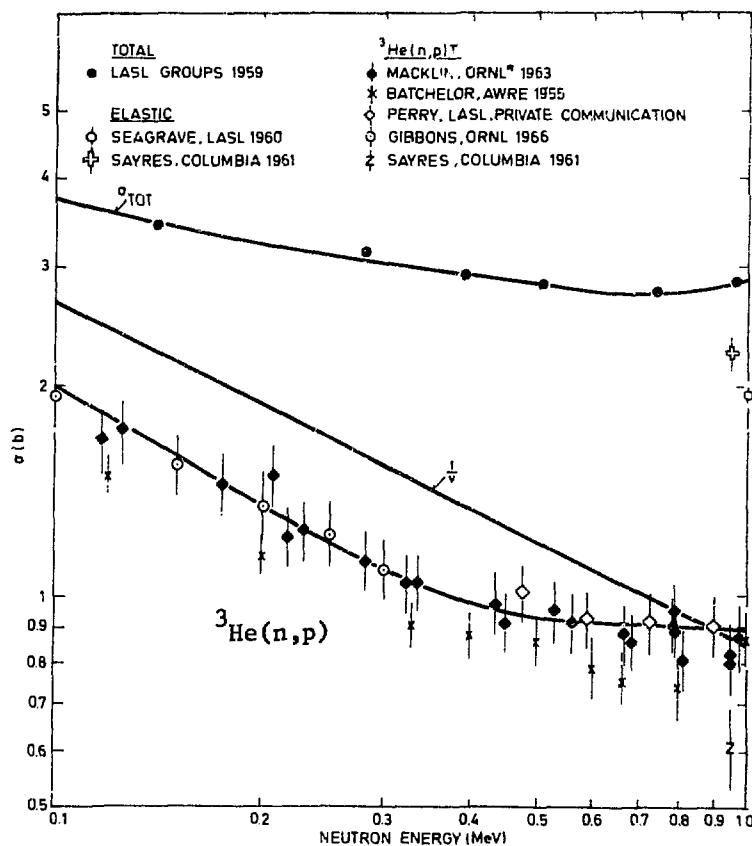

Fig. 8.

The (n,p), elastic, and total cross sections for ^{3}He from 100 keV to 1 MeV. The Costello data[60] have been omitted for the sake of clarity.

It should be noted, however, that the energy points are too sparse above a few keV to reproduce the structure observed in ^{10}B.

Although the thermal (n,p) cross section is known to better than 1%, the energy at which this cross section deviates from 1/v is not well established. It should also be emphasized that experiments have not been carried out from 11 eV to a few keV, thereby placing severe restrictions upon the accuracy accompanying the use of the ^{3}He(n,p)T cross-section standard. The 10% error estimates on the ORNL experimental data are directly related to the uncertainties in the analysis of the target samples employed. Certainly, further absolute measurements are needed on this cross-section standard, especially above ~ 100 eV.

IV. ^{6}Li(n,α)t CROSS SECTION

In the region below E_n = 1.7 MeV, the ^{6}Li(n,α) cross-section evaluation is based on a comprehensive R-matrix analysis of reactions in the ^{7}Li system. The R-matrix formalism[62] is well suited for describing reactions in this system, since it accounts for both the 1/v behavior and resonance structure of the cross sections. Furthermore, the cross sections from such an analysis satisfy general physical constraints imposed by unitarity, causality, and conservation of total angular momentum and parity.

Data from the reactions ^{6}Li(n,n)^{6}Li, ^{6}Li(n,α)T, and ^{4}He(t,t)^{4}He at energies corresponding to E_n below 1.7 MeV, were fitted simultaneously using the multi-channel, multilevel R-matrix analysis code, EDA.[63] Starting from the usual parameters of the R matrix, eigenvalues ε_λ, reduced width amplitudes $\gamma_{\lambda c}$, and channel radii a_c, the code calculates unitary collision-matrix elements in accordance with general relations given by Lane and Thomas,[64] then forms experimental observables for each reaction using the M-matrix trace formalism of Wolfenstein.[65] An automated search algorithm adjusts the resonance parameters to achieve a "best fit" to all the data included in the analysis in a least-squares sense. Quantities specifying the two-body channels of the ^{7}Li system considered in this analysis are given in Table II.

The types of data considered for each reaction, along with references for the measurements included in the analysis, are listed in Table III. Starting values for the resonance parameters were chosen to accomodate all the known levels[87] in ^{7}Li below 10-MeV excitation energy, as well as distant-level contributions in each state. The fits obtained from searching over the resonance parameters are described briefly for each reaction below.

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TABLE II

CHANNEL QUANTITIES FOR THE ^{7}Li SYSTEM ANALYSIS

Channel	Channel Radius (f)	Channel Spin (s)	ℓ_{max}
n-^{6}Li	4.20	1/2, 3/2	1
t-α	4.02	1/2	4

TABLE III

DATA INCLUDED IN THE ^{7}Li SYSTEM ANALYSIS

Reaction	Data Type	References
^{6}Li(n,n)^{6}Li	σ_{int}	66, 67
	$\sigma(\theta)$	66, 67, 68, 69
	$P(\theta)$	69
^{6}Li(n,t)^{4}He	σ_{int}	70, 71, 72
	$\sigma(\theta)$	73
n-^{6}Li	σ_T	74, 75
^{4}He(t,t)^{4}He	$\sigma(\theta)$ (E_t = 1.7-11 MeV)	76, 77
	$P(\theta)$	78

A. ^{6}Li(n,n)^{6}Li

Calculated values of the elastic integrated cross section are shown in Fig. 9 and compared with the experimental data of Lane[66] and Knitter[67] in Fig. 9B. The 5/2$^-$ resonance at E_n = 250 keV, which dominates reactions in the ^{7}Li system in the keV range, is clearly evident in this cross section. Below the peak of the resonance, the R-matrix fit lies well above Lane's points, and agrees at low energies with measurements by Asami,[80] although these data were not included in the analysis. The shapes of the elastic angular distributions and polarizations are reproduced well by the calculations over the entire energy range.

B. ^{6}Li(n,t)^{4}He

The calculated value of the integrated cross section at thermal is 940 b., in exact agreement with the value obtained by Diment.[74] The 1/v dependence of
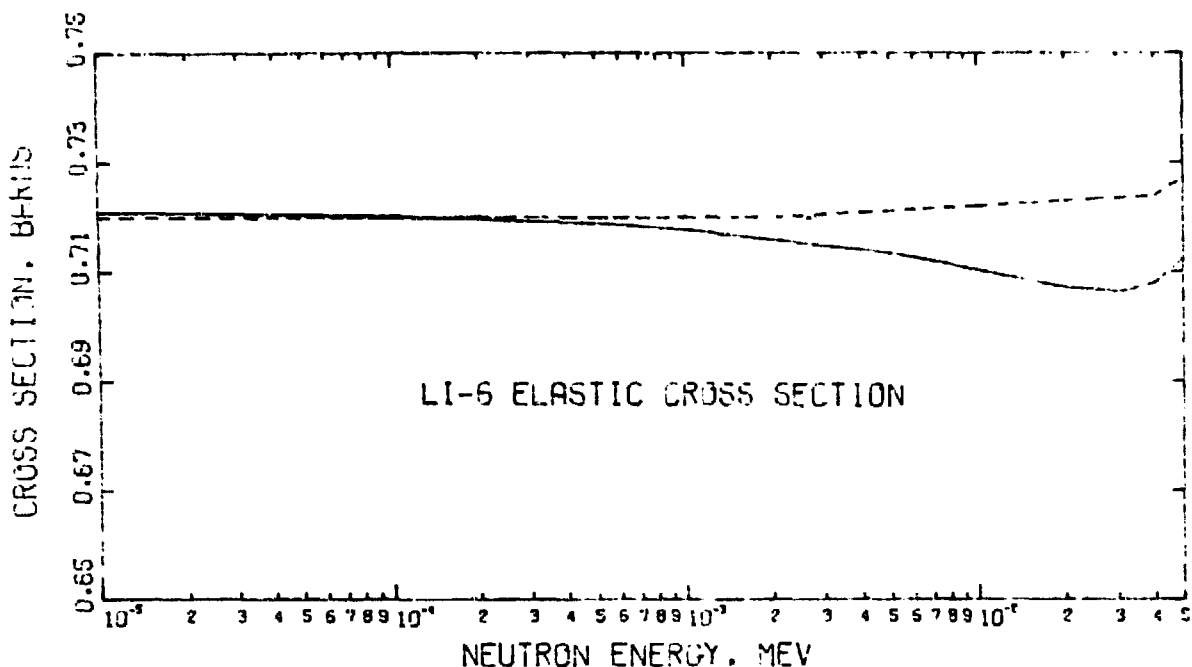
13

CROSS SECTION, BARNS (y-axis)
NEUTRON ENERGY, MEV (x-axis)

LI-6 ELASTIC CROSS SECTION

Fig. 9A.
$^6Li(n,n)^6Li$ integrated cross section for E_n between 10 eV and 50 keV. On this and all subsequent figures, the solid curve is ENDF/B-IV and the dashed curve is ENDF/B-III.

the calculated cross section at low energies comes from apparently distant-level contributions in both s-wave states, with the $J = 1/2$ transition contributing approximately 3 times the cross section of the $J = 3/2$ transition. Calculated and experimental data for neutron energies between 10 eV and 2 MeV are compared in Figs. 10A and 10B [note that the ordinate in Fig. 10A is $\sigma(E_n) \sqrt{E_n}$]. The calculations in the 1/v region agree well with the (n,α) $^6Li/^{10}B$ ratio measure- ments of Sowerby,[70] converted to $^6Li(n,\alpha)$ cross sections using the Version IV $^{10}B(n,\alpha)$. The calculated cross sections also agree well with Coates'[71] measure- ments below 35 keV, then rises to become 8% higher in the minimum at ~ 100 keV, and 20% higher at the peak of the $5/2^-$ resonance at 240 keV, as shown in Fig. 10B. On the back side of the resonance, the calculations remain slightly higher than Coates' values, following the measurements of Poenitz[72] and Fort[81] above 400 keV.

Thus, the resonance is broader and taller in the calculated cross section than in the measurements of Coates, though not as broad and tall as recent meas- urements of Friesenhahn[82] indicate. These differences between the calculated cross sections and the measurements, which involve shape as well as normalization,
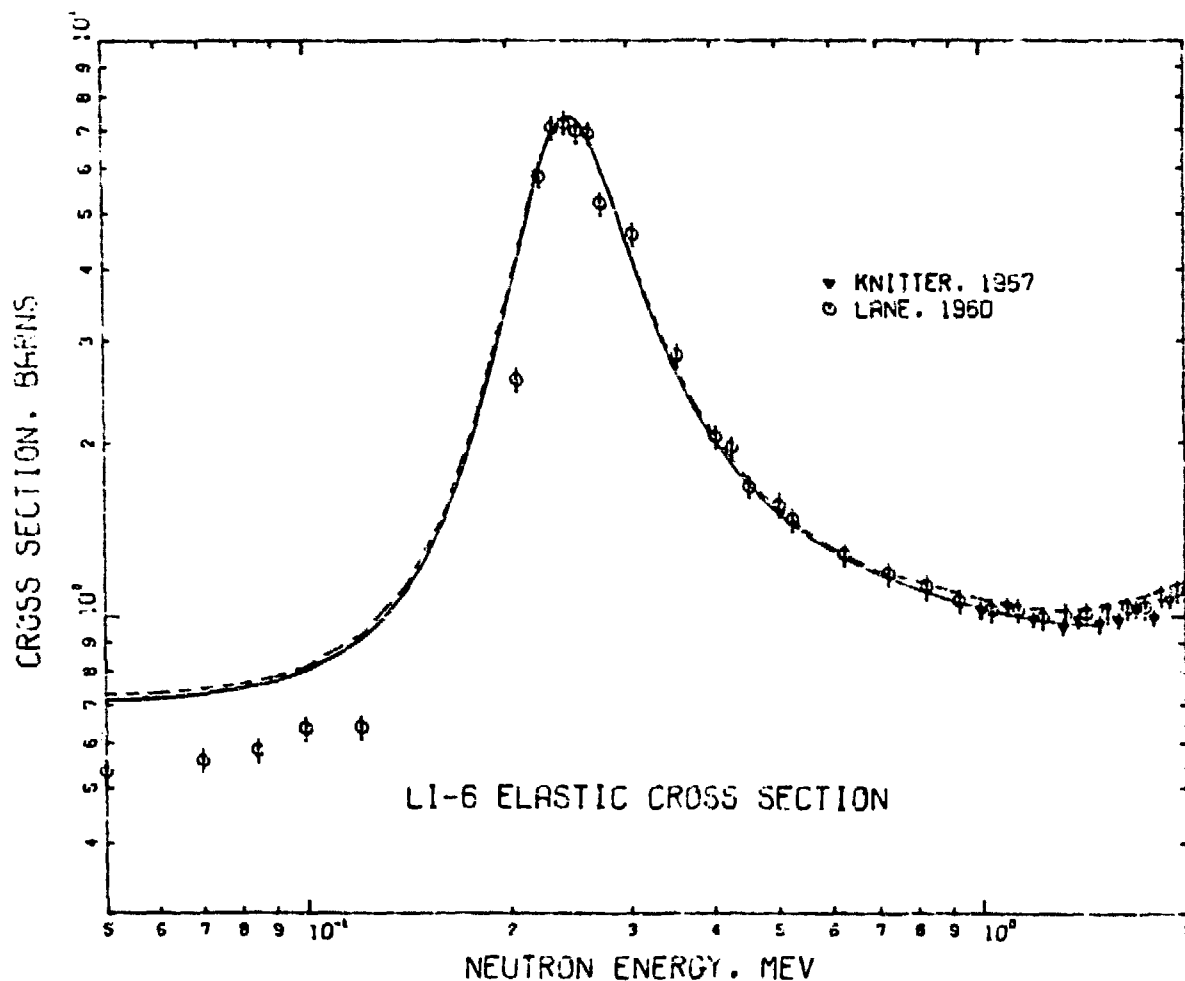
14

Fig. 9B.
$^6Li(n,n)^6Li$ integrated cross section for E_n between 50 keV and 2 MeV. The data are from Refs. 66 and 67.

appear to result from fitting simultaneously the precisely determined neutron total cross section described below.

C. $n-^6Li$, σ_T

The fit to the neutron total cross section from 10 eV to 2 MeV is shown in Fig. 11A and 11B. One sees that excellent agreement is obtained with measurements of Diment and Uttley.[74] This is partly due to the fact that these data were weighted heavily in the analysis by their small errors (typically ~ 1%). The energy of the resonance peak in the calculated total cross section is 247 keV, indicating that the experimentally observed ~ 7 keV shift relative to the
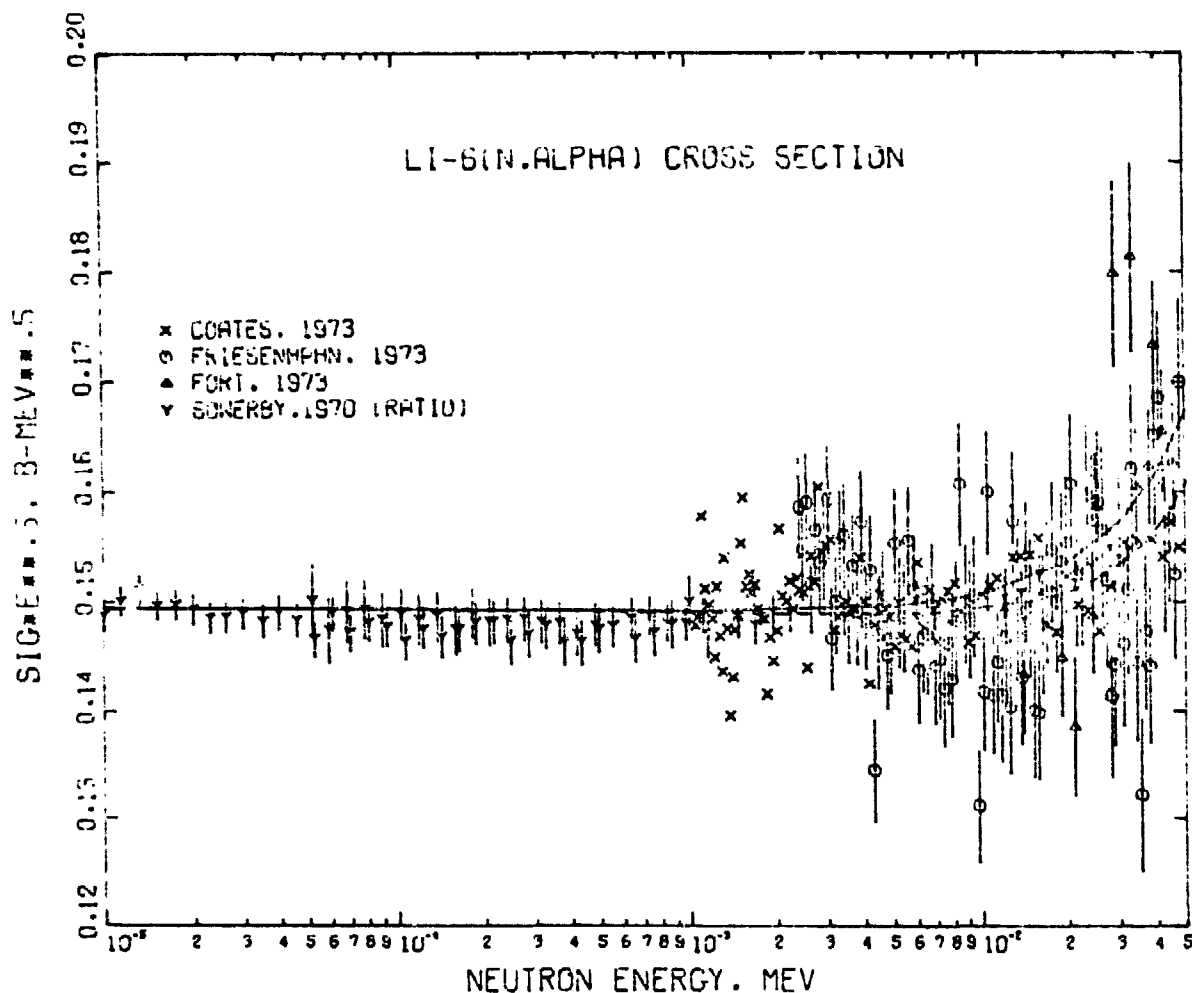
15

Fig. 10A.

The ^{6}Li(n,t)^{4}He integrated cross section for E_n in the range 10 eV to 50 keV. The data are from Refs. 70-71, and 81-82.

peak of the (n,t) cross section (240 keV) is real. In the calculations, this shift comes from interference of the resonant amplitude with the hard-sphere amplitude for elastic scattering, and with another 5/2$^-$ level just below the neutron threshold.

D. ^{4}He(t,t)^{4}He

Fits to a selection of differential cross-section and polarization measurements for ^{4}He(t,t) elastic scattering are shown in Fig. 12 to illustrate the consistency of the resonance parameters with the considerable structure evident in the data from this reaction. In particular, these data determine the parameters of most of the levels below the neutron threshold, and supply additional
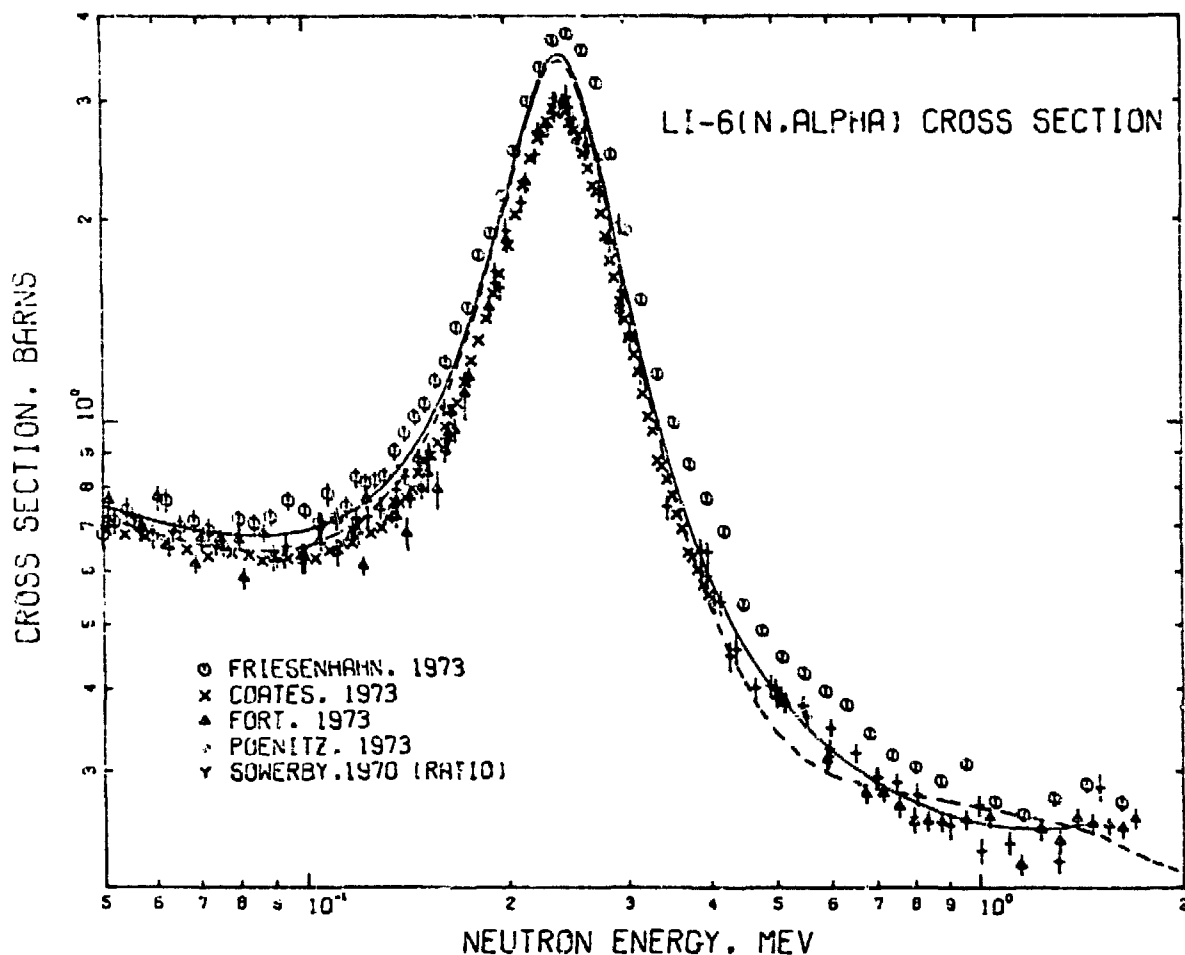
LI-6(N.ALPHA) CROSS SECTION

○ FRIESENHAHN. 1973
× COATES. 1973
▲ FORT. 1973
⚹ POENITZ. 1973
⍓ SOWERBY.1970 (RATIO)

CROSS SECTION. BARNS

NEUTRON ENERGY. MEV

Fig. 10B.

The ^{6}Li(n,t)^{4}He integrated cross section for E_n in the range 50 keV to 2 MeV.
The data are from Refs. 70-72, and 81-82.

constraints on the parameters of the important 5/2$^-$ resonance at 250 keV.
^{4}He(t,t) measurements in the region of 5/2$^-$ resonance available at the time this
analysis was performed were not sufficiently accurate, however, to influence the
fit nearly as much as did the neutron total cross section, for instance.

Although this analysis was completely independent of that used to provide
the Version III evaluation for ^{6}Li at low energies, the results obtained are
quite similar. This is because the results are highly constrained in both cases
by fitting the accurate total cross-section measurements of Diment. Our analysis
indicates that including the effects of all other known resonances and data from
other reactions still does not sufficiently relax the single-level nature of the
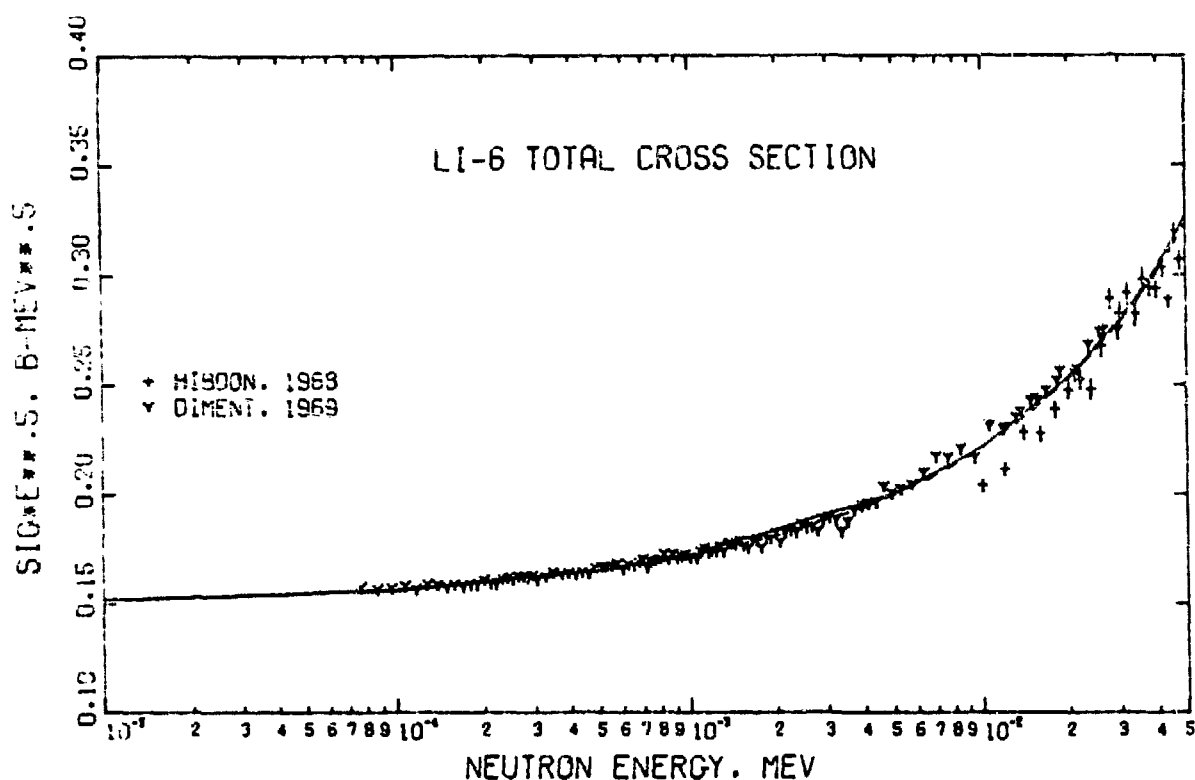
17

Fig. 11A.

The n-^{6}Li total cross section for E_n in the range 10 eV-50 keV. The data are from Refs. 74 and 83.

relationship among the cross sections near the 5/2$^-$ resonance to allow the apparent discrepancy between the total and reaction cross sections to be resolved. Therefore, we cannot be confident that the (n,t) cross section resulting from this analysis represents the "true" cross section to standards accuracy over the resonance.

Recent work at Los Alamos is directed at resolving this perplexing question by supplementing direct measurements of the neutron cross sections with accurate

Fig. 11B.

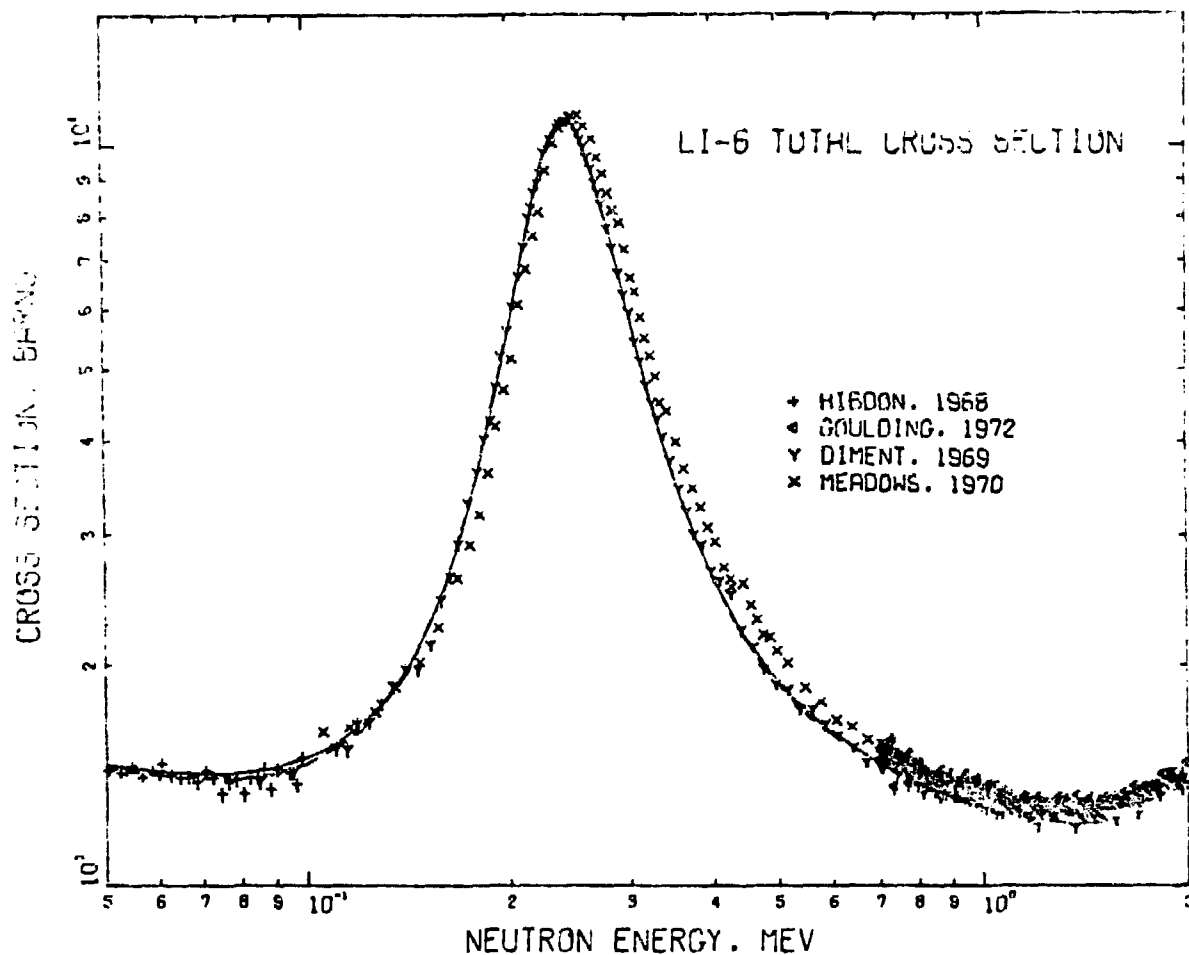The n-^{6}Li total cross section for E_n in the range 50 keV-2 MeV. The data are from Refs. 74, 75, 83, and 84.

charged-particle measurements for ^{4}He(t,t) scattering in the region of the res-onance. Preliminary results which include this information were reported[86] at the Washington Nuclear Cross Sections and Technology Conference, and new results will be available for Version V of ENDF/B.
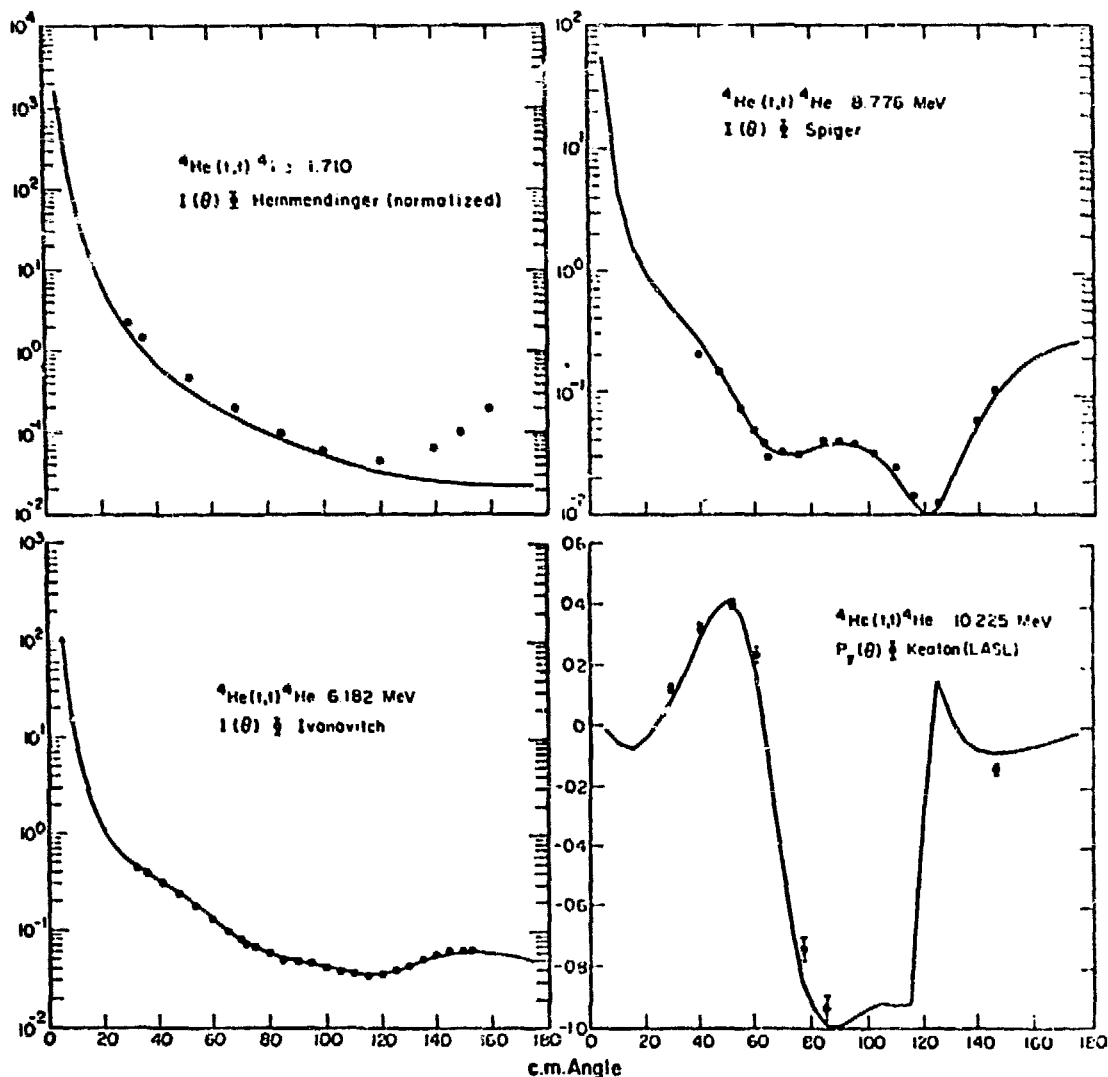
Fig. 12.

Representative fits to ^{4}He(t,t)^{4}He differential cross-section[76,77,85] and polarization[78] measurements for E_t in the range 1.7-10 MeV. The angular distribution at 8.776 MeV is close to the energy of the 5/2$^-$ resonance at $E_n \approx$ 250 keV. The units for I(θ) are b/sr.

V. $^{10}B(n,\alpha_0)^7Li$ AND $^{10}B(n,\alpha_1\gamma)^7Li^*$ CROSS SECTIONS

The $^{10}B(n,\alpha)$ cross section at low energies ($E_n < 1.0$ MeV) is based on a comprehensive R-matrix analysis of reactions in the ^{11}B system, similar to that described in the previous section for ^7Li. The two-body channel specifications used for this system are given in Table IV.

TABLE IV

CHANNEL QUANTITIES FOR THE ^{11}B SYSTEM ANALYSIS

Channel	Channel Radius (f)	Channel Spin (s)	ℓ_{max}
$n-^{10}B$	4.05	5/2, 7/2	1
$\alpha-^7Li(g.s)$	4.00	3/2	3
$\alpha-^7Li^*(0.478)$	6.17	1/2	3

Table V lists for each reaction the types of data considered, and references for the measurements included in the analysis.

TABLE V

DATA INCLUDED IN THE ^{11}B SYSTEM ANALYSIS

Reaction	Data Type	References
$^{10}B(n,n)^{10}B$	σ_{int}	87
	$\sigma(\theta)$, $P(\theta)$	87
$^{10}B(n,\alpha_0)^7Li$	σ_{int}	89, 90
	$\sigma(\theta)$	91
$^{10}B(n,\alpha_1)^7Li^*$	σ_{int}	92
$n-^{10}B$	σ_T	93
$^{10}B(n,\alpha_0+\alpha_1)$	σ_{int}	94
$^7Li(\alpha,\alpha)^7Li$	$\sigma(\theta)$ ($E_\alpha = 4-6$ MeV)	95, 96
$^7Li(\alpha,\alpha')^7Li^*$	σ_{int} ($E_\alpha = 3-5$ MeV)	97

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Starting values for the resonance parameters were based on current information about the level scheme[87,95,98] of ^{11}B. The fits obtained from searching over the resonance parameters are discussed briefly by reaction in the sections below.

A. ^{10}B(n,n)^{10}B

Two resonances are apparent in the elastic scattering data; a broad $7/2^+$ level which shows strongly in the integrated cross section at $E_n \approx 300$ keV, and a $5/2^-$ level which is evident in the differential cross-section and polarization data at 500 keV. Figure 13 shows that the fit to the integrated cross section reproduces the broad structure at 300 keV, and generally follows the data of Lane et al.[87] up to 1 MeV, although the calculated curve indicates a broader resonance than do Lane's data. Representative fits to the differential cross-section and polarization data are shown in Fig. 14. The change in the polarization from slightly negative at 375 keV to strongly positive at 850 keV indicates the presence of the $5/2^-$ level.
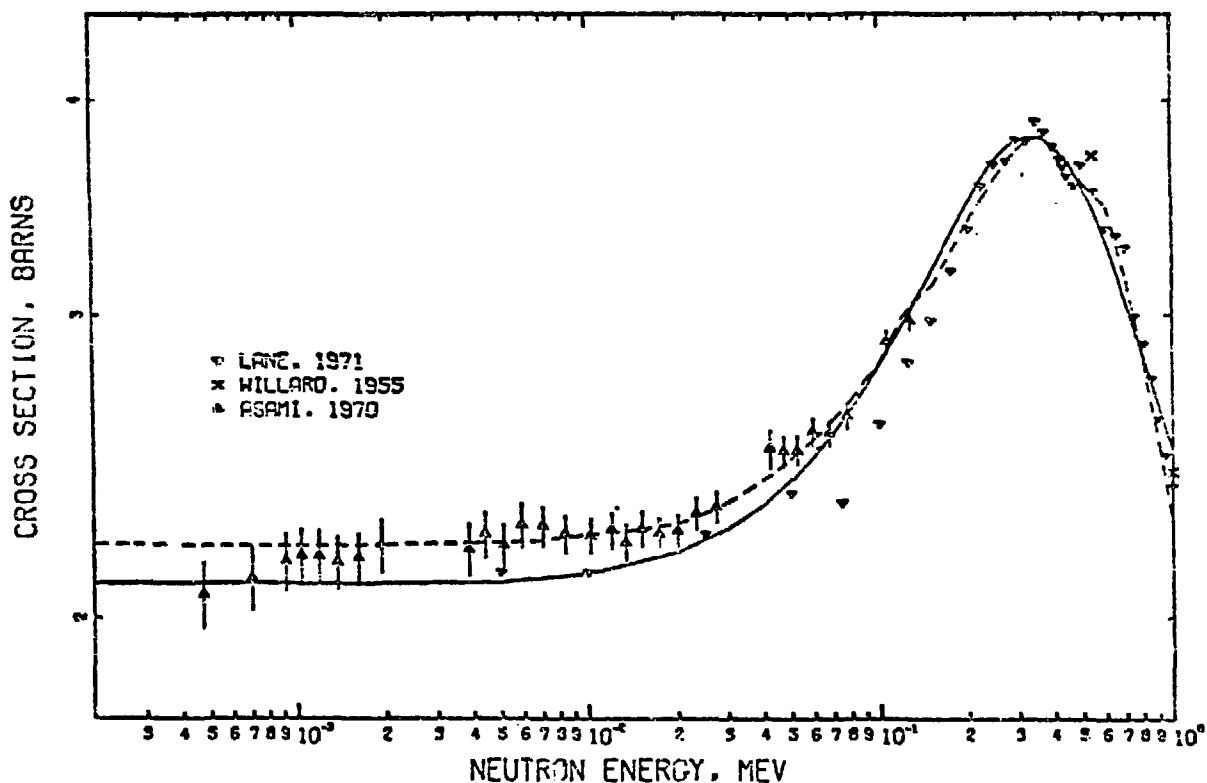

Fig. 13.
The ^{10}B(n,n)^{10}B integrated cross section for E_n between 0.2 keV and 1 MeV. The data are from Refs. 87, 88, and 99.
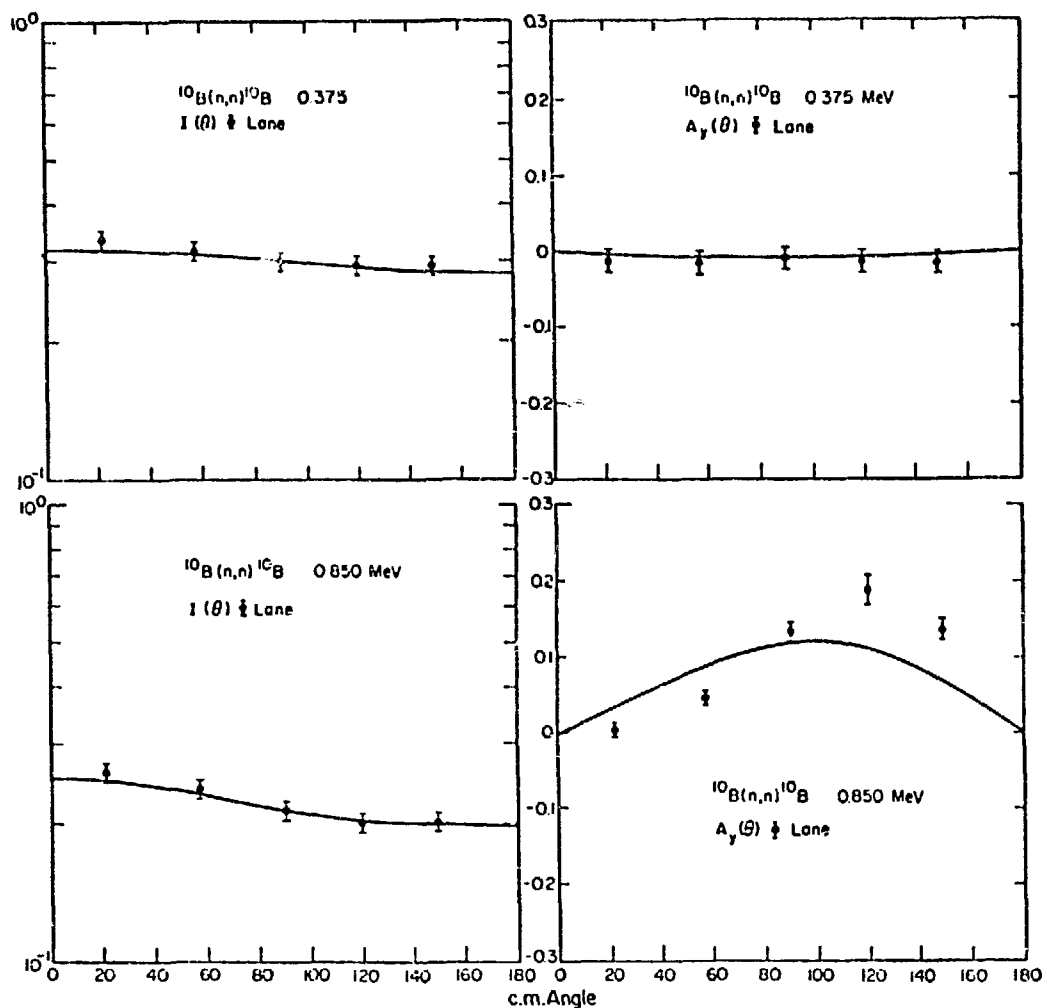
Fig. 14.
Representative fits to the $^{10}B(n,n)^{10}B$ differential cross section and polarization measurements of Lane[87] for E_n between 375 and 850 keV.

B. $^{10}B(n,\alpha_0)^7Li$ and $^{10}B(n,\alpha_1)^7Li^*$

The broad $7/2^+$ level evident in the elastic integrated cross section is largly responsible for the sizeable $1/v$ integrated cross section for these re-actions. However, significant departures from the $1/v$ dependence occur above 100 keV, particularly in the (n,α_0) cross section. One of these deviations is due to the $5/2^-$ resonance discussed previously, and another is tentatively at-tributed to a $5/2^+$ level occurring at $E_n \approx 250$ keV. Figures 15A and 15B show the R-matrix fit to the separate (n,α_0) and (n,α_1) integrated cross sections. The upper curve follows the measurements of Macklin and Gibbons[89] quite closely
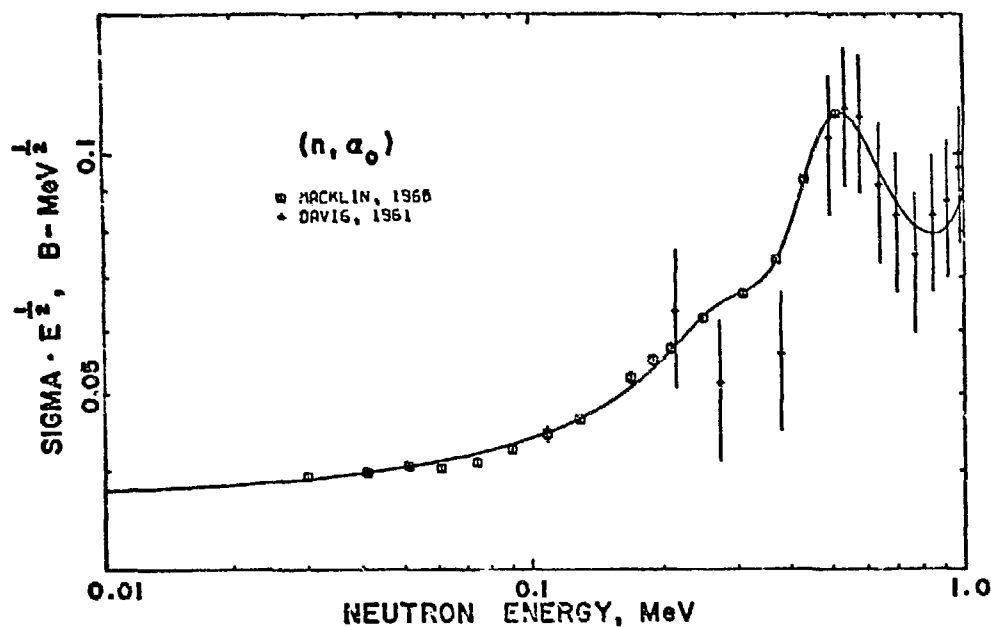
23

(n, α₀)

Fig. 15A.
The $^{10}B(n,\alpha_0)^7Li$ integrated cross section for E_n between 0.01 and 1 MeV. The data are from Refs. 89 and 90.

at the low energies, and those of Davis[90] above 500 keV. The lower curve agrees well with Friesenhahn's preliminary (n,α_1) data,[92] and follows the data of Davis above 500 keV. The calculated $^{10}B(n,\alpha_0+\alpha_1)$ cross section (Fig. 16) accurately reproduces the known thermal value of 3836.5 b., but does not pick up the detail of Mooring's measurements[94] in the 250–500 keV region. The fit to a selection of $^{10}B(n,\alpha_0)$ angular distributions measured by Van der Zwaan and Geiger[91] (actually for the inverse reaction) are shown in Fig. 17. The pronounced backward peaking of the angular distribution near 500 keV is due to the 5/2⁻ resonance.

C. $n-^{10}B$ σ_T

The calculated neutron total cross section is shown in Fig. 18 compared with various measurements. The agreement with Diment[93] is generally good, except at energies above 700 keV, where the calculated values approach more closely the measurements of Bockelman.[105]

D. $^7Li(\alpha,\alpha_0)^7Li$ and $^7Li(\alpha,\alpha_1)^7Li^*$

The $\alpha-^7Li$ reactions are considered in this analysis because they provide further unitary constraints on the neutron cross sections of interest, and because some of the resonances in this energy region show up prominently in these
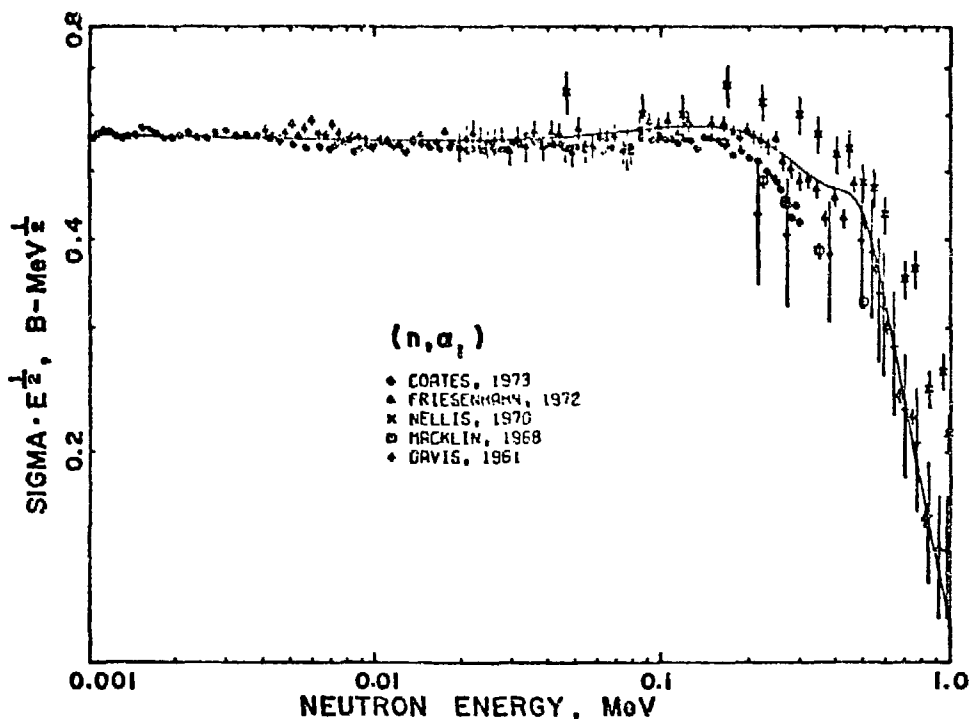
24

Fig. 15B.
The $^{10}B(n,\alpha_1)^7Li^*$ integrated cross section for E_n between
1 keV and 1 MeV. The data are from Refs. 71, 89, 90, 92,
and 100.

reactions. Figure 19 shows fits to some of the $^7Li(\alpha,\alpha)^7Li$ angular distributions measured by Cusson.[95] Although these fits follow the qualitative features of the angular distributions, calculated values of the integrated (α_0,α_1) cross section indicate possible deficiencies in the level structure that are not apparent from considering the neutron reactions alone.

Evaluated neutron cross sections resulting from this R-matrix analysis at low energies agree well in most cases with the neutron data that were included in the analysis. However, $^{10}B(n,\alpha)$ data[82,106] that became available soon after the evaluation was submitted for ENDF/B-IV differ substantially from those used in the analysis. With sufficient data to determine the correct level structure, this comprehensive R-matrix approach can be expected to give a consistent set of smoothed cross sections that are determined more accurately than the individual measurements. In this case, we feel that present uncertainties in the data and in the level parameters limit the accuracy of the evaluated cross sections to

25
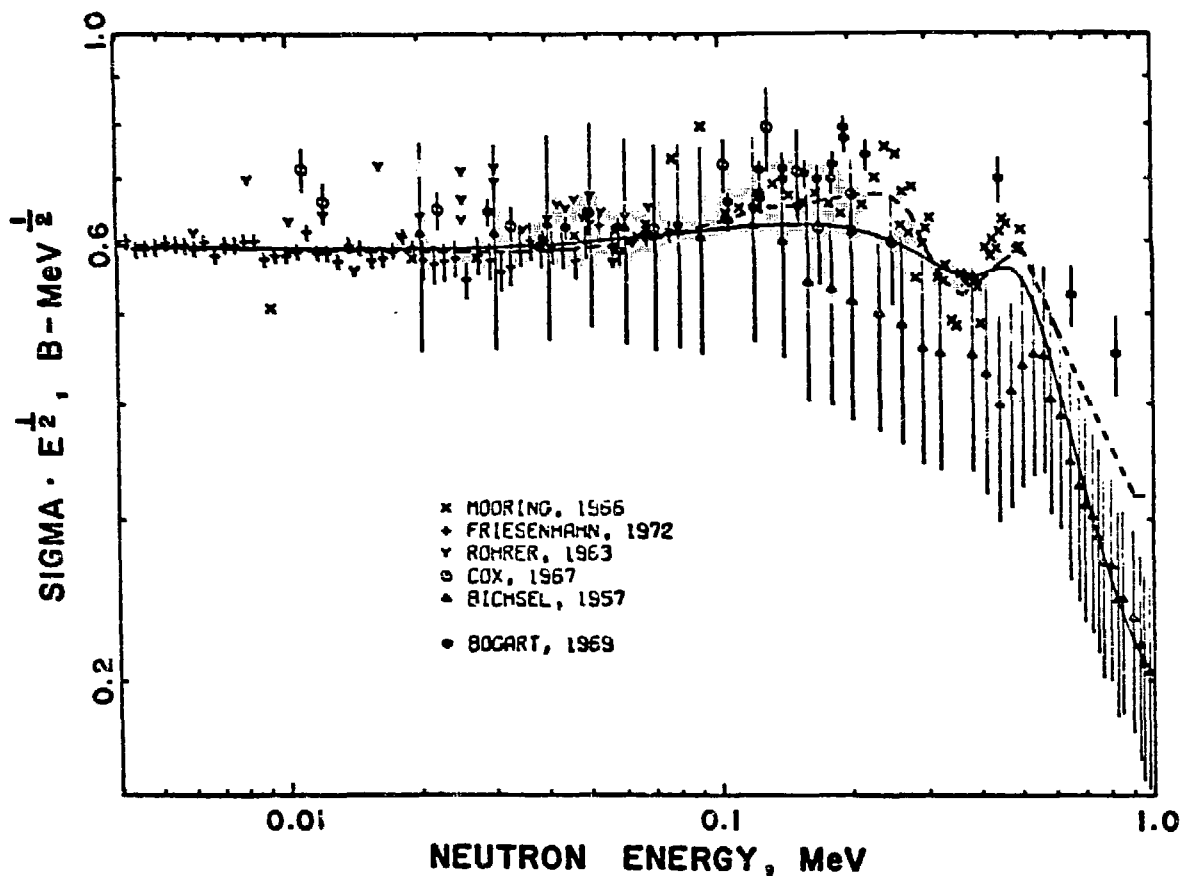
Fig. 16.
The summed $^{10}B(n,\alpha_0) + ^{10}B(n,\alpha_1)$ integrated cross section for E_n between 4 keV and 1. MeV. The data are from Refs. 92, 94, 97, and 101-103.

~ 5% for $\sigma_{n,n}$ and σ_T, and as much as 20% for $\sigma_{n,\alpha}$ in the region between 200 keV and 1 MeV. The thermal value is probably determined to better than 1%, however, with the uncertainty in the evaluated (n,α) cross section increasing to ~ 5% at 200 keV.
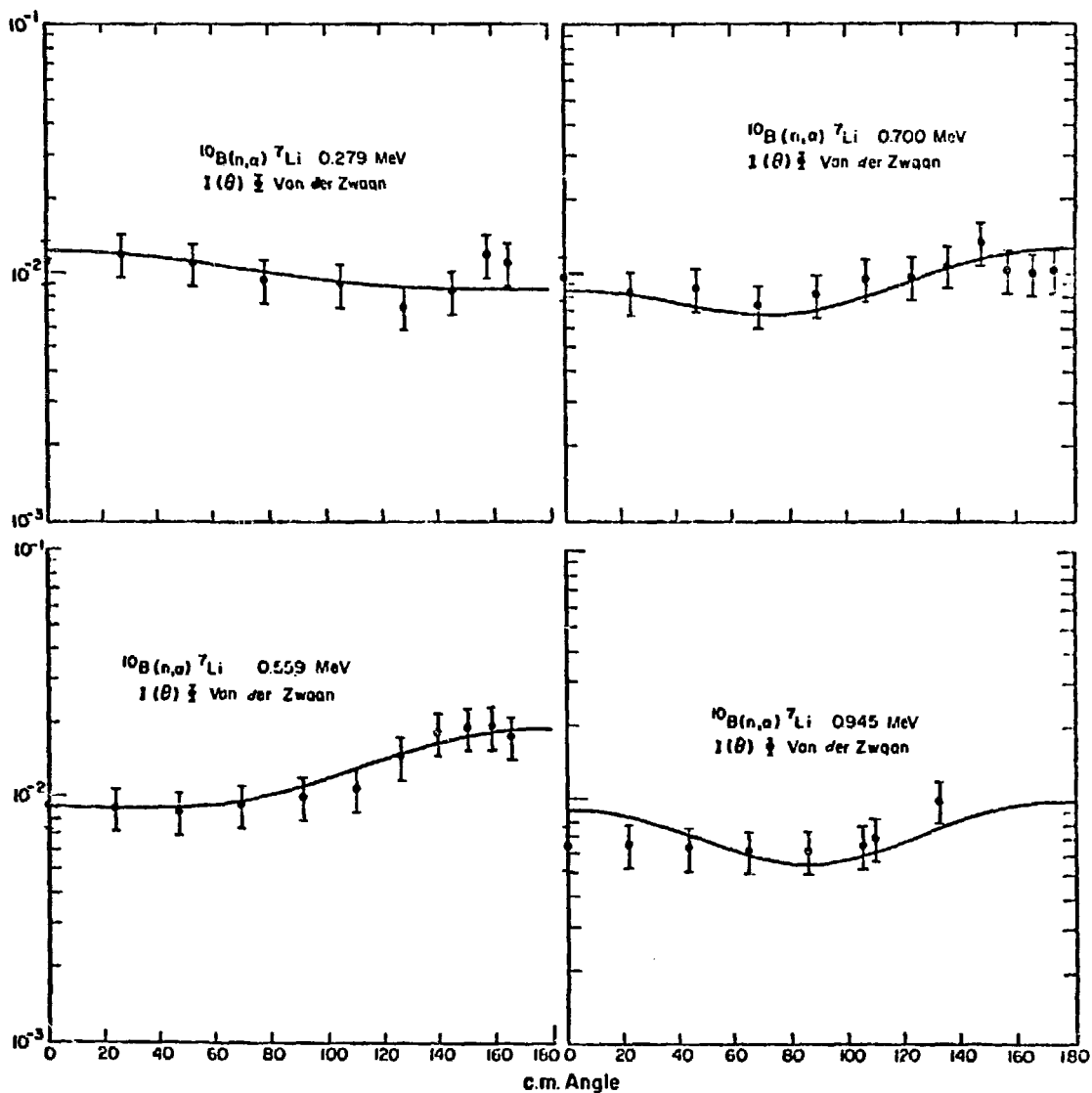
Fig. 17.
Representative fits to the $^{10}B(n,\alpha)^7Li$ differential cross-section measurements of Van der Zwaan and Geiger[91] for E_n between 279 and 945 keV. The units for $I(\theta)$ are b/sr.

Fig. 18.
The n-^{10}B total cross section between 10 keV and 1 MeV. The data are from
Refs. 93, 101, 104, and 105.

Fig. 19.
Representative fits to the $^7Li(\alpha,\alpha)^7Li$ differential cross-section measurements of Cusson[95] at alpha energies between 4 and 6 MeV. The units of $I(\theta)$ are b/sr.

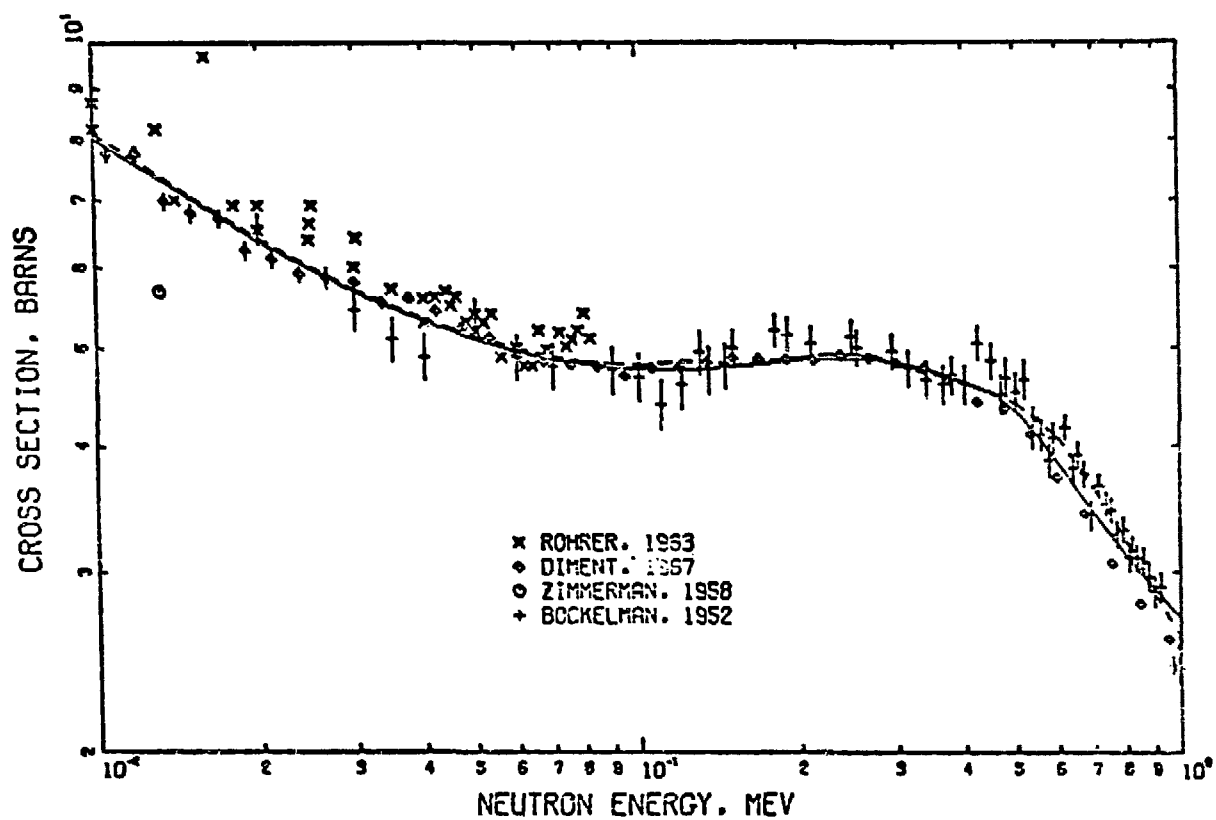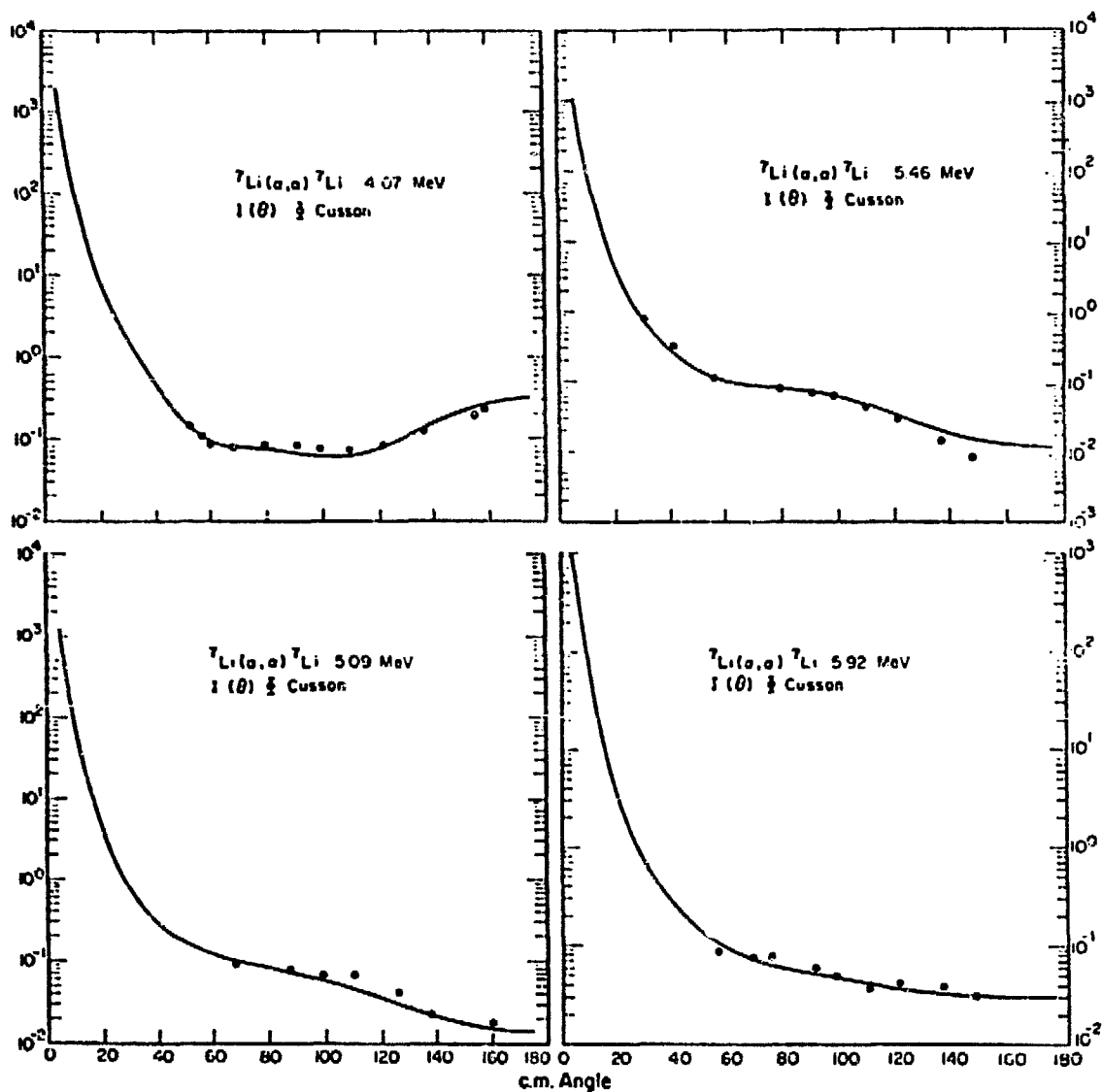# REFERENCES

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