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Discrepancies in (n,2n) reaction excitation functions of rare earth isotopes

Recommendations for selection of the reliable data

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Abstract

Analysis of (n,2n) reaction cross sections from different evaluated nuclear data libraries is performed for rare earth isotopes (Z=58-71). The cross sections are plotted and the discrepancies are shown. The cross sections calculated on the basis of the excitation function systematics are compared against the evaluated data to determine the reliability of the latter.

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Discrepancies in (n,2n) reaction excitation functions of rare earth isotopes. Recommendations for selection of the reliable data.

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ABSTRACT.

Analysis of (n,2n) reaction cross sections from different evaluated nuclear data libraries is performed for rare earth isotopes (Z=58-71). The cross sections are plotted and the discrepancies are shown. The cross sections calculated on the basis of the excitation function systematics are compared against the evaluated data to determine the reliability of the latter.

An activity in creation of international data libraries (for example, FENDL library) leads to the problem of selection of more reliable data from different national or regional libraries. Because of large discrepancies in many cases it is not easy to decide which data is more reliable. As a rule, there are no serious arguments to reject the data even if they differ essentially from the others. To solve the problem we propose a systematics that permits to select reliable excitation functions.

The analysis of the threshold reaction cross sections from different data libraries shows considerable discrepancies in the excitation functions. These discrepancies are particularly large, when there are no or too little experimental data. As a rule, the evaluated data are calculated on the basis of theoretical models taking into account the 14-15 MeV systematics and discrepancies among these calculated data exist for most reactions and isotopes. We think that it is useful to publish the results of this comparison. We understand that it is very difficult to correct the existing libraries but hope that our recommendations will be taken into account.

In this paper the (n,2n) reaction excitation functions for rare earth isotopes from the following libraries: BROND-2 /1/, ENDF/B-VI /2/, JENDL-3 /3/, ADL-3 /4/, EAF-3 /5/ were compared. We are aware of the EAF-4 library, but unfortunately these data were not at our disposal.

As a criteria for determination which evaluated data from the libraries mentioned above seem to be more reliable, the (n,2n) reaction excitation functions, calculated on the basis of the excitation function systematics, are plotted together with those from the libraries. As the systematics' excitation functions are obtained independently from the experimental data and model calculations it seems to us reasonable to consider the systematics curves, or those excitation functions which are close to the systematics, as more reliable.

Below, a brief description of the systematics used in this work for calculation of the (n,2n) reaction excitation functions in the energy region up to 20 MeV is given. As it was mentioned above this systematics is based on experimental data and its detailed

description was published in the Refs. 6-8. The essential features and relations of the systematics are the following:

1. The value of cross section in the maximum of (n,2n) reaction excitation function depends essentially on the interrelation of (n,2n) and (n,np) reaction thresholds $(Q_{n,2n}$ and $Q_{n,np}$, respectively): $Q_{n,2n} \leq Q_{n,np}$ or $Q_{n,2n} > Q_{n,np}$.

At $Q_{n,2n} \leq Q_{n,np}$ the maximum (top) cross sections of the (n, 2n)-reaction excitation functions are determined by the following equation:

$$\sigma_{top} = 65.4 \text{ A}^{2/3} \text{ [mb]},$$
 (1)

where A is the atomic mass number.

This maximum (top) value is reached in the neutron energy region of 5-8 MeV (in most cases 6-7 MeV) above the reaction threshold. The analysis of experimental and theoretical excitation functions shows that this equation is reasonable for any A (within A=10-210), if the condition $Q_{n,2n} \leq Q_{n,np}$ is fulfilled. In the range of mass numbers A=50-210, where there is enough experimental data, this is quite well proved. However, for the nuclei with A<50 there are no experimental data near maximum of the (n,2n) reaction excitation functions and the reliability of the systematics was checked against theoretical model calculations which take into account recent achievements in the description of nuclear reactions.

The (n,2n)-reaction excitation functions, in the neutron energy region between the threshold and the maximum, are similar and can be described by the normalized excitation function in scales ($\sigma/\sigma_{max} - \Delta E/\Delta E_{max}$) (see Table). Here σ_{max} is cross section at the maximum, $\Delta E=E-E_{th}$, E_{th} - threshold energy, $\Delta E_{max} = E_{max} - E_{th}$. E is a neutron energy, and E_{max} - neutron energy at the maximum of (n,2n) excitation function.

If $Q_{n,2n} < Q_{n,np}$, σ_{max} is equal to σ_{top} (see eq.1).

If $Q_{n,2n}>Q_{n,np}$, σ_{max} is determined from the experimental data or from other considerations, however, the shape of the excitation function is described by the same normalized function.

$\Delta E / \Delta E_{max}$	σ/σ_{max}	$\Delta E / \Delta E_{max}$	σ/σ_{max}
0.05	0.03	0.50	0.81
0.10	0.09	0.55	0.85
0.15	0.18	0.60	0.88
0.20	0.30	0.65	0.91
0.25	0.42	0.70	0.93
0.30	0.53	0.75	0.95
0.35	0.60	0.80	0.97
0.40	0.68	0.85	0.98
0.45	0.75	0.90	0.99

Table. Normalized excitation function of the (n, 2n)-reaction.

For $Q_{n,2n}>Q_{n,np}$ the (n,2n) cross section in the maximum of the excitation function is below the values calculated from the equation (1), and the difference is determined by contribution of the (n,np) reaction cross section at the same neutron energy. The maximum of both reaction excitation functions lies near En=20 MeV and the sum of the (n,2n) and (n,np) reaction cross sections is approximately equal to σ_{too} .

$$\sigma_{\rm top} \approx \sigma_{\rm n,2n} + \sigma_{\rm n,np}, \qquad (2)$$

providing the value of $Q_{n,3n}$ is above ~20 MeV.

The (n,2n) reaction cross section in the energy region above the maximum was calculated by subtraction of the (n,3n) reaction cross section from σ_{top} . The (n,3n) reaction cross sections were calculated from the relation (3), also based on the experimental data. It was shown in Refs.6-8, that the shapes of the (n,3n) reaction excitation functions are similar in the neutron energy region between the threshold and the neutron energy at the maximum of the excitation function and can be approximated by the equation:

$$\sigma = \sigma_{\max} \left(\Delta E / \Delta E_{m} \right)^{3.3} \cdot \exp[3.3(1 - \Delta E / \Delta E_{m})].$$
(3)

Here ΔE and ΔE_m are counted from the (n,3n) reaction threshold, and σ_{max} is determined by the equation:

$$\sigma_{\max} \approx 10 \text{ A [mb]}. \tag{4}$$

Within experimental uncertainties these equations describe available experimental (n,3n) excitation functions. Taking into account (n,3n) reaction competition results in (n,2n) reaction excitation functions which agree very well with experimental data in a whole energy range from the threshold up to 20 MeV.

It was proposed that ΔE_m for (n,3n) reaction excitation functions is equal to 10 MeV. This value was determined from the experimental data of L.Veeser et al /9/ and B.Bayhurst et al /10/ for (n,3n) reaction cross sections in the energy region from the threshold up to 26 MeV.

The recommended data obtained using our method are presented on Fig.1-50 as solid curves.

Finally, we would like to make some general remarks. Fig.1-50 show, that in most cases the (n,2n) cross section values at the maximum of excitation functions are rather close. However, there are great discrepancies in shapes of the excitation functions. Many curves have very steep slope above the threshold that contradicts new experimental data. One can see a fast decrease of the (n,2n) cross sections in the energy region above the energy value at which the cross section maximum is observed. It was proved, on the basis of the experimental data, that the maxima of (n,3n) reaction cross sections are lower than those of (n,2n) reactions. Also the cross section increase above the threshold is weaker for (n,3n) reactions than for (n,2n) ones. The fast drop in cross sections after the maximum seems to be unreasonable. It contradicts also available experimental data.

It should be mentioned that similar discrepancies for the (n,2n) reactions are also observed for many other elements. Preliminary analysis indicates the same problems also for the (n,p) and (n,α) reactions.

Acknowledgments

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References

1. A.I.Blokhin, et al., "Current status of Russian Nuclear Data Libraries", Nuclear Data For Science and Technology, Vol. 2, p.695, edited by J.K.Dickens (American Nuclear Society, LaGrange Park, IL, 1994).

2. Cross Section Evaluation Working Group, ENDF/B-VI Summary Documentation, Report BNL-NCS-17541 (ENDF-201) (1991), edited by P.F.Rose, National Nuclear Data Center, Brookhaven National Laboratory, Upton, NY, USA.

3. T.Nakagawa, et al., Japanese Evaluated Nuclear Data Library, Version 3, Revision 2, J.Nucl.Sci.Technol. 32, 1259 (1995).

4. O.T.Grudzevich, A.V.Ignatyuk, A.V.Zelenetsky, A.B.Pashchenko, "Catalog of ADL-3 Library", in: Voprosy Atomnoi Nauki I Tekhniki, Series Yadernye Konstanty, (1993), v.3-4. See also IAEA-NDS-137, 1995.

5. J.Kopecky, H.A.J. Van der Kamp, H.Gruppelaar and D.Nierop, "The European Activation File EAF-3 with Neutron Activation and Transmutation Cross Sections", ECN-C-92-058, September 1992.

6. V.N.Manokhin, "Systematics of the (n, 2n) and (n, 3n) reaction excitation functions", Jadernye Konstanty, (1994), v.1. See also: Report INDC(CCP)-398, Vienna, 1996.

7.A.I.Blokhin, V.N.Manokhin, "Empirical dependence of parameters of neutron threshold reaction excitation functions on A, Z, (N-Z)", in: Proc. Int. Conf. on Nuclear Data for Science and Technology, Trieste, Italy, 1997 (in Press).

8. A.I.Blokhin, V.N.Manokhin, S.M.Nasyrova, "Investigation of threshold reaction excitation function by similarity method", Preprint FEI - 2620, 1997 (in Russian).

9. L.R.Veeser, E.D.Arthur, P.G.Young, "Cross sections for (n,2n) and (n,3n) reactions above 14 MeV", Phys. Rev. C16(1977), p.1792.

10. B.P.Bayhurst, J.S.Gilmore, R.J.Prestwood et al., "Cross sections for (n,xn) reactions between 7.5 and 28 MeV", Phys. Rev. C12(1975), p. 451.

Fig.1. Cross section of 136 Ce(n,2n) 135 Ce reaction. Fig.2. Cross section of 138 Ce(n,2n) 137 Ce reaction. Fig.3. Cross section of 140 Ce(n,2n) 139 Ce reaction. Fig.4. Cross section of 142 Ce(n,2n) 141 Ce reaction. Fig.5. Cross section of ¹⁴²Nd(n,2n)¹⁴¹Nd reaction. Fig.6. Cross section of 143 Nd(n,2n) 142 Nd reaction. Fig.7. Cross section of 144 Nd(n,2n) 143 Nd reaction. Fig.8. Cross section of ¹⁴⁵Nd(n,2n)¹⁴⁴Nd reaction. Fig.9. Cross section of $^{146}Nd(n,2n)^{145}Nd$ reaction. Fig10. Cross section of ¹⁴⁸Nd(n,2n)¹⁴⁷Nd reaction. Fig.11. Cross section of ¹⁵⁰Nd(n,2n)¹⁴⁹Nd reaction. Fig.12. Cross section of ¹⁴⁴Sm(n,2n)¹⁴³Sm reaction. Fig. 13. Cross section of 147 Sm(n,2n) 146 Sm reaction. Fig.14. Cross section of ¹⁴⁸Sm(n,2n)¹⁴⁷Sm reaction. Fig.15. Cross section of 149 Sm(n,2n) 148 Sm reaction. Fig. 16. Cross section of 150 Sm(n,2n) 149 Sm reaction. Fig. 17. Cross section of ¹⁵²Sm(n,2n)¹⁵¹Sm reaction. Fig. 18. Cross section of 154 Sm(n,2n) 153 Sm reaction. Fig. 19. Cross section of ¹⁵¹Eu(n,2n)¹⁵⁰Eu reaction. Fig.20. Cross section of 153 Eu(n,2n) 152 Eu reaction. Fig.21. Cross section of ¹⁵²Gd(n,2n)¹⁵¹Gd reaction. Fig.22. Cross section of ¹⁵⁴Gd(n,2n)¹⁵³Gd reaction. Fig.23. Cross section of ¹⁵⁵Gd(n,2n)¹⁵⁴Gd reaction. Fig.24. Cross section of ¹⁵⁶Gd(n,2n)¹⁵⁵Gd reaction. Fig.25. Cross section of ¹⁵⁷Gd(n,2n)¹⁵⁶Gd reaction. Fig.26. Cross section of ¹⁵⁸Gd(n,2n)¹⁵⁷Gd reaction. Fig.27. Cross section of ¹⁶⁰Gd(n,2n)¹⁵⁹Gd reaction. Fig.28. Cross section of ¹⁵⁹Tb(n,2n)¹⁵⁸Tb reaction. Fig.29. Cross section of 156 Dy(n,2n) 155 Dy reaction. Fig.30. Cross section of 158 Dy(n,2n) 157 Dy reaction. Fig.31. Cross section of 160 Dy(n,2n) 159 Dy reaction.

Fig.32. Cross section of 161 Dy(n,2n) 160 Dy reaction. Fig.33. Cross section of 162 Dy(n,2n) 161 Dy reaction. Fig.34. Cross section of 163 Dy(n,2n) 162 Dy reaction. Fig.35. Cross section of 164 Dy(n,2n) 163 Dy reaction. Fig.36. Cross section of ¹⁶⁵Ho(n,2n)¹⁶⁴Ho reaction. Fig.37. Cross section of 162 Er(n,2n) 161 Er reaction. Fig.38. Cross section of 164 Er(n,2n) 163 Er reaction. Fig.39. Cross section of 166 Er(n,2n) 165 Er reaction. Fig. 40. Cross section of 167 Er(n,2n) 166 Er reaction. Fig.41. Cross section of 168 Er(n,2n) 167 Er reaction. Fig.42. Cross section of 170 Er(n,2n) 169 Er reaction. Fig.43. Cross section of 169 Tm(n,2n) 168 Tm reaction. Fig.44. Cross section of ¹⁶⁸Yb(n,2n)¹⁶⁷Yb reaction. Fig.45. Cross section of 170 Yb(n,2n) 169 Yb reaction. Fig.46. Cross section of 171 Yb(n,2n) 170 Yb reaction. Fig.47. Cross section of 172 Yb(n,2n) 171 Yb reaction. Fig.48. Cross section of 173 Yb(n,2n) 172 Yb reaction. Fig.49. Cross section of ¹⁷⁴Yb(n,2n)¹⁷³Yb reaction.

Fig. 50. Cross section of ${}^{175}Lu(n,2n){}^{174}Lu$ reaction.



Fig.2. Cross section of $^{138}Ce(n,2n)^{137}Ce$ reaction.









Fig.4. Cross section of $^{142}Ce(n,2n)^{141}Ce$ reaction.



Fig.6. Cross section of 143 Nd(n,2n) 142 Nd reaction.







Fig.8. Cross section of ¹⁴⁵Nd(n,2n)¹⁴⁴Nd reaction.







Fig. 10. Cross section of $^{148}Nd(n,2n)^{147}Nd$ reaction.







Fig.12. Cross section of 144 Sm(n,2n) 143 Sm reaction.







Fig. 14. Cross section of 148 Sm(n,2n) 147 Sm reaction.







Fig. 16. Cross section of 150 Sm(n,2n) 149 Sm reaction.

Fig.18. Cross section of 154 Sm(n,2n) 153 Sm reaction.

Fig.20. Cross section of ¹⁵³Eu(n,2n)¹⁵²Eu reaction.

Fig.22. Cross section of 154 Gd(n,2n) 153 Gd reaction.

Fig.24. Cross section of 156 Gd(n,2n) 155 Gd reaction.

Fig.26. Cross section of 158 Gd(n,2n) 157 Gd reaction.

Fig.28. Cross section of ¹⁵⁹Tb(n,2n)¹⁵⁸Tb reaction.

Fig.30. Cross section of 158 Dy(n,2n) 157 Dy reaction.

En (MeV)

0.0

Fig.32. Cross section of 161 Dy(n,2n) 160 Dy reaction.

Fig.34. Cross section of 163 Dy(n,2n) 162 Dy reaction.

Fig.36. Cross section of 165 Ho(n,2n) 164 Ho reaction.

Fig.38. Cross section of 164 Er(n,2n) 163 Er reaction.

Fig.40. Cross section of 167 Er(n,2n) 166 Er reaction.

Fig.42. Cross section of 170 Er(n,2n) 169 Er reaction.

Fig.44. Cross section of 168 Yb(n,2n) 167 Yb reaction.

Fig.46. Cross section of 171 Yb(n,2n) 170 Yb reaction.

Fig.48. Cross section of 173 Yb(n,2n) 172 Yb reaction.

Fig. 50. Cross section of $^{175}Lu(n,2n)^{174}Lu$ reaction.

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