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Unresolved Resonance Region for ${ }^{233} \mathrm{U}$
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## ABSTRACT

The single level Breit Wigner resonance parameters are evaluated for ${ }^{233} \mathrm{U}$ in the resolved resonance region starting from the area analysis data reported by Nizamuddin and Blons.

The statistical mean resonance parameters for ${ }^{233} \mathrm{U}$ in the unresolved resonance region are evaluated by simultaneous and consistent adjustment of mean fission width and $p$ and $s$ wave strength functions. Our evaluated mean resonance parameters reproduce well the total and the partial neutron induced reaction cross sections given in ENDF/B-IV file in the unresolved resonance for ${ }^{233} \mathrm{U}$.

# EVALUATION OF RESONANCE PARAMETERS IN RESOLVED AND UNRESOLVED RESONANCE REGION FOR ${ }^{233} \mathrm{U}$. 

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## 1. <br> INTRODUCTION

We recommend in this note a complete set of resolved and unresolved resonance parameters for use in fast reactor design calculations. No unresolved parameters are available in the ENDF/B-IV file (1). In the resolved resonance regions since the fast reactor cross section processing code RAMBHA ${ }^{(2)}$ developed at RRC can process only the single level Breit Wigner (SLBW) data, we present in this note the SLBW parameters for ${ }^{233} \mathrm{U}$ in the resolved resonance region and the mean resonance parameters in the unresolved resonance region. These parameters are proposed to be placed in the appropriate format in the RRC data file (2) (RRCDF) which is compatible with the code RAMBHA ${ }^{(2)}$.
2. EVALUATION OF SLBW PARAMETERS FOR ${ }^{233} U$

At present, we are satisfied with single level Breit Wigner representation of cross sections in the resolved resonance region for the following reasons

1) In fast power reactors, the neutron flux is relatively less in the lower energy region $0-100 \mathrm{eV}$ which is the resolved resonance region for ${ }^{233} \mathrm{U}$.
2) In a typical 500 MWe fast breeder reactor fuelled with this isotope, the resolved resonance region contributes less than about $5 \%$ to the Doppler effect contributed by ${ }^{233} \mathrm{U}$ isotope.
3) Doppler broadening formulations are relatively simpler with the use of this formalism.

Several resolved resonance data sets are available in SLBW formalism in the literature ${ }^{(4-14)}$. We effect considerable simplification in our evaluation by selecting only one recent set of data based on completeness for our purpose.

We have selected the recent work by Nizamuddin and Blons ( These authors have reported measurements of the fission cross section of ${ }^{233} U$ at liquid nitrogen temperature between 6 and 124 eV and analysed the results by a single level formalism. They presented the values of $E_{0}, \Gamma$ and $\sigma_{0} \Gamma_{f}$ These parameters were shown to represent their measured cross section quite well provided that, in addition to the 136 well resolved resonances, 33 broad levels were added in the vicinity of some of the highly asymmetric resonances. For the well resolved resonances they derived the fission widths $\Gamma_{f}$ using a constant value of radiation width

$$
\Gamma_{\gamma}=\left\langle\Gamma_{\gamma}\right\rangle=0.039 \mathrm{eV}
$$

They also report ${ }^{(4)}$ that a $\chi^{2}$ distribution with $\nu=3$ degrees-of-freedom matches well the observed fission width distribution. Table 1 gives the values of $k, E_{0}, \Gamma_{k},\left(\sigma_{o_{k}} \Gamma_{f_{k}}\right)$ and $\Gamma_{f k}$ as reported by Nizamuddin and Blows
(4) in the first five columns.

From the values given in Table l, our aim is to deduce the following parameters.

for all resonances. $E_{0}$ and $\Gamma_{f}$ are already given for all the well resolved resonances in Table $1 . \Gamma_{\gamma}$ is assumed to be the same for all resonances and taken to be 30 meV . The value of $\left(g \Gamma_{n}\right)$ is deduced from the equation:

$$
\left.g \Gamma_{n}=\frac{\left(\sigma_{0} \Gamma_{f}\right)}{\Gamma_{f}} \cdot \frac{\Gamma}{4 \pi \pi^{2}}\right)
$$

The spin assignments are now to be made for the resonances. The spins for the resonances are not known from ref. 4 and can be found in principle by looking for the validity of the conservation relations such as

$$
\begin{aligned}
& \Gamma=\frac{g \Gamma_{n}}{g_{\text {assigned }}}+\Gamma_{r}+\Gamma_{f} \\
& \Gamma_{r}=\Gamma-\Gamma_{f}-\frac{\left(g \Gamma_{n}\right)}{g_{\text {assigned }}}>0
\end{aligned}
$$

It is found that both values of $J, J=2$ or 3 are acceptable in view of the large uncertainties in the individual partial widths and also because

$$
\Gamma_{n} \ll \Gamma_{f}
$$

The BNL document ${ }^{(5)}$ gives $J=2$ for some resonances. In our evaluation, for all the resonances we assign $J=2$ and thus

$$
g=\frac{2 J+1}{2(2 I+1)}=\frac{5}{12}
$$

for ${ }^{233} \mathrm{U}$. This completes the evaluation for the real resolved levels.

Now coming to the 33 "artifical resolved levels", we adopt the following procedure to evaluate the individual resonance parameters. For these "artificial levels" only $\Gamma$ and $\sigma_{0} \Gamma_{f}$ are given; We require to find $\Gamma_{r}, \Gamma_{f}$ and $g$. We assume $\left\langle\Gamma_{r}\right\rangle$ to be 0.039 eV . The value of $\left\langle\Gamma_{n}\right\rangle$ from the $\Gamma_{n}$ values of the well resolved 133 resonances is found to be:

$$
\left\langle\Gamma_{n}\right\rangle=0.1232 E-02
$$

An initial guess value of $\Gamma_{f}$ is evaluated using the following conservations relation.

$$
\Gamma_{f} \stackrel{\text { guess }}{=} \Gamma-\left\langle\Gamma_{r}\right\rangle-\left\langle\Gamma_{n}\right\rangle
$$

Using this guess value of $\Gamma_{f}$ we obtain the value of $\Gamma_{f}$ for the individual artifical resonances from the given values of $\Gamma$ and $\left(\sigma_{0} \Gamma_{f}\right)$. using the following relation :-

$$
\Gamma_{n}=\frac{\left(\sigma_{0} \Gamma_{f}\right)}{\Gamma_{f} \text { guess }} \cdot \frac{\Gamma}{4 \pi \lambda^{2}} \cdot \frac{12}{5}
$$

Where $g$ is taken to be 5/12. This $\Gamma_{n}$ is used to re-evaluate $\Gamma_{f}$ for the individual artificial resonance as follows:

$$
\Gamma_{f}=\Gamma-\Gamma_{n}-0.039
$$

Thus we obtain through iteration using the basic conservation relations both $\Gamma_{f}$ and $\Gamma_{n}$ for the artificial resonances. The iteration is repeated until the $\Gamma_{n}$ value converges to $95 \%$ certainty. The complete set $\Gamma_{n}, \Gamma_{r}, \Gamma_{f}, E_{0}$ and $g$ are tabulated in Table 1.
3. EVALU ATION OF UNRESOLVED PARAMETERS FOR ${ }^{233} \mathrm{U}$. 3.1 Review of the Earlier Publications: The unresolved resonance parameters as reported in the recent literature are complied with our comments below. The unresolved resonance region for our data set will cover the 0.101 to 40.93 KeV energy region for our purpose.

Average s-wave level spacing

$$
\frac{\text { Value (eV) }}{0.718 \pm 0.35} \quad \frac{\text { Year }}{1972} \quad \text { Ref. }
$$

## Comments

Obtained from staircase plots. In all 53 resonances were considered. All data upto 39.37 eV was considered with fitting error of $7.2 \mathrm{E}-4$ due to experimental uncertainties. This value is applicable to all $J$ values. Data upto 62.27 eV containing 10 resonances for $J=3$ sping gave a value of $\langle D\rangle=1.14 \pm 0.5$

| 0.71 | 1974 | Nizamuddin \& Blons (4) | Experimental value corresponding to the distribution of all the levels including the 33 somewhat broad ( $\Gamma>500 \mathrm{meV}$ ) levels added in the vicinity of some of the highly asymmetric resonances for obtaining good representation of the measured cross sections. The distribution of well resolved (real) levels alone gives a somewhat higher value of 0.88 eV . The difference between these two values shows that certain closely spaced leveis have been missed due to resolution effects. The energy range spanned was from 6 to 124 eV . Measurements were made at liquid nitrogen temperature to reduce Doppler broadening. |
| :---: | :---: | :---: | :---: |
| $0.61 \pm 0.07$ | 1970 | Kolar ${ }^{(6)}$ | From the single level resonance parameters upto 30 eV comprising 45 spacings. |
| 0.87 | 1967 | Hennies ${ }^{(7)}$ | Based on a value given by Michaudon. |
| $\begin{aligned} & \langle D\rangle_{J=2}=1.896 \\ & \langle D\rangle_{J=3}=1.354 \end{aligned}$ | 1968 | Boroughs $\text { et al }{ }^{(8)}$ | Obtained by using as a guideline, the statistical average of the single level resonance parameters to fit the cross sections averaged over quarter lethargy energy groups. Energy range considered is from 61 eV to 100 keV . |
| 0.56 | 1973 | Reynolds and Steiglitz | From analysis of the data for 76 resonances between 0.0 and 60.0 eV on the basis of Wigner distribution. The observed spacing is 0.79 eV which has been corrected for the missing levels. |

0.621968 Bergen ${ }^{(10)}$

## Average radiation width $\left\langle\Gamma_{\gamma}\right\rangle$

Average $p$ wave level spacing
$3.16 ;$ for $J=1 \quad 1968$ Borough ${ }^{\text {(8) }}$
$1.896 ;$ for $J=2$
$1.354 ;$ for $J=3$
1.0053 ;for $J=4$
Value (aV) Year Ref.
3.16; for $J=11968$ Borough ${ }^{(8)}$
1.896; for $J=2$
1.354; for $\mathrm{J}=3$

1. 0053 ;for $J=4$

| $\frac{\text { Value (meV) }}{39.0}$ | $\frac{\text { Year }}{1974} \frac{\text { Ref. }}{\text { Nizamuddin }}$ |
| :--- | :--- |
| 54.0 | 1967 Genies $^{(7)}$ |
| 39.4 | 1968 Borough |
|  |  |
| 40.0 | 1973 Reynolds |

Sixty eight levels were considered from 20 eV through 63 eV . The spacing was derived from the least squares line drawn through the data. Actually the slight curvature of the level spacing plot suggest that levels may have been overlooked due to experimental resolution and Doppler broadening effects.

## Comments

It is assumed that all levels are equally likely to be excited. Thus, the number of levels excited depends only on the statistical factor. The energy range considered is from 61 eV to 100 keV . Parameters were chosen to fit the quarter lethargy average cross sections.

| 48.44 | 1965 | BNL-325 ${ }^{(11)}$ | Calculated from 31 resolved resonances using simple aver aging. |
| :---: | :---: | :---: | :---: |
| 45.0 | 1966 | Bergen ${ }^{(10)}$ | Evaluated. |
| 47.0 | 1972 | $\text { Guylassy }{ }^{(5)}$ | Obtained from the analysis of 25 resonances, Uncertainty generated by finite sample size is 11 meV . |
| 45.0 | 1970 | $\text { Kikuchi }^{(15)}$ | From Channel Theory. |
| Average fission width $\left\langle\Gamma_{f}\right\rangle$ |  |  |  |
| Value (eV) | Year | Ref. | Comments |
| 0.372 | 1974 | Nizamuddin | Calculated from their values of total widths by assuming the radiation width computed with theoretical formulae. It was of course assumed that <br> $\Gamma_{n}$ is negligible. Distribution of these widths compares favourably with the $\chi^{2}$ distribution with $\quad y=3$ degrees of freedom and this $\left\langle\Gamma_{f}\right\rangle$. Energy range from 6 eV to 124 eV is considered in the analysis. |
| 0.314 | 1965 | BNL-325 ${ }^{(11)}$ | Calculated from 31 resolved resonances using simple averaging. |
| 0.3413 | 1968 | Bergen ${ }^{(10)}$ | Evaluated with single level analysis. The multilevel analysis gives a value of 379 meV . |
| 0.389 | 1965 | Nifenecker ${ }^{(12)}$ | Evaluated. |
| 0.382 | 1968 | $\text { Boroughs }{ }^{(8)}$ | The value is at 1 keV ; Obtained by fitting the quarter lethargy energy group average cross sections in the energy range from 61 electron Volts. |


|  |  |  | to $100 \mathrm{keV} . \quad\left\langle\Gamma_{f}\right\rangle^{2}=0$ is the same for both $J=2$ and $J=3$. The values are given as a function of energy from 0.07 keV to 100 keV in a tabular form. |
| :---: | :---: | :---: | :---: |
| 0.569 | 1973 | Reynolds ${ }^{(9)}$ | The distribution of fission widths agrees well with $\boldsymbol{X}^{2}$ distribution with 3 degrees of freedom. However, the statistics on the distribution of values are not good enough to allow it to be resolved into two different distributions for $J=2$ and $J=3$ sequences. |
| 0.372 | 1972 | Guylassy ${ }^{(5)}$ | Obtained from the analysis of 85 resonances. Uncertainty generated by finite sample size is 23 meV . |

## Average fission width for $p$ wave sequences

$$
\begin{aligned}
& \left\langle r_{f}\right\rangle^{\left(G^{=1)}=0.10058\right.} \frac{\text { Value }(\mathrm{eV})}{1968} \frac{\text { Year }}{\text { Boroughs }}(8) \\
& \left\langle\Gamma_{f}^{(J=2)}=0.6058\right. \\
& \left\langle r_{f}\right\rangle^{(J=3)}=0.431 \\
& \left\langle r_{f}^{(J=4)}=0.3352 .\right.
\end{aligned}
$$

## Comments

Fission widths for $p$ waves were obtained from the formula

$$
\left\langle\Gamma_{f}\right\rangle^{(J)}=\frac{\langle D\rangle^{(\sigma)}}{\pi}
$$

The spacing for the $p$ wave resonances was calculated from the above mentioned equation using the $s$ wave values.

The s wave strength function

| $\frac{\text { Value (eV) }}{\left(10^{-4} \text { units) }\right.}$ | Year |  |  |
| :--- | :--- | :--- | :--- |
| $2.25 \pm 0.55$ | 1970 | Kolar $^{(6)}$ |  |

> Comments

46 levels up to 30 eV are considered and are taken to be all $s$ wave levels.

| $0.8 \pm 0.2$ | 1964 | Nordheim ${ }^{(13)}$ | Quoted from a survey by Garrison (1963). |
| :---: | :---: | :---: | :---: |
| 0.306 | 1965 | BNL $325^{(11)}$ | Derived from the average observed level spacing and 2 g โassuming $\mathrm{g}=0.5$. |
| 2.14 | 1965 | Nifenecker ${ }^{(12)}$ | Evaluated. |
| 1.1 | 1970 | Kikuchi ${ }^{(15)}$ | From Channel |
| $\begin{aligned} & 0.95 \text { to } 1.15 \\ & (0.07<\mathrm{E} \\ & < \\ & <100 \mathrm{keV}) \end{aligned}$ | 1968 | Boroughs ${ }^{(8)}$ | Unresolved resonance para meters were obtained by using the statistical average of the single level resonance para meters in the resolved resonance range with the requirement that the best fit to the experi mentally observed $\sigma_{f}$ and $\sigma_{c}$ values in the energy range 61 eV . to 100 eV had to be obtained. It is however not expected that the recommended unresolved parameters will accurately predict the scattering cross sections. |
| $1.3_{-0.90}^{+0.99}$ | 1971 | Ryabov ${ }^{(14)}$ | Method of maximum likehood is used. The error is due mainly to the finite sample size. |
| 0.89 | 1973 | Reynolds ${ }^{(9)}$ | Obtained from the slope of the plot of a sum of the reduced neturon widths as a function of energy. The assumption here is that the strength functions are equal for each of the spin states. |
| 2.31 | 1968 | Bergen ${ }^{(10)}$ | Obtained by single level fit in in the resolved resonance energy region. |
| 0.991 | 1972 | Guylassy ${ }^{(5)}$ | Number of resonance analysed is 30 . Uncertainty due to finite sample size is of the order of 0.26 . |

The $p$ wave strength function

| $\frac{\text { Value }}{1.5}$ | $\frac{\text { Year }}{1968}$ | Ref. <br> Boroughs |
| :--- | :--- | :--- |
| 1.42 | 1970 | Same as for the s averts <br> Strength function. |
| (15) | From Channel Theory. |  |

Having complied the unresolved resonance parameters which were available with us, we note that there are wide discrepancies in the mean resonance data reported in the literature.
3.2 Present Evaluation of Unresolved Resonance Data

We present below our evaluation of a mean resonance data set. that reproduces well the total and partial reaction cross sections given in ENDF/B-IV file.

Starting from the pointwise energy versus cross section data given in ENDF/B-IV file ${ }^{(1)}$, we calculate the following average cross

$$
\begin{aligned}
& \text { sections. } \\
& \left\langle\sigma_{x}\right\rangle=\frac{\int_{g+1}^{E_{g}} \sigma_{x}(E) d E}{\int_{E_{g+1}}^{E_{g}} d E}=\frac{\int_{E_{g+1}}^{E_{g}} \sigma_{x}(E) d E}{\Delta E_{g}}
\end{aligned}
$$

where $x$ stands for any one of the following processes: capture, fission, elastic, total. The subscript $g$ denotes the energy group bounded by the energies $E_{g}$ and $E_{g+1}$ and $\Delta E_{g}$ is the width of of the energy group g. These calculations were done by invoking an option in the RAMBHA code ${ }^{(2)}$. The unresolved resonance

$$
{ }^{\text {data set }}\left\{S_{\ell, J},\left\langle\Gamma_{x}\right\rangle^{(\ell, J)}, R,\langle D\rangle^{(\ell, J)}\right\}
$$

must reproduce the above cross sections (total as well as partial) satisfactorily: Now,
and

$$
\begin{aligned}
& \left\langle\sigma_{x}\right\rangle=\sum_{(l, J)} \frac{2 \pi^{2} \lambda^{2}\left\langle\frac{\Gamma_{n} \Gamma_{x}}{\Gamma}\right\rangle_{(l, J)}}{\langle D\rangle^{(l, J)}} \\
& \left\langle\sigma_{t}\right\rangle=\sigma_{p}+\sum_{x}\left\langle\sigma_{x}\right\rangle
\end{aligned}
$$

where the symbols have their waal meanings $(16,17,18)$. To start the adjustment process, we input to ADDJA ${ }^{(16)}$ the quantities
$\left\langle\sigma_{x}\right\rangle(\bar{E})$ and $\bar{E}$ where $x$ refers to the partial
and total cross sections.

For each value of $\overline{\mathrm{E}}$ the following quantities are input

$$
\begin{aligned}
& \nu_{f}(l, J)=3 \quad \text { (Ref. 4) } \\
& \nu_{n}^{(l, J)}=2 \text { for } l=1, J=2,3 \\
& =1 \text { for all other } X \text { and } J \\
& \left\langle\Gamma_{\gamma}\right\rangle^{(\ell, J)}=0.039 \text { for all } \lambda \text { and J. (Ref. 4) } \\
& \langle D\rangle^{\ell=0, J=2}=1.723 \mathrm{eV} \quad=\quad\langle D\rangle^{\ell=1, J=2} \\
& \begin{array}{l}
\langle D\rangle^{\ell=0, J=3}=1.231 \mathrm{eV} \\
\langle D\rangle^{\ell=1, J=3}=2.872 \mathrm{eV} \quad-\quad\langle D\rangle^{\ell}=1, \mathrm{~J}=4 \\
=0.95\rangle^{\ell=1, J=3} \\
=0.9572 \mathrm{eV}
\end{array} \\
& \text { These values correspond to a } \bar{D}=0.718 \mathrm{eV}(\mathrm{~J}=\text { all) }
\end{aligned}
$$

There are two $s$ wave and 4 p wave sequences. These are characterised by

$$
\begin{aligned}
& \ell=0, \quad J=2 \text { and } 3 \\
& \ell=1, \quad J=1 \text { to } 4
\end{aligned}
$$

The ENDF/B-IV file gives for the nuclear radius a value of $\left(1.23(231.043)^{1 / 3}+0.8\right] \cdot 10^{-1}=0.834749 \mathrm{fm}$.

It was found that this value of nuclear radius given in ENDF/B-IV file was too small so that the $p$ and $s$ wave strength functions were required to be adjusted much beyond their spread reported in the literature. Also, the scattering cross section could not be sati factorily fitted. We found after some parametric studies using ADDJA code ${ }^{(16)}$ that a value of $R=0.9 \mathrm{fm}$ is acceptable to our evaluation.

With these values of $R,\left\langle\Gamma_{\gamma}\right\rangle^{(l, J)},\langle D\rangle,(l, J), \nu_{f}^{(l, J)}$ and $\nu_{n}^{(l, J)}$ we adjusted the following parameters:

$$
\left\langle\Gamma_{f}\right\rangle^{(Q, J)}, s_{1} \quad \text { and } \quad s_{0}
$$

to obtain best fit to $\left\langle\sigma_{\xi}\right\rangle,\left\langle\sigma_{k}\right\rangle$ and $\left\langle\sigma_{c}\right\rangle$ The code ADDJA was used to do these adjustments. Obviously the adjusted quantities $\left\langle\Gamma_{f}\right\rangle^{(l, J)}$, and $S_{0}$ depend on $\bar{E}$. Care is taken to see that again these are not permitted to vary beyond the spread that exists in the literature. Thus $S_{1}$ was allowed to vary between 0.9 and 2.0 (in $10^{-4}$ units), $S_{0}$ between 0.9 and 1.3 ( $10^{-4}$ units). The $\left\langle\Gamma_{f}\right\rangle$ are assumed to have the following values as the initial guess

$$
\begin{array}{ll}
\left\langle\Gamma_{f}\right\rangle^{l}=0, J=2 & =1.21 \mathrm{eV} \\
\left\langle\Gamma_{f}\right\rangle^{l}=0, J=3 & =0.3813 \mathrm{eV} \\
\left\langle\Gamma_{f}\right\rangle^{l=1, J} & =0.6506 \mathrm{eV} \text { for } J=1 \text { to } 4
\end{array}
$$

It is assumed that $\left\langle\Gamma_{f}\right\rangle^{\ell=1, J_{i s}}$ independent of $J$. The $\left\langle\Gamma_{f}\right\rangle$ values are adjusted, using the relation

$$
\left\langle\Gamma_{f}\right\rangle^{i}=\epsilon\left\langle\Gamma_{f}\right\rangle^{i-1} \frac{\left\langle\sigma_{f}\right\rangle^{c}}{\left\langle\sigma_{f}\right\rangle^{g}}
$$

Here $\epsilon$ is a constant parameter (which may be put to unity) meant to accelerate the convergence; $i$ is the iteration index; $\left\langle\sigma_{f}\right\rangle^{c}$ is the calculated value and $\cdots\left\langle\sigma_{s}\right\rangle^{g}$ is the given value. $(l, J)$
Once $\left\langle\Gamma_{f}\right\rangle$ values are obtained $S_{0}$ and $S_{1}$ are adjusted in a similar way to fit the total cross section within $1 \%$. Whin these, $\left\langle\sigma_{\ddagger}\right\rangle^{c}$ would have now changed. The values of $\left\langle\Gamma_{f}\right\rangle^{(\ell, J)}$ are again adjusted to fit $\left\langle\sigma_{f}\right\rangle$. This procedure is repeated till acceptable $\left\langle\sigma_{f}\right\rangle^{c}\left\langle\sigma_{c}^{c}\right\rangle^{c}$ and $\left\langle\sigma_{t}\right\rangle^{c}$ values are calculated. In Table 3 we give both the $\left\langle\sigma_{x}\right\rangle^{g}$ values (those of ENDF/B-IV) and the values of $\left\langle\sigma_{z}\right\rangle^{c}$ obtained using the final unresolved resonance data set given in Table 2.

It is seen that the selected mean resonance data set given in Table 2 is able to satisfactorily fit $\left\langle\sigma_{t}\right\rangle$ to $I \%$ and other partial cross sections to about 3 to $5 \%$ on the average.

It must be stressed that the unresolved parameters are, . to some extent, non unique, the non uniqueness arising from the choice among the mean resonance data sets, all such sets leading to the 'same' average cross sections within their quoted uncertainties ${ }^{(18)}$.

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## REFERENCES

1. D. Garber, C. Dunford and S. Pearlstein, BNL-NCS -50496 (ENDF-102), Vol. 1 (1975).
2. S. Ganesan (Ed), "Activity Report of Reactor Physcis Section". Internal Note No. FRG/01100/RP-187, p. 5 (1980). Reactor Research Centre, Kalpakkam.
3. S. Ganesan, P. Bhaskar Rao and R. Shankar Singh, RRC-6, Reactor Research Centre, Kalpakkam (1976).
4. A. Nizamuddin and J.Blons, Nucl.Sci. Eng., 54, 116 (1974).
5. M. Guylassy and S. T. Perkins, UCRL - 50400, Vol. 13 (1972). See also UCRL -50400, Vol. 12 (1972).
6. W.Kolar, G. Carraro and G. Nastri, Proc. Conf. On Nuclear Data for Reactors, Vol. I, p. 387 (1970).
7. H.H. Hennies, ibid, Vol. II, p. 333 (1967).
8. G. L. Boroughs, C.W. Craven Jr., M.K. Drake, GA-8854 (1968).
9. J.T. Reynolds and R.G. Steiglitz, KAPL - M. 7323 (1973).
10. D.W. Bergen, LA - 3676 - MS (1966). See also D.W. Bergen and M.G. Silbert, Phys. Rev. 166, 1178 (1968).
11. J.R. Stehn et al., BNL-325 Second Edition, Supplement No. 2 (1965).
12. H. Nifenecker and G. Perrin, Proc. of the Symposium on the Physics and Chemistry of Fission, Salzburg, 22-26, March 1965.
13. L.W. Nordheim, "The Doppler Coefficient", in the Technology of Nuclear Reactor Safety, Vol. I, J.J. Thompson, J.G. Beckerley (Eds), MIT Press (1964).

14 Yu. V. Ryabov et al., Sov. J. Nucl. Phys. 13 (3) 255 (1971).
15 Y. Kikuchi and S. An, J. Nucl. Sci. Tech. 7.(4), 157 (1970).
16 S. Ganesan, Atomkernenergie 29, 14 (1977).
17. S. Ganesan, RRC-42 (1980).Reactor Research Centre, Kalpakkam.
18. S. Ganesan, Nucl. sci. Eng., 74, 49 (1980).

## Table 1

## Reported (Ref, 4) and Our Deduced Resonance Parameters

| 1 $k$ | $\begin{aligned} & 2 \\ & E_{0 k} \\ & (\mathrm{eV}) \end{aligned}$ | $\begin{aligned} & 3 \\ & \Gamma_{\dot{k}} \\ & (\mathrm{meV}) \end{aligned}$ | $\begin{gathered} \sigma_{o k}^{4} \Gamma_{f k} \\ (b, \mathrm{eV}) \end{gathered}$ | $\begin{aligned} & 5 \\ & \Gamma_{f k} \\ & (\mathrm{meV}) \end{aligned}$ | $\begin{gathered} 6 \\ \mathrm{LF} \end{gathered}$ | $\begin{aligned} & 7 \\ & \Gamma_{n k} \\ & (e V) \end{aligned}$ | $\begin{gathered} \Gamma_{f k}^{*} \\ (\mathrm{meV}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | 5. 89 | 320 | 26 | 281 | 0 | . 159 | --- |
| 2. | 6.27 | 538 | 12 | --- | 1 | . 074 | 499 |
| 3. | 6.64 | 500 | 57 | --- | 1 | . 375 | 461 |
| 4. | 6.82 | 138 | 110 | 99 | 0 | . 954 | --- |
| 5. | 7.50 | 200 | 5 | 161 | 0 | . 043 | --- |
| 6. | 8.64 | 248 | 5 | 209 | 0 | . 047 | --- |
| 7. | 9. 26 | 298 | 15 | 259 | 0 | . 146 | --- |
| 8. | 9.71 | 500 | 4 | --. | 1 | . 038 | 461 |
| 9. | 10.39 | 315 | 172 | 258 | 0 | 1.991 | -- |
| 10. | 10.36 | 1000 | 1 | --- | 1 | . 010 | 961 |
| 11. | 11. 31 | 218 | 8 | 179 | 0 | . 101 | --.. |
| 12. | 11. 39 | 2000 | 129 | --- | 1 | 1.428 | 1960 |
| 13. | 12.79 | 309 | 122 | 254 | 0 | 1. 732 | --- |
| 14. | 13.45 | 144 | 4 | 105 | 0 | . 067 | --- |
| 15. | 13.73 | 255 | 25 | 216 | 0 | . 370 | -- |
| 16. | 13. 95 | 1000 | 15 | --- | 1 | . 199 | 961 |
| 17. | 14. 22 | 490 | 2 | - | 1 | . 028 | 451 |
| 18. | 15.33 | 122 | 30 | 92 | 0 | . 556 | --- |
| 19. | 15.47 | 255 | 34 | --- | 1 | . 568 | 215 |
| 20. | 15.82 | 200 | 6 | --- | 1 | . 108 | 161 |
| 21. | 16. 20 | 426 | 66 | 387 | 0 | 1.074 | --- |
| 22. | 16. 56 | 219 | 46 | 180 | 0 | c 846 | --- |
| 23. | 17. 28 | 1500 | 22 | --- | 1 | . 356 | 1461 |
| 24. | 17.63 | 300 | 5 | --- | 1 | . 084 | 861 |
| 25. | 17.97 | 298 | 19 | 169 | 0 | . 383 | -- |

Table 1 (Contd. .)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 26. | 18. 28 | 379 | 9 | --- | 1 | . 167 | 340 |
| 27. | 18.48 | 135 | 8 | 96 | 0 | . 190 | --- |
| 28. | 18.96 | 316 | 113 | 294 | 0 | 2.101 | - |
| 29. | 19.63 | 2500 | 26 | -- | 1 | . 473 | 2461 |
| 30. | 20.59 | 364 | 44 | 325 | 0 | . 926 | --- |
| 31. | 21. 58 | 2000 | 35 | --- | 1 | . 703 | 1960 |
| 32. | 21. 86 | 254 | 54 | 215 | 0 | 1. 272 | --- |
| 33. | 22. 34 | 412 | 173 | 364 | 0 | 3.991 | - |
| 34. | 22.90 | 692 | 30 | 653 | 0 | . 664 | --- |
| 35. | 23.75 | 453 | 28 | 414 | 0 | . 664 | --- |
| 36. | 24.30 | 1000 | 27 | 961 | 0 | . 623 | --- |
| 37. | 25.25 | 274 | 33 | 235 | 0 | . 886 | --- |
| 38. | 25. 78 | 660 | 25 | 621 | 0 | . 625 | -- |
| 39. | 26. 25 | 495 | 11 | 456 | 0 | . 286 | --- |
| 40. | 26. 62 | 260 | 15 | 221 | 0 | . 429 | --- |
| 41. | 26.98 | 592 | 7 | 553 | 0 | . 184 | --- |
| 42 。 | 27.76 | 900 | 23 | 861 | 0 | . 609 | --- |
| 43. | 28.07 | 168 | 1 | 129 | 0 | . 033 | --- |
| 44. | 28. 28 | 230 | 9 | 191 | 0 | . 280 | -- |
| 45. | 29.04 | 540 | 74 | 501 | 0 | 2. 113 | - |
| 46. | 29.58 | 112 | 4 | 73 | 0 | . 166 | -- |
| 47. | 30.35 | 396 | 6 | 357 | 0 | . 184 | --- |
| 48. | 30.72 | 261 | 23 | 224 | 0 | . 751 | - |
| 49. | 31.33 | 325 | 11 | 286 | 0 | . 357 | --- |
| 50. | 31.69 | 600 | 18 | --- | 1 | . 557 | 560 |
| 51. | 32.01 | 217 | 32 | 178 | 0 | 1.139 | --- |
| 52. | 33. 14 | 740 | 27 | 701 | 0 | . 862 | - |
| 53. | 33.95 | 1300 | 67 | 1261 | 0 | 2.140 | --- |
| 54. | 34.51 | 647 | 42 | 599 | 0 | 1.428 | --- |
| 55. | 35. 25 | 395 | 8 | 356 | 0 | . 285 | --- |
| 56. | 35. 75 | 900 | 24 | 861 | 0 | . 818 | --- |

Table 1. (Contd.. .)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 57. | 36.53 | 197 | 23 | 158 | 0 | . 956 | --- |
| 58. | 37. 20 | 420 | 3 | --- | 1 | . 112 | 381 |
| 59. | 37.48 | 395 | 22 | 356 | 0 | . 835 | --- |
| 60. | 39.33 | 686 | 25 | 647 | 0 | . 951 | --- |
| 61. | 39.83 | 445 | 8 | 406 | 0 | . 319 | --- |
| 62. | 40.41 | 900 | 33 | 861 | 0 | 1.272 | --- |
| 63. | 41.03 | 175 | 9 | 136 | 0 | . 434 | --- |
| 64. | 41. 79 | 392 | 1 | 353 | 0 | . 042 | --- |
| 65. | 42.09 | 592 | 4 | 553 | 0 | . 164 | --- |
| 66. | 42.62 | 209 | 20 | 152 | 0 | 1. 069 . | --- |
| 67. | 43.50 | 341 | 13 | 321 | 0 | . 548 |  |
| 68. | 44.10 | 300 | 2 | - | 1 | . 093 | 261 |
| 69. | 44.52 | 1060 | 28 | 1041 | 0 | 1.158 | --- |
| 70. | 45.25 | 138 | 1 | --- | 1 | . 058 | 99 |
| 71. | 45.45 | 150 | 1 | 111 | 0 | . 056 | --- |
| 72. | 46.10 | 192 | 11 | 153 | 0 | . 581 | --- |
| 73. | 46.53 | 245 | 2 | 206 | 0 | . 101 | --- |
| 74. | 47.22 | 507 | 27 | 468 | 0 | 1. 260 | - |
| 75. | 48.68 | 171 | 40 | 131 | 0 | 2.319 | --- |
| 76. | 49.10 | 516 | 14 | 477 | 0 | . 678 |  |
| 77. | 50.40 | 1100 | 25 | 1061 | 0 | 1.192 | --- |
| 78. | 51.00 | 500 | 3 | 461 | 0 | . 151 | --- |
| 79. | 51.85 | 150 | 1 | 111 | 0 | . 032 | --- |
| 80. | 52.10 | 280 | 2 | 241 | 0 | . 083 | --- |
| 81. | 53.03 | 240 | 12 | 201 | 0 | . 693 | --- |
| 82. | 53.32 | 360 | 12 | 321 | 0 | . 655 | - |
| 83. | 53.94 | 230 | 4 | -- | 1 | . 237 | 191 |
| 84. | 54.05 | 500 | 36 | 461 | 0 | 1.926 | --- |
| 85. | 54.41 | 295 | 2 | --- | 1 | . 114 | 256 |
| 86. | 54.78 | 263 | 26 | 224 | 0 | 1. 555 | --- |
| 87. | 55. 20 | 490 | 3 | --- | 1 | . 164 | 451 |

Table 1 (Contd. .)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 88. | 55.95 | 860 | 60 | 821 | 0 | 3. 208 | --- |
| 89. | 56.44 | 373 | 24 | 331 | 0 | 1.393 | --- |
| 90. | 56.88 | 1500 | 28 | --- | 1 | 1. 493 | 1460 |
| 91. | 57.48 | 780 | 53 | 731 | 0 | 2. 966 | - |
| 92. | 58.18 | 1300 | 33 | --- | 1 | 1.808 | 1259 |
| 93. | 58.52 | 225 | 13 | 186 | 0 | . 840 | --- |
| 94. | 59.10 | 295 | 1 | 256 | 0 | . 062 | --- |
| 95. | 60.01 | 220 | 1 | 181 | 0 | . 040 | --- |
| 96. | 60.42 | 1700 | 4 | --- | 1 | . 226 | 1661 |
| 97. | 60.95 | 940 | 18 | 901 | 0 | 1.044 | --- |
| 98. | 61.38 | 400 | 31 | 361 | 0 | 1.924 | --- |
| 99. | 62.59 | 135 | 22 | 83 | 0 | 2. 043 | --- |
| 100. | 63.49 | 1000 | 9 | --- | 1 | . 543 | 960 |
| 101. | 64.03 | 370 | 14 | 331 | 0 | . 914 | --- |
| 102. | 64.44 | 239 | 25 | 200 | 0 | 1. 756 | --- |
| 103. | 65.09 | 238 | 10 | 199 | 0 | . 710 | --- |
| 104. | 65.49 | 630 | 9 | 591 | 0 | . 573 | --- |
| 105. | 66.56 | 770 | 12 | 731 | 0 | . 768 | --- |
| 106. | 67.30 | 940 | 7 | 901 | 0 | . 474 | --- |
| 107. | 67.98 | 333 | 8 | 294 | 0 | . 562 | --- |
| 108. | 69.23 | 1000 | 42 | 961 | 0 | 2. 761 | --- |
| 109. | 70.19 | 533 | 34 | 487 | 0 | 2. 383 | --- |
| 110. | 71.75 | 349 | 4 | 310 | 0 | . 295 | --- |
| 111. | 72. 22 | 800 | 9 | 761 | 0 | . 623 | --- |
| 112. | 73.43 | 125 | 21 | 86 | 0 | 2. 045 | --- |
| 113. | 74.03 | 510 | ${ }^{\prime} 78$ | 471 | 0 | 5. 705 | --- |
| 114. | 75.00 | 258 | 10 | 219 | 0 | . 806 | --- |
| 115. | 75.49 | 290 | 49 | 251 | 0 | 3. 899 | --- |
| 116. | 76.77 | 872 | 9 | 833 | 0 | . 660 | -- |
| 117. | 78.18 | 570 | 31 | 531 | 0 | 2. 374 | --- |
| 118. | 78.46 | 900 | 6 | --- | 1 | . 449 | 861 |

Table 1 (Contd.)

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 119. | 79.00 | 1200 | 11 | $-$ | 1 | . 820 | 1160 |
| 120. | 79.78 | 596 | 39 | 557 | 0 | 3.038 | --- |
| 121. | 81.47 | 1300 | 25 | 1261 | 0 | 1.916 | --- |
| 122. | 82.35 | 740 | 26 | 701 | 0 | 2.062 | --- |
| 123. | 82.78 | 135 | 24 | 96 | 0 | 2. 549 | --- |
| 124. | 84.75 | 815 | 7 | 776 | 0 | . 568 | --- |
| 125. | 85.22 | 400 | 11 | 361 | 0 | . 948 | --- |
| 126. | 85.73 | 590 | 5 | 551 | 0 | . 419 | --- |
| 127. | 86.78 | 295 | 1 | --- | 1 | . 091 | 256 |
| 128. | 87.13 | 150 | 4 | 111 | 0 | . 430 | --- |
| 129. | 87.70 | 88 |  | 49 | 0 | . 014 | --- |
| 130. | 88.89 | 342 | 28 | 303 | 0 | 2. 563 | --- |
| 131. | 89.76 | 558 | 8 | 519 | 0 | . 704 | --- |
| 132. | 90.55 | 253 | 89 | 214 | 0 | 8.693 | --- |
| 133. | 91.72 | 740 | 8 | 701 | 0 | . 707 | --- |
| 134. | 92.67 | 517 | 17 | 478 | 0 | 1. 555 | --- |
| 135. | 93.25 | 590 | 5 | - | 1 | . 456 | 551 |
| 136. | 93.77 | 104 | 14 | 65 | 0 | 1.916 | --- |
| 137. | '95. 22 | 101 | 14 | 62 | 0 | 1.981 | --- |
| 138. | 96.42 | 1600 | 44 | 1561 | 0 | 3. 968 | --- |
| 139. | 97.81 | 229 | 53 | 190 | 0 | 5. 701 | --- |
| 140. | 98.58 | 315 | 23 | 276 | 0 | 2. 361 | --- |
| 141. | 99.30 | 540 | 17 | 501 | 0 | 1.660 | --- |
| 142. | 99.95 | 540 | 32 | 501 | 0 | 3.145 | --- |

* LF is a flag denoting whether the resonance is real ( $\mathrm{LF}=0$ ) or artificial ( $\mathrm{LF}=1$ ) .
** For artificial resonances.

Table 2


Table 3
Calculated Cross Sections from the ENDF/B-IV File

| SI. <br> No. <br> 好 | Lower <br> Limit <br> (eV) |  | Upper Limit (eV) |  | $\begin{gathered} \text { Average } \\ \bar{E} \\ (\mathrm{eV}) \end{gathered}$ | $\left\langle\sigma_{t}\right\rangle$ | $\begin{gathered} \left\langle\sigma_{e l}\right\rangle \\ \quad \text { (barr } \end{gathered}$ | $\left\langle\sigma_{f}\right\rangle$ | $\left\langle\sigma_{c}\right\rangle$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | $24.83+$ |  | $40.930+$ |  | $32.88+3$ | $\begin{aligned} & 13.51 \\ & (13.71) \end{aligned}$ | $\begin{aligned} & 10.24 \\ & (10.64) \end{aligned}$ | $\begin{aligned} & 2.948 \\ & (2.754) \end{aligned}$ | $\begin{aligned} & 0.329 \\ & (0.320) \end{aligned}$ |
| 12 | $15.06+$ |  | $24.83+$ |  | $19.945+3$ | $\begin{aligned} & 14.57 \\ & (14.48) \end{aligned}$ | $\begin{aligned} & 10.76 \\ & (10.70) \end{aligned}$ | $\begin{aligned} & 3.422 \\ & (3.381) \end{aligned}$ | $\begin{aligned} & 0.392 \\ & (0.397) \end{aligned}$ |
| 13 | $9.13+$ |  | $15.6+3$ |  | $12.095+3$ | $\begin{aligned} & 15.75 \\ & (15.49) \end{aligned}$ | $\begin{aligned} & 11.27 \\ & (10.68) \end{aligned}$ | $\begin{aligned} & 4.012 \\ & (4.35) \end{aligned}$ | $\begin{aligned} & 0.469 \\ & (0.457) \end{aligned}$ |
| 14 | $5.54+3$ |  | $9.13+3$ |  | $7.335+3$ | $\begin{aligned} & 16.61 \\ & (16.55) \end{aligned}$ | $\begin{aligned} & 11.26 \\ & (10.67) \end{aligned}$ | $\begin{aligned} & 4.789 \\ & (5.31) \end{aligned}$ | $\begin{aligned} & 0.567 \\ & (0.568) \end{aligned}$ |
| 15 | $3.36+3$ |  | $5.54+3$ |  | $4.45+3$ | $\begin{aligned} & 17.63 \\ & (17.69) \end{aligned}$ | $\begin{aligned} & 11.20 \\ & (10.64) \end{aligned}$ | $\begin{aligned} & 5.752 \\ & (6.361) \end{aligned}$ | $\begin{aligned} & 0.686 \\ & (0.693) \end{aligned}$ |
| 16 | $2.04+3$ |  | $3.36+3$ |  | $2.7+3$ | $\begin{aligned} & 18.58 \\ & (18.64) \end{aligned}$ | $\begin{aligned} & 10.76 \\ & (10.58) \end{aligned}$ | $\begin{aligned} & 6.982 \\ & (7.185) \end{aligned}$ | $\begin{aligned} & 0.837 \\ & (0.870) \end{aligned}$ |
| 17 | $1.24+3$ |  | $2.04+3$ |  | $1.64+3$ | $\begin{aligned} & 19.71 \\ & (19.82) \end{aligned}$ | $\begin{gathered} 9.73 \\ (10.48) \end{gathered}$ | $\begin{aligned} & 9.070 \\ & (8.43) \end{aligned}$ | $\begin{gathered} 0.897 \\ (0.906 \end{gathered}$ |
| 18 | 749.68 |  | $1.24+3$ |  | $0.995+3$ | $\begin{aligned} & 22.12 \\ & (22.20) \end{aligned}$ | $\begin{aligned} & 10.10 \\ & (10.47) \end{aligned}$ | $\begin{aligned} & 10.94 \\ & (10.47) \end{aligned}$ | $\begin{aligned} & 1.080 \\ & (1.144) \end{aligned}$ |
| 19 | 454.71 |  | 749.68 |  | 602.195 | $\begin{aligned} & 25.51 \\ & (25.61) \end{aligned}$ | $\begin{aligned} & 10.55 \\ & (10.59) \end{aligned}$ | $\begin{aligned} & 13.4 C \\ & (13.56) \end{aligned}$ | $\begin{aligned} & 1.559 \\ & (1.545) \end{aligned}$ |
| 20 | 275.79 |  | 454.71 |  | 365.25 | $\begin{aligned} & 29.96 \\ & (30.03) \end{aligned}$ | $\begin{aligned} & 11.02 \\ & (10.54) \end{aligned}$ | $\begin{aligned} & 16.70 \\ & (17.22) \end{aligned}$ | $\begin{aligned} & 2.241 \\ & (2.271) \end{aligned}$ |
| 21 | 101.46 |  | 275.79 |  | 188.63 | $\begin{aligned} & 38.4 \\ & (38.58) \end{aligned}$ | $\begin{aligned} & 11.75 \\ & (10.60) \end{aligned}$ | $\begin{aligned} & 23.19 \\ & (24.44) \end{aligned}$ | $\begin{aligned} & 3.526 \\ & (3.547) \end{aligned}$ |

The values of cross sections given in the brackets are those obtained using our selected mean resonance data set given in Table 2
** The Sl No. here corresponds to the energy group number as used in the 25 group calculations at RRC.
a Read $24.83+3$ as $24.83 \times 10^{3}$

$$
4183
$$

