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International Centre for Theoretical Physics



1930-13

**Joint ICTP-IAEA Advanced Workshop on Model Codes for Spallation Reactions**

*4 - 8 February 2008*

**Detailed investigation of Residual Nuclei Produced in Spallation Reactions at GSI**

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# Detailed Investigation of Residual Nuclei Produced in Spallation Reactions at GSI

José Benlliure

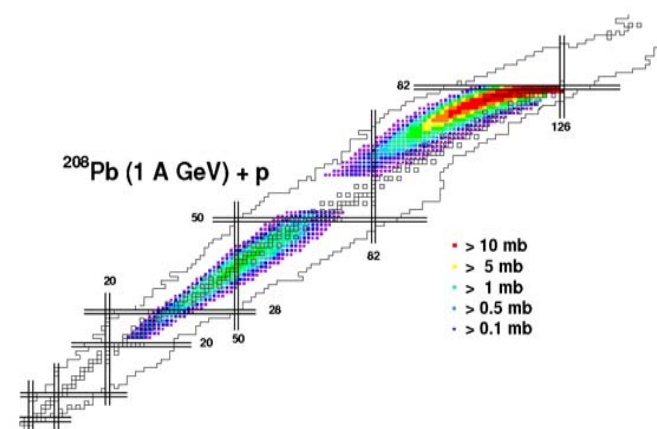
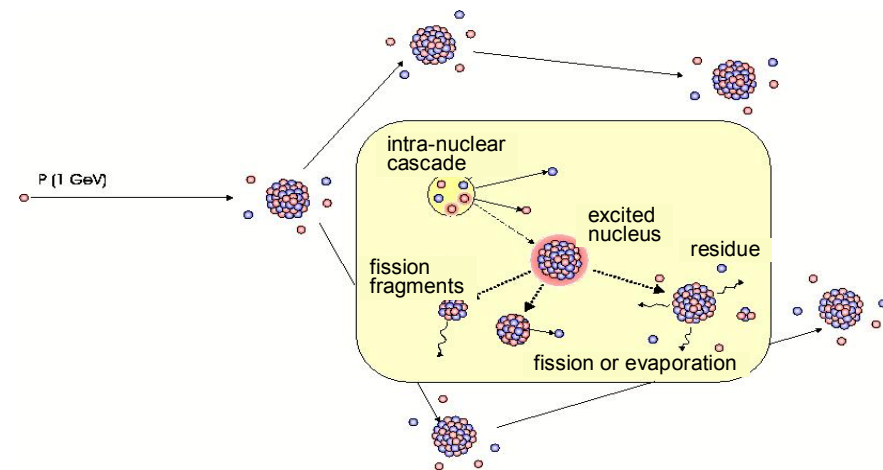
University of Santiago de Compostela  
Spain

# Motivation

## Accurate measurements of isotopic production cross sections of spallation residues

Residual nuclei provide information on both stages of the collision:

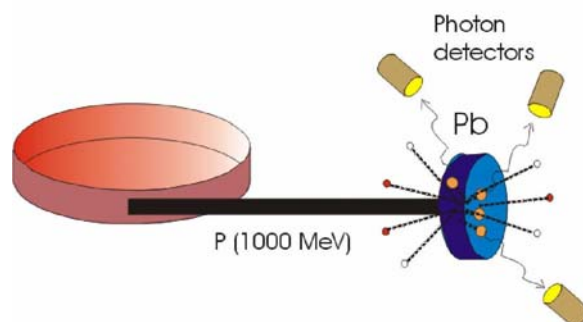
- Residues close in neutron and atomic number to the initial nucleus are more sensitive to the first stage of the collision
- Lighter residues are more sensitive to the de-excitation phase (evaporation or fission)



# Experimental technique

## Reaction kinematics

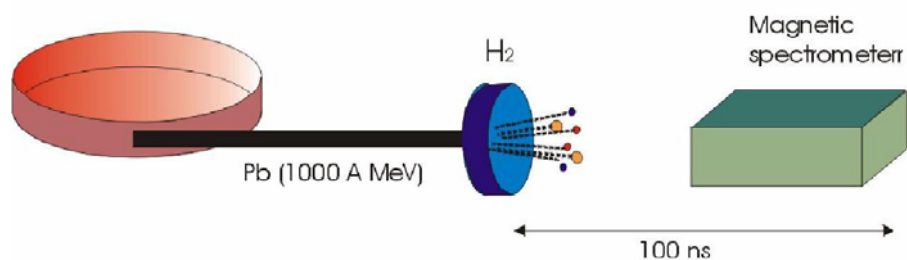
### Direct kinematics



### $\gamma$ -ray spectroscopy or mass spectrometry

- simple experimental set-up
- fast experiments: full excitation functions
- residue identification after  $\beta$ -decay
- mostly isobaric distributions are provided
- no kinematical information

### Inverse kinematics



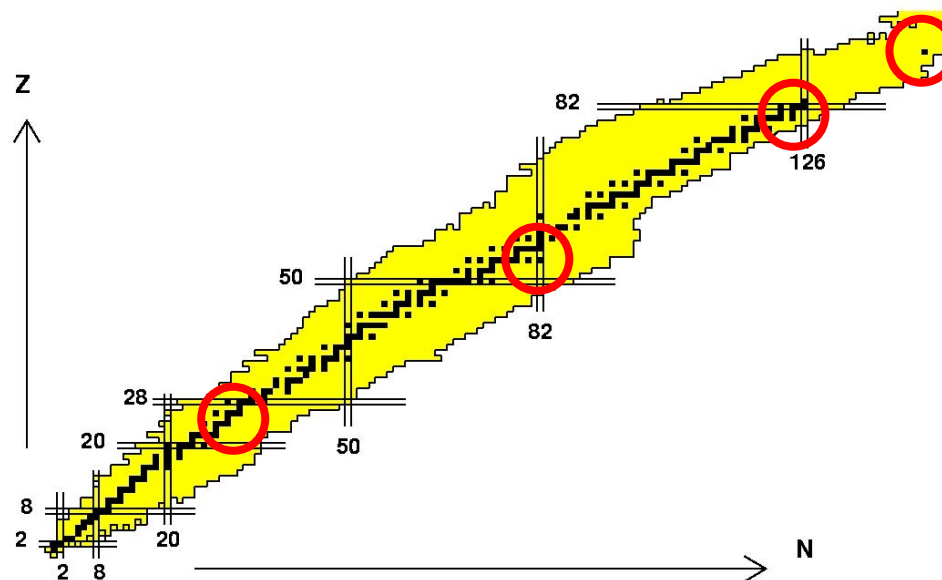
### In-flight magnetic identification

- full isotopic identification
- momentum measurement
- complicated experimental set-up
- long beam times
- only selected reactions can be investigated

# Experimental programme

## Experimental programme

- ✓  $^{238}\text{U}(1000 \text{ A MeV})+p,d$
- ✓  $^{208}\text{Pb}(1000 \text{ A MeV})+p,d$
- ✓  $^{208}\text{Pb}(500 \text{ A MeV})+p$
- ✓  $^{197}\text{Au}(800 \text{ A MeV})+p$
- ✓  $^{136}\text{Xe}(1000,500,200 \text{ A MeV})+p$
- ✓  $^{56}\text{Fe}(1000,500 \text{ A MeV})+p$



Collaboration GSI,IPN-Orsay,SPhN-Saclay,USC, CENBG

Partially funded by UE under FP5 HINDAS project

# Layout

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- ✓ Experimental technique
  - Isotopic identification of spallation residues
  - Cross sections determination
  
- ✓ Results
  - Isotopic production cross sections
  - Longitudinal momentum distributions
  
- ✓ The first stage of the collision
  
- ✓ Pre-fragment de-excitation
  - Fission
  - Statistical evaporation
  - Intermediate-mass fragment emission
  
- ✓ Summary

# Experimental technique: setup

## Gesellschaft für Schwerionenforschung (GSI)

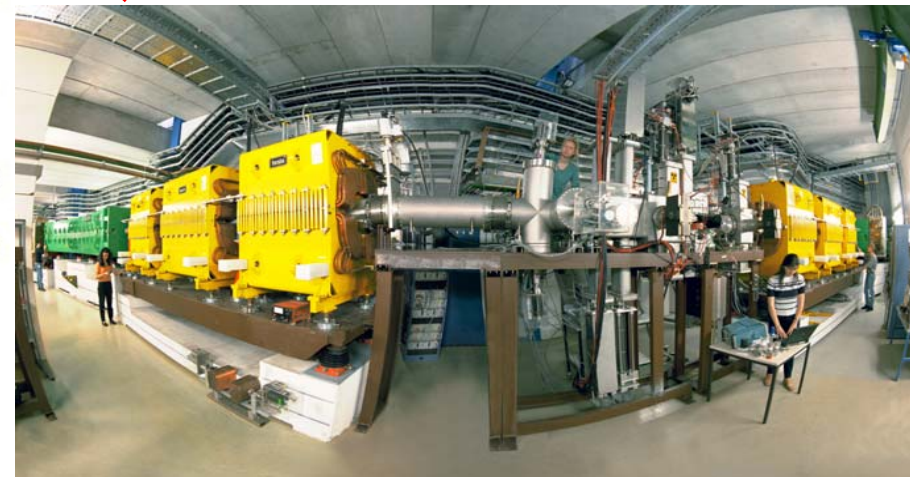
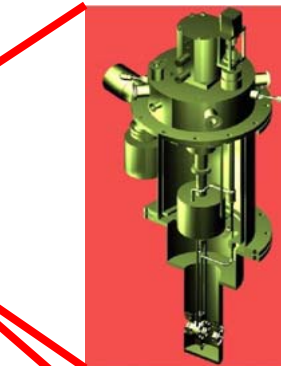
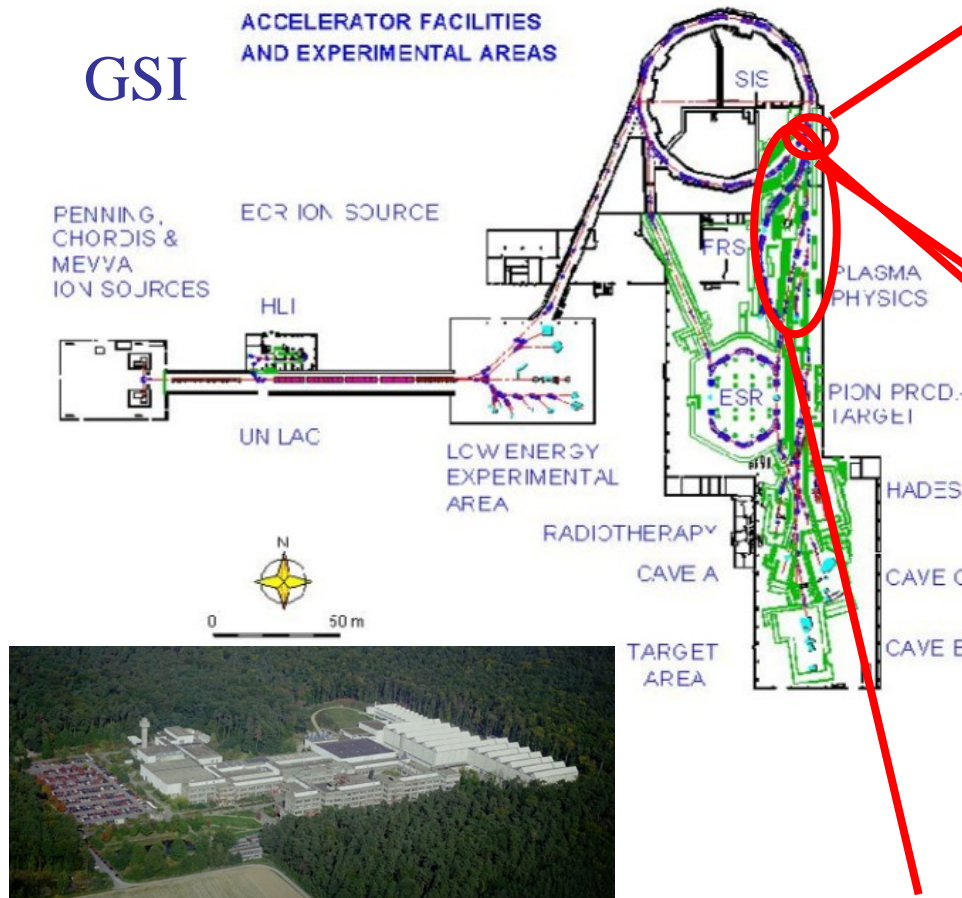
Relativistic heavy-ion beams

- pulsed beams (~ 4 s spill, 8 s cycle)
- 200 A MeV – 1000 A MeV

Secondary Electron Monitor (SEETRAM)

Cryogenic target (1 cm thickness)

- 1 cm thick., Ti windows (36 mg/cm<sup>2</sup>)
- H<sub>2</sub> (87 mg/cm<sub>2</sub>), D<sub>2</sub> (201 mg/cm<sup>2</sup>)



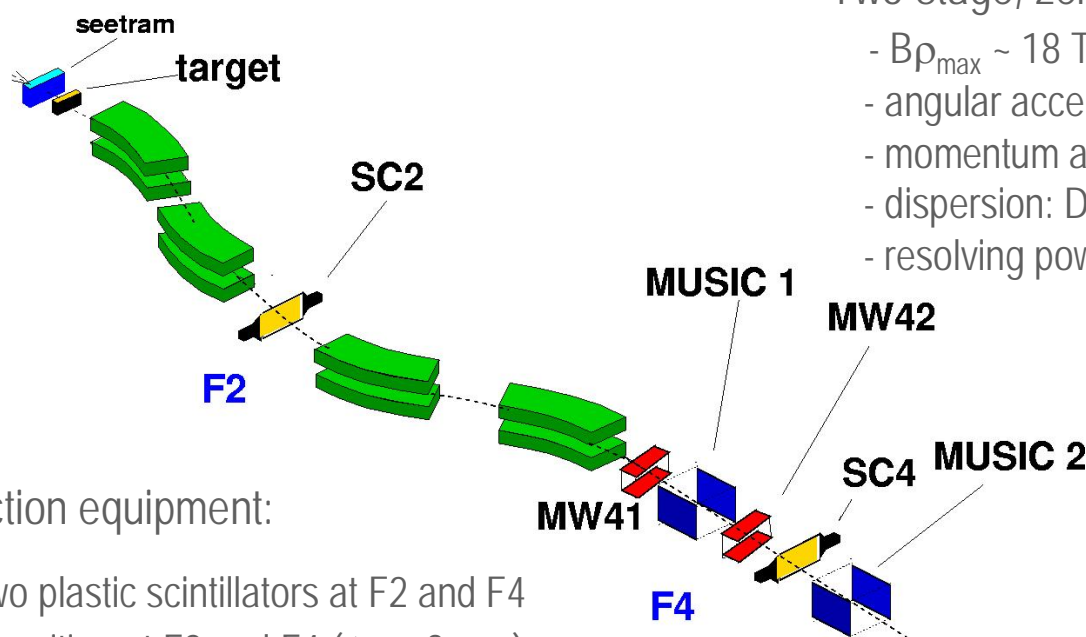
José Benlliure, Advanced Workshop on Spallation Models

ICTP-Trieste, Feb. 4-8, 2008



# Experimental technique:setup

## FRagment Separator (FRS)



Two-stage, zero degree achromatic spectrometer:

- $B\rho_{\max} \sim 18 \text{ Tm}$
- angular acceptance:  $\Delta\theta \sim 15 \text{ mrad}$
- momentum acceptance:  $\Delta p/p \sim 3\%$
- dispersion:  $D_{\text{TA-F2}} \sim 7 \text{ cm}/\%$  (F2 image plane  $\sim 20 \text{ cm}$ )
- resolving power:  $B\rho/\Delta B\rho \sim 1500$

Detection equipment:

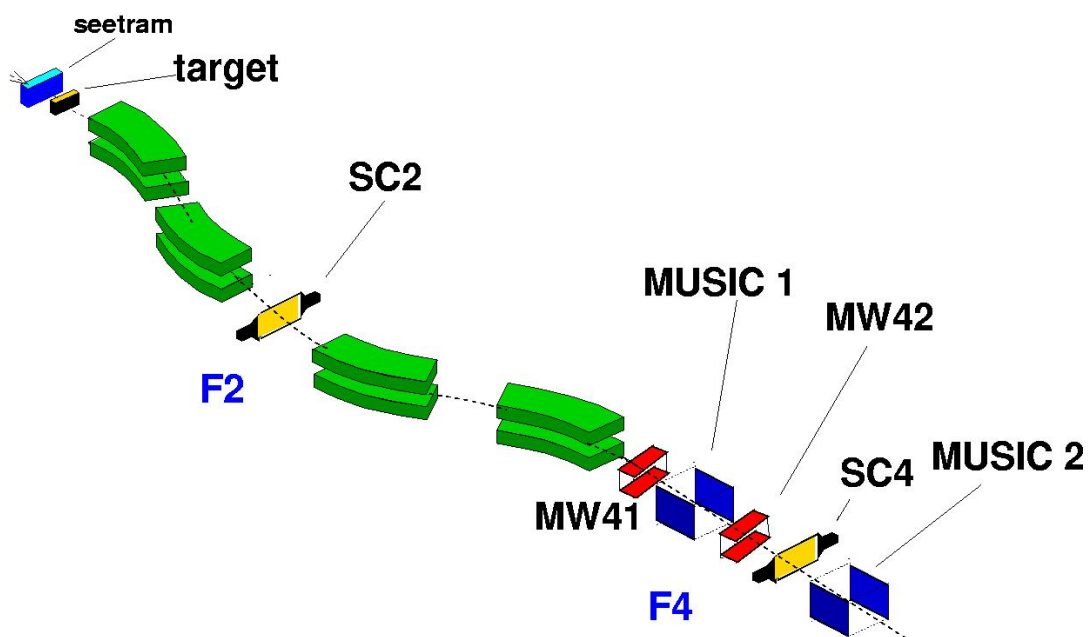
- Two plastic scintillators at F2 and F4  
position at F2 and F4 ( $\Delta x \sim 3 \text{ mm}$ )  
F2-F4 Time of Flight ( $\Delta\text{ToF} \sim 150 \text{ ps}$ )
- Multi-Sampling Ionisation Chamber (MUSIC)  
 $dE/dx$ , position and angle
- Multi-wire chambers for position calibrations

$$\frac{A}{Q} \propto \frac{B\rho}{\beta\gamma}$$



# Experimental technique:setup

## Fragment Separator (FRS)



✓ (A/Z) identification:  $\frac{A}{Z} \propto \frac{B\rho}{\beta\gamma}$

$$\begin{cases} B\rho = (B\rho)_0 \cdot \left(1 - \frac{x_2 - M_2 x_4}{D_1}\right) \\ \beta\gamma = \frac{L}{c \cdot \text{ToF}} \cdot \left(1 - \frac{L^2}{c^2 \cdot \text{ToF}^2}\right)^{-1/2} \end{cases}$$

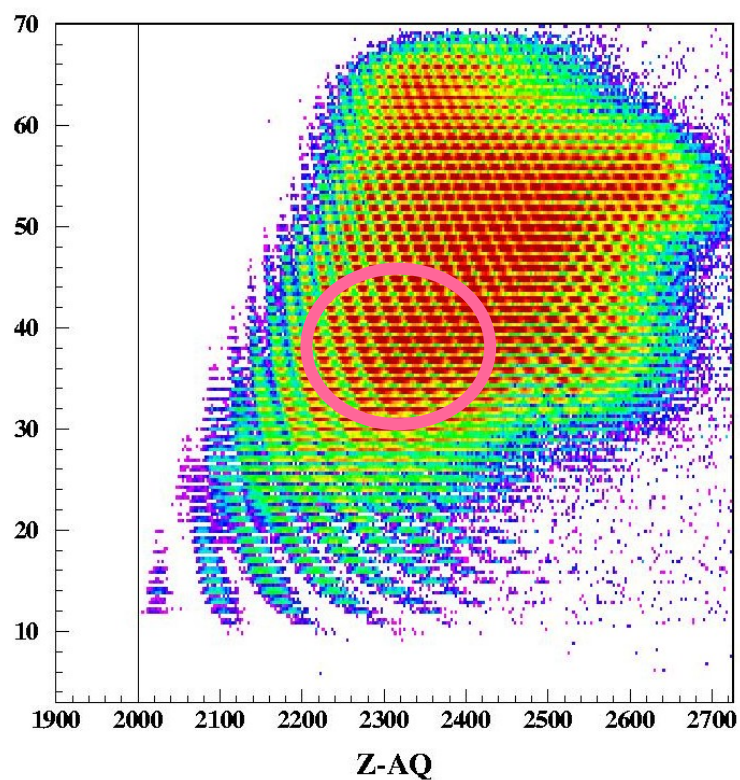
✓ Z identification:  $Z \propto \sqrt{dE/dx}$

✓ Longitudinal velocities:

$$v \rightarrow \beta\gamma = \frac{Z}{A} B\rho$$

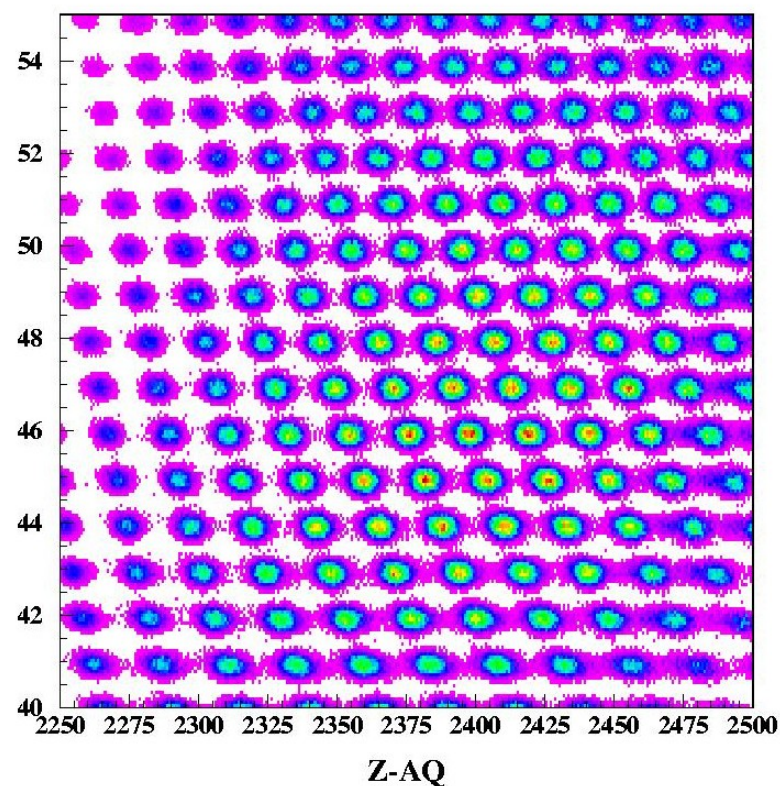
# Experimental technique: isotopic identification

## Isotopic identification procedure



More than 1000  
fission  
Fragments identified  
in the reaction  
 $^{238}\text{U}(1 \text{ A GeV})+d$

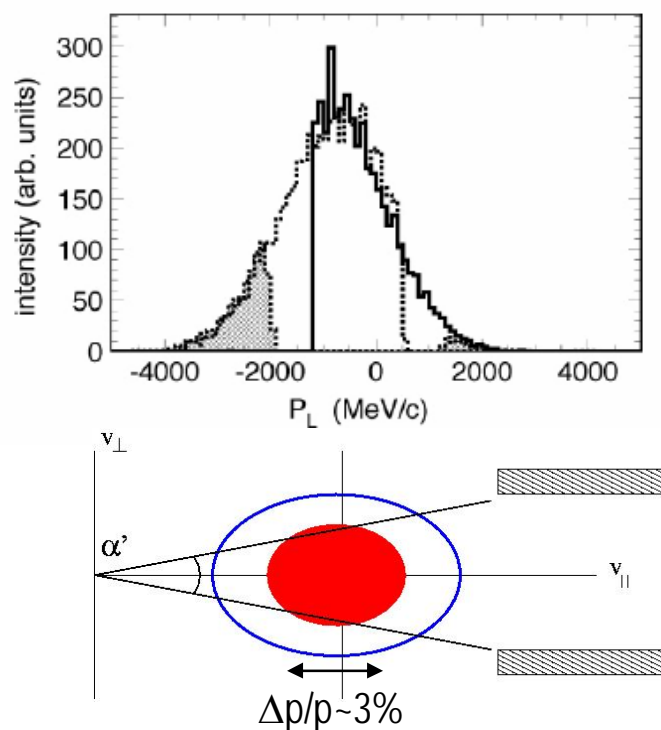
J. Pereira, et al.,  
PRC 75 (2007) 014602



# Experimental technique: isotopic production yields

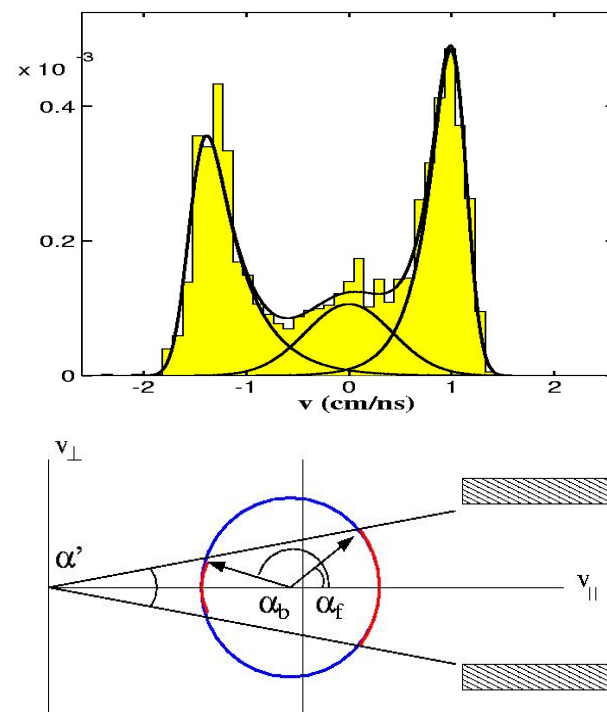
## Reconstruction of the longitudinal momentum distribution

### Fragmentation



$$T_{fr} = 1 - \exp\left(-\frac{\alpha^2}{2\sigma(\theta)^2}\right)$$

### Fission



$$T_f = \frac{1 - \cos \alpha_f}{2}$$

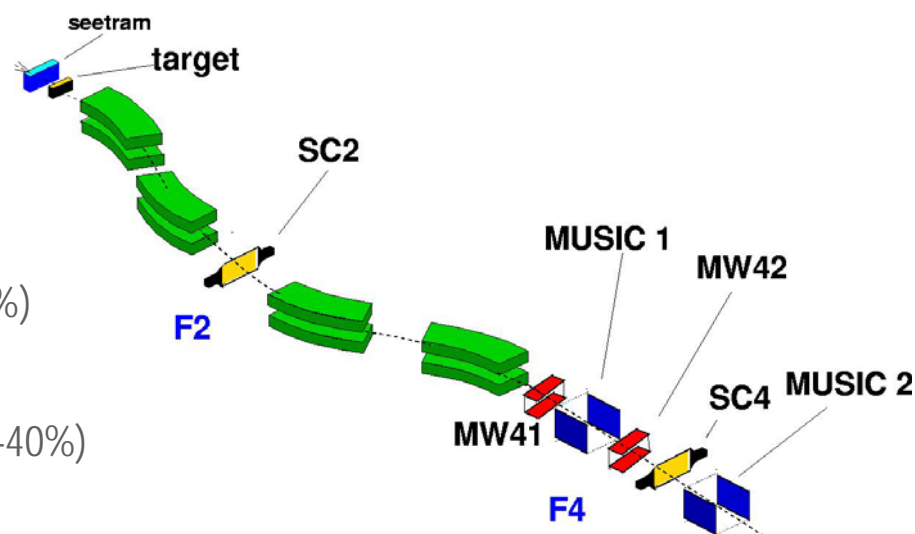
$$T_b = \frac{1 + \cos \alpha_b}{2}$$

# Experimental technique: isotopic production yields

## Reconstruction of the isotopic production yields

$$Y(Z,A) = Y^{\text{mes}}(Z,A) \cdot f_{\text{sc2}} \cdot f_{\text{eff}} \cdot f_{\text{chs}} \cdot f_{\text{Ti}} \cdot f_{\text{mr}} \cdot f_{\text{T}} \cdot f_{\text{DT}}$$

- $f_{\text{sc2}}$ : Interactions of nuclei in scintillator SC2 (~5%)
- $f_{\text{eff}}$ : Detection efficiencies (~97%)
- $f_{\text{chs}}$ : Charge-state contamination (~1-30%)
- $f_{\text{Ti}}$ : Nuclear reactions in the Ti target container (~1%)
- $f_{\text{mr}}$ : Multiple-reactions in the target (~5-30%)
- $f_{\text{T}}$ : Angular transmission (frag. ~85-100%, fission ~10-40%)
- $f_{\text{DT}}$ : Acquisition dead time (~20%)



# Experimental technique: cross sections

## Determination of the isotopic production cross sections

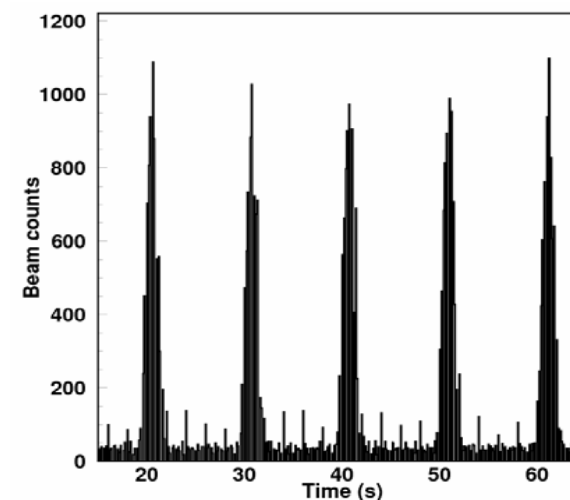
$$\sigma(N, Z) = \frac{Y(N, Z)}{N_{pro} \cdot N_{tar}}$$

### Accuracy

- ✓ Beam intensity: ~5-10%
- ✓ Target thickness: ~5%
- ✓ yield statistics: < 1%
- ✓ yield corrections: ~5-30%

final accuracy

- fragmentation ~ 5-15%
- fission ~ 15-30%



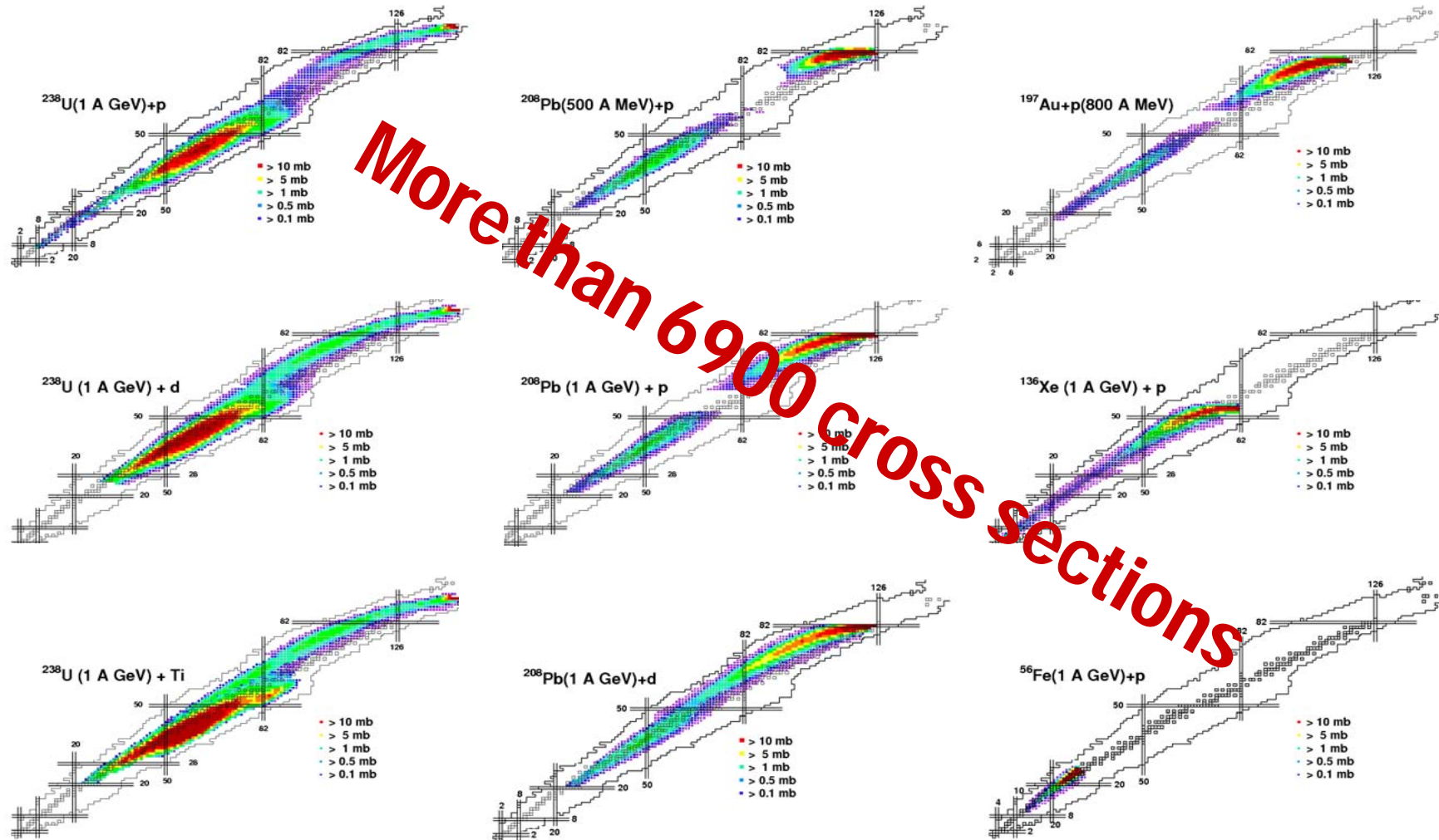
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- ✓ Experimental technique
  - Isotopic identification of spallation residues
  - Cross sections determination
  
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  - Intermediate-mass fragment emission
  
- ✓ Summary

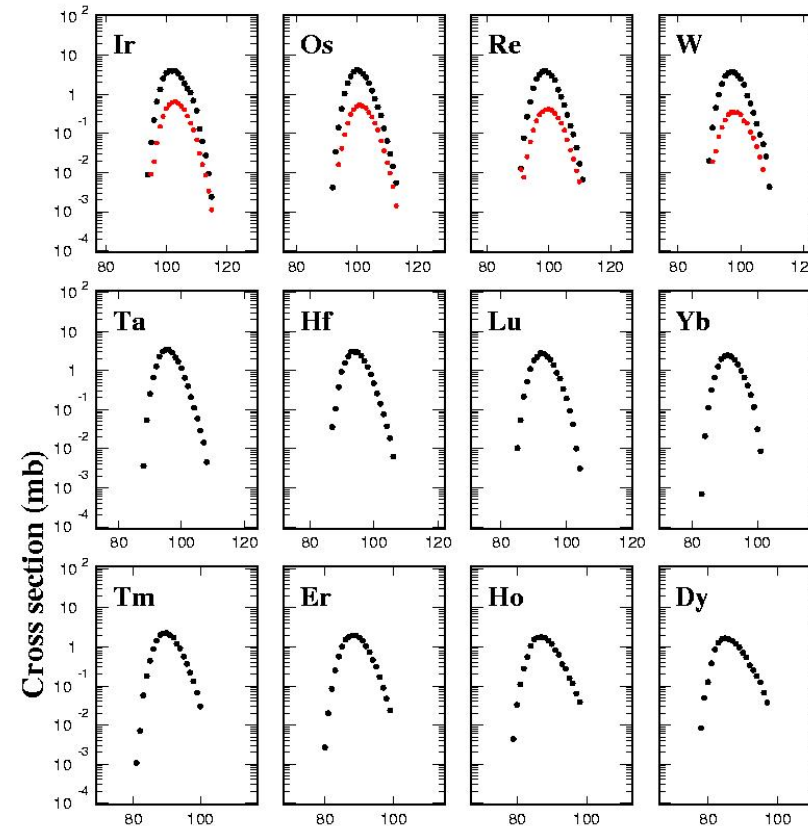
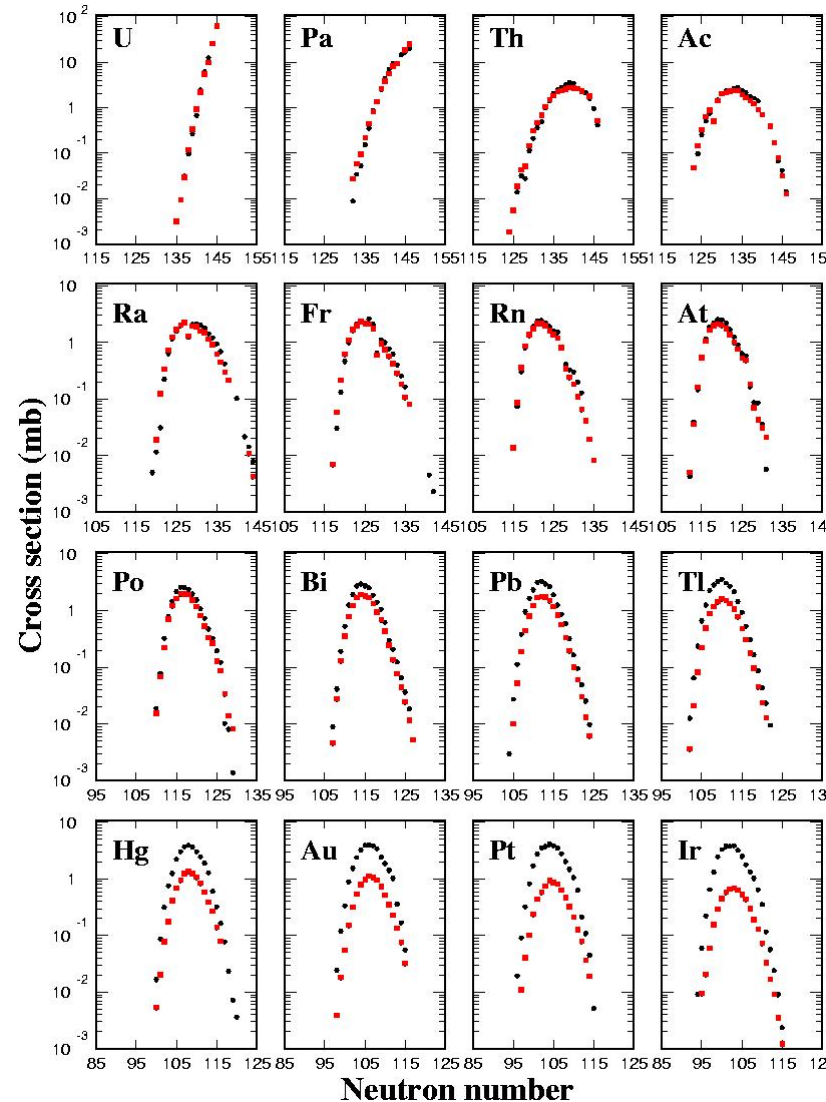


# Results: Isotopic Production Cross Sections





# Results: Isotopic Production Cross Sections



$^{238}\text{U}(1 \text{ A GeV}) + p$

$^{238}\text{U}(1 \text{ A GeV}) + d$

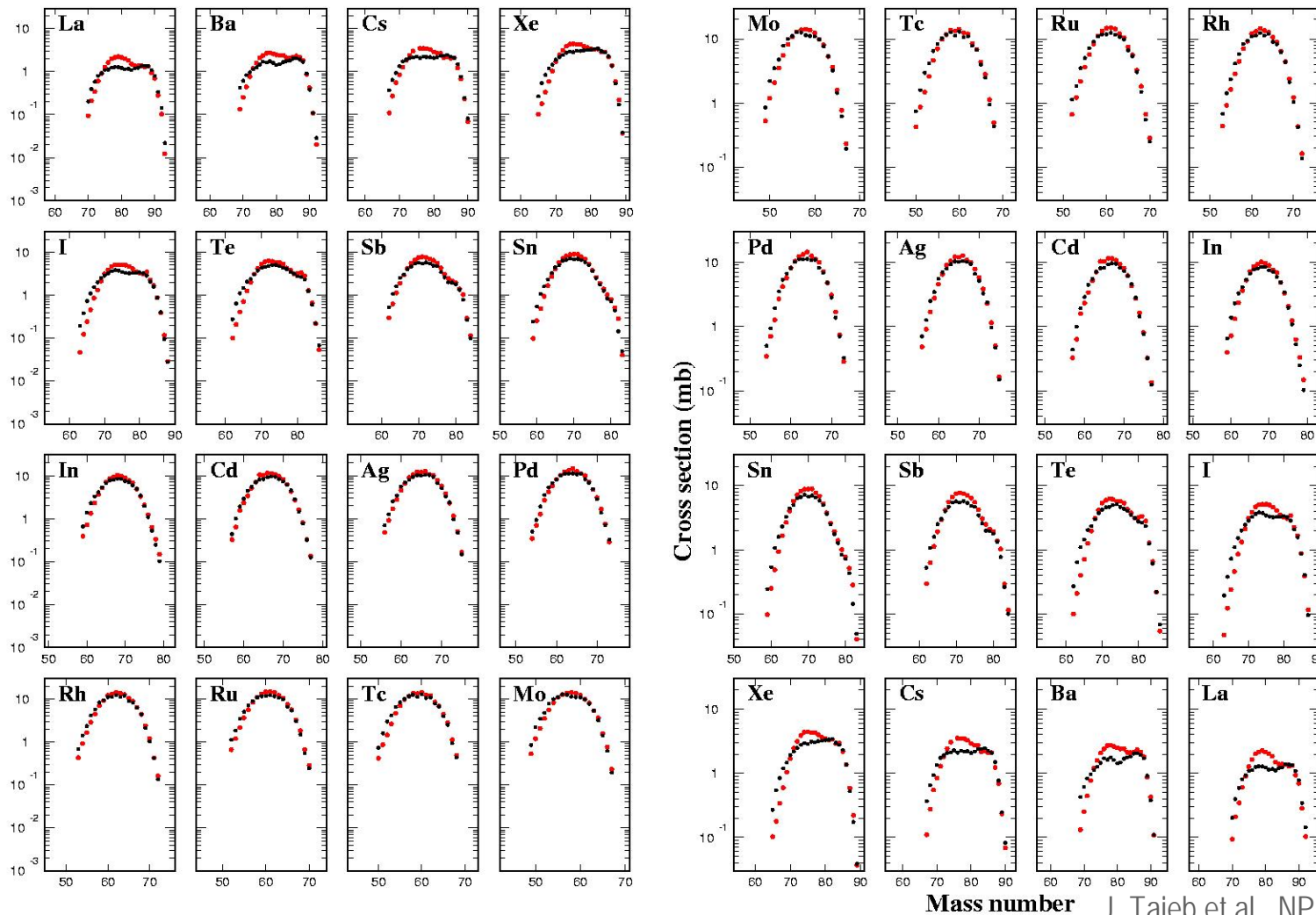
Evaporation residues

M. Bernas et al., NPA 725 (2003) 213

E. Casarejos et al., PRC 74 (2006) 044612

ICTP-Trieste, Feb. 4-8, 2008

# Results: Isotopic Production Cross Sections



$^{238}\text{U}(1 \text{ A GeV}) + p$

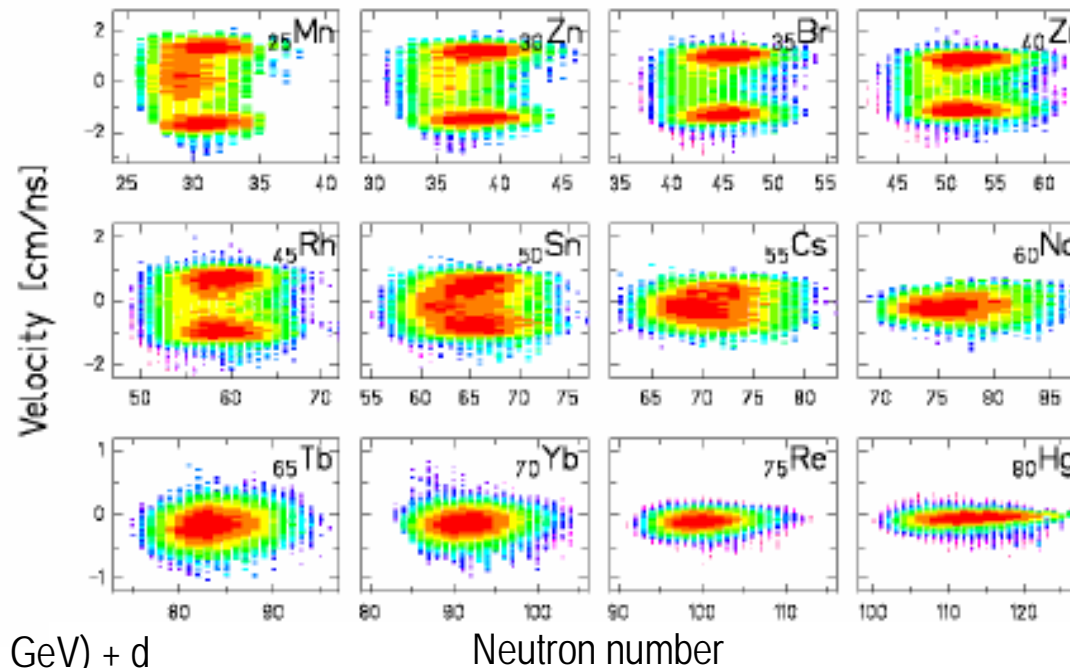
$^{238}\text{U}(1 \text{ A GeV}) + d$

Fission residues

J. Taieb et al., NPA 724 (2003) 413

J. Pereira et al., PRC 75 (2007) 014602

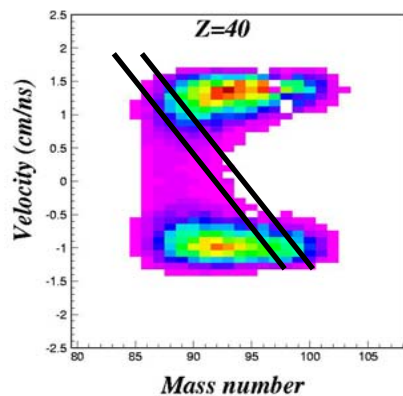
# Results: Velocity distributions



$^{208}\text{Pb}(1 \text{ A GeV}) + p$

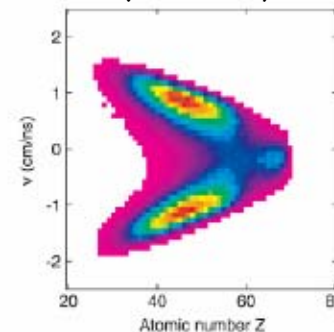
T. Enqvist et al.,  
NPA 686 (2001) 481

$^{238}\text{U}(1 \text{ A GeV}) + d$

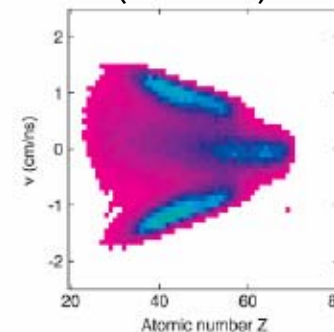


J. Pereira et al.,  
PRC 75 (2007) 014602

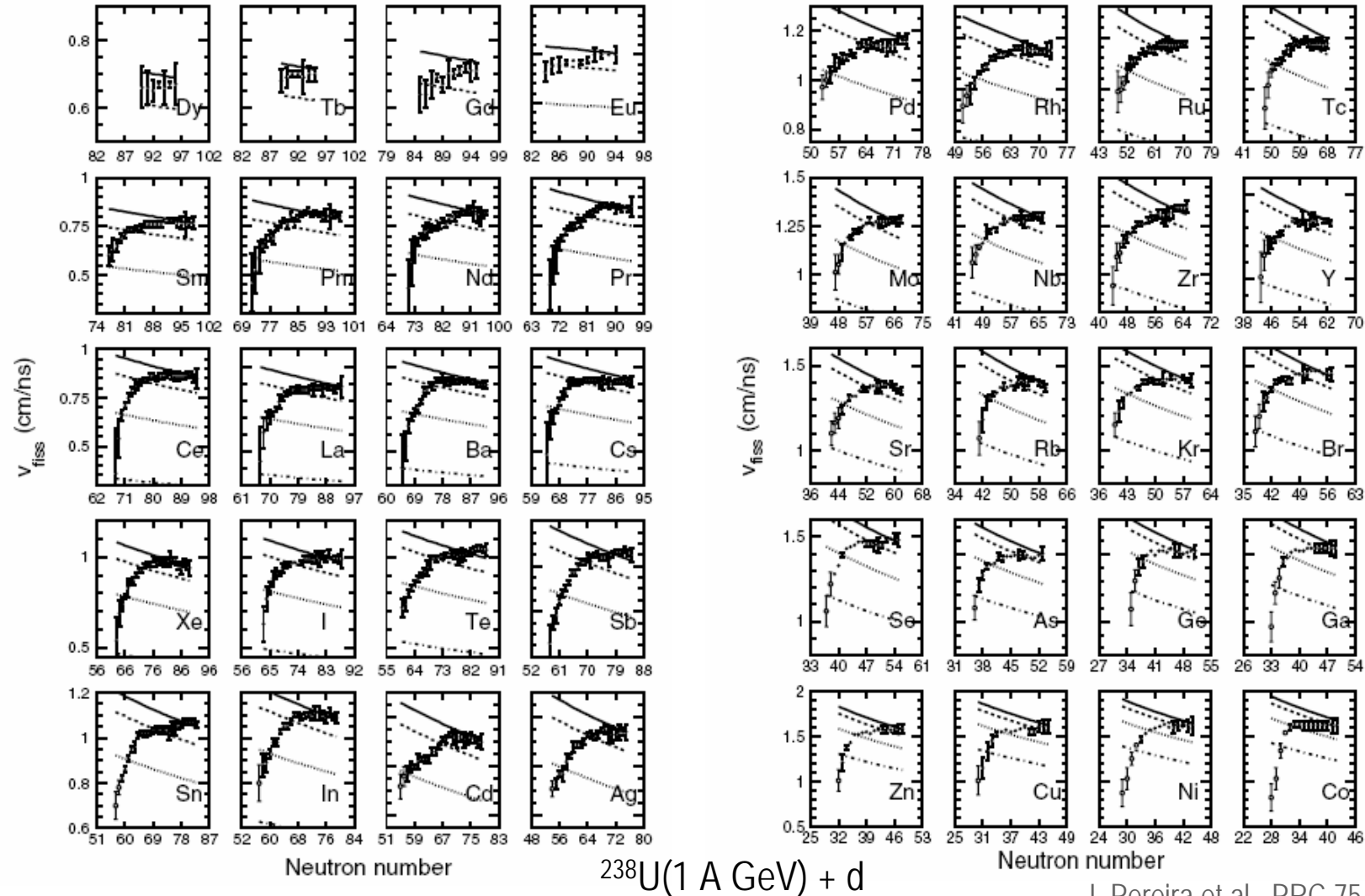
$^{238}\text{U}(1 \text{ A GeV}) + d$



$^{238}\text{U}(1 \text{ A GeV}) + \text{Ti}$



# Results: Velocity distributions



J. Pereira et al., PRC 75 (2007) 014602

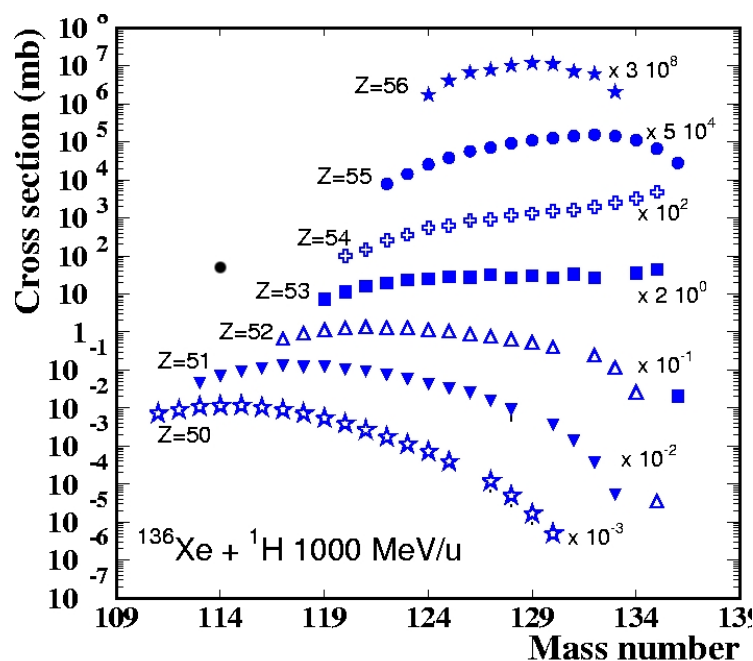
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# The first stage of the collision

$^{136}\text{Xe}(1 \text{ A GeV}) + p$



Residual nuclei close in neutron and atomic number to the initial nucleus are more sensitive to the first stage of the collision

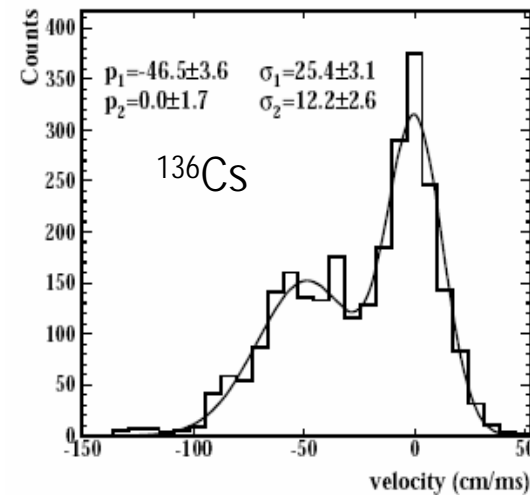
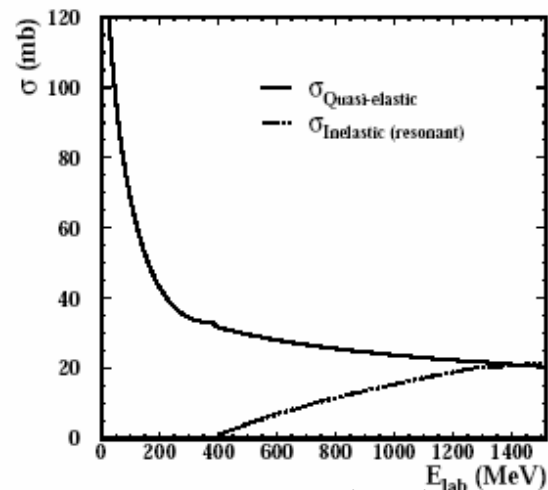
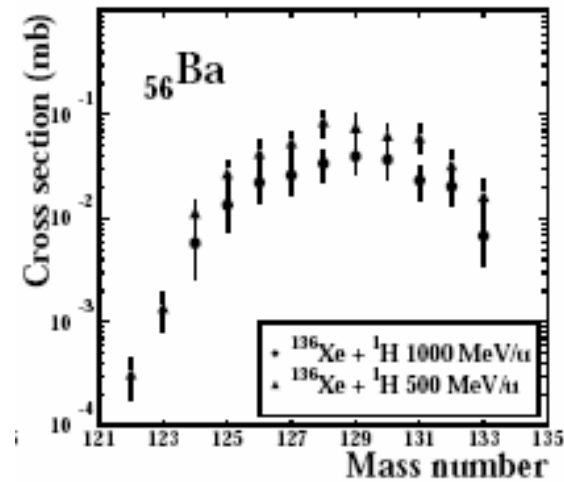
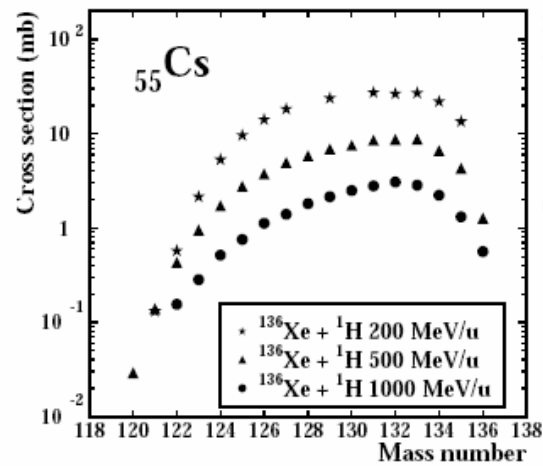
- In particular the charge-exchange channels can provide insight into the NN interaction in the nuclear medium

M. Fernández., PhD USC (2008), to be published



# The first stage of the collision

$^{136}\text{Xe}(1 \text{ A GeV}) + p$



M. Fernández., PhD USC (2008), to be published

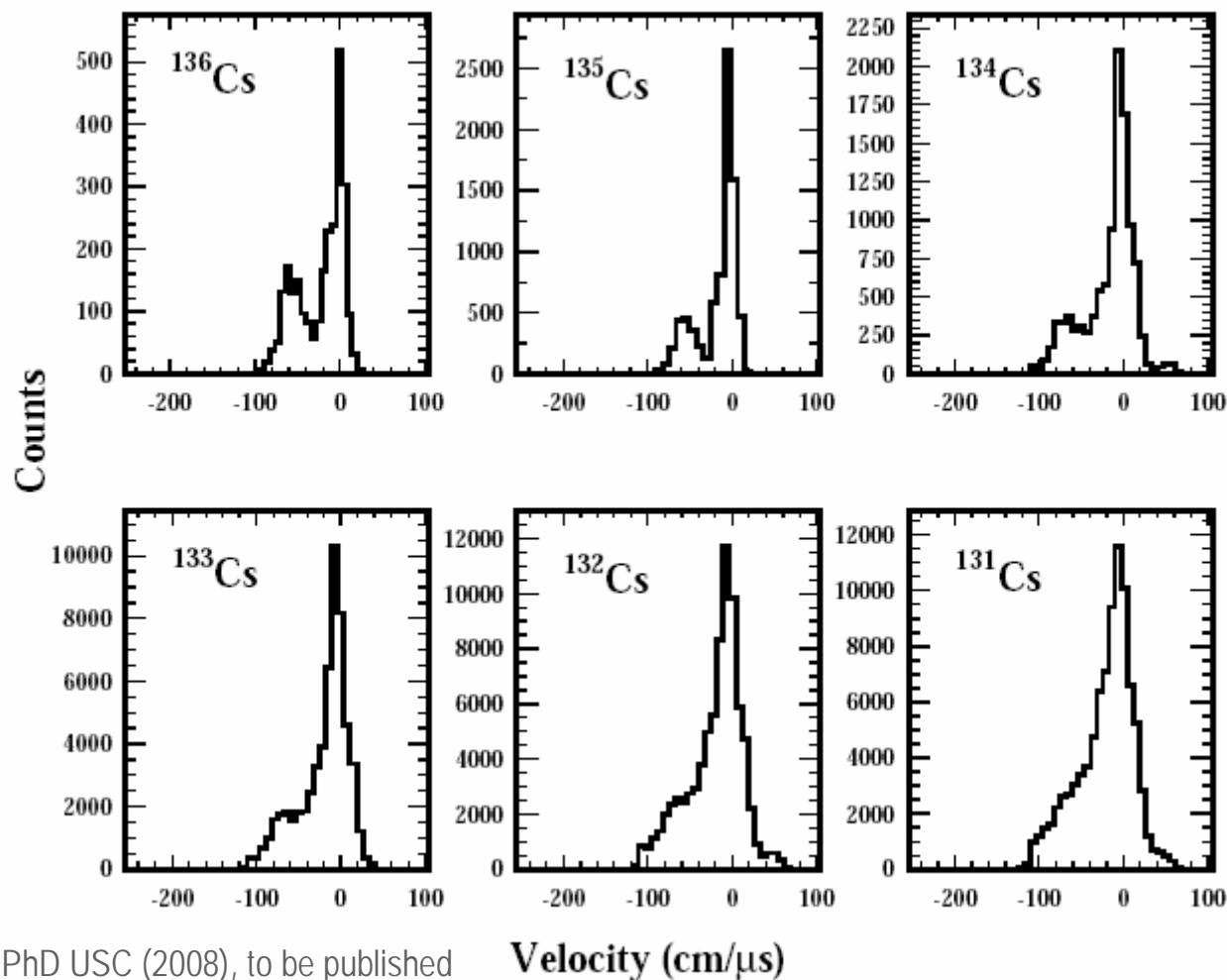
José Benlliure, Advanced Workshop on Spallation Models

ICTP-Trieste, Feb. 4-8, 2008



# The first stage of the collision

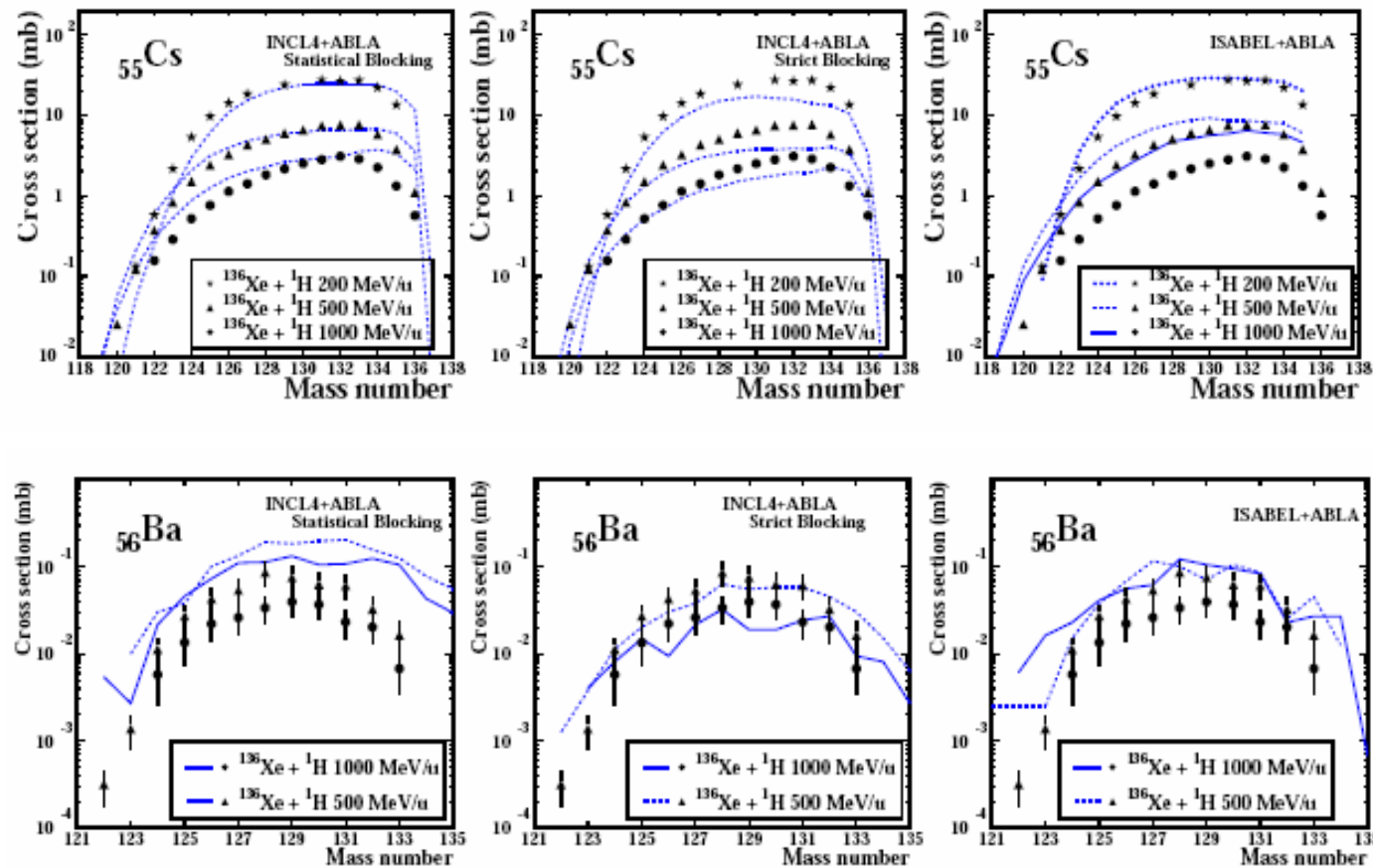
$^{136}\text{Xe}(1 \text{ A GeV}) + \text{p}$



M. Fernández., PhD USC (2008), to be published

# The first stage of the collision

$^{136}\text{Xe}(1 \text{ A GeV}) + p$



M. Fernández., PhD USC (2008), to be published

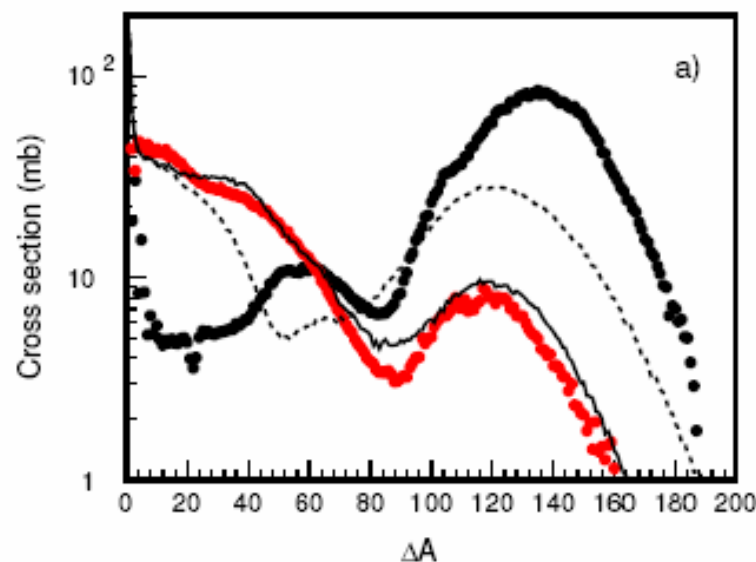
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  - Statistical evaporation
  - Intermediate-mass fragment emission
  
- ✓ Summary

# Pre-fragment de-excitation: fission

Fission probability:  $\Gamma_f/\Gamma_n$



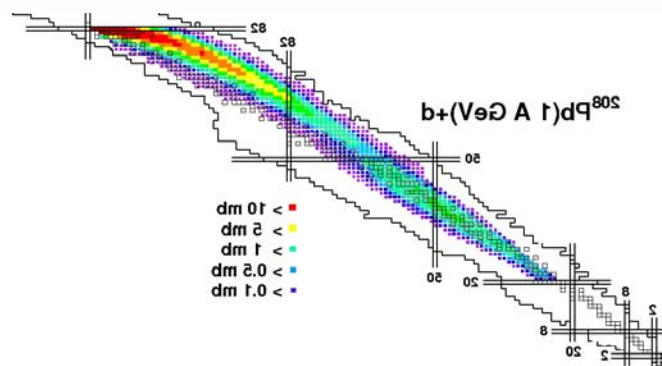
$^{208}\text{Pb}(1 \text{ A GeV}) + d$

$^{238}\text{U}(1 \text{ A GeV}) + d$

Isabel+ABLA ( $^{208}\text{Pb}(1 \text{ A GeV})+d$ )

---  $\Gamma_f$ : statistical model for fission

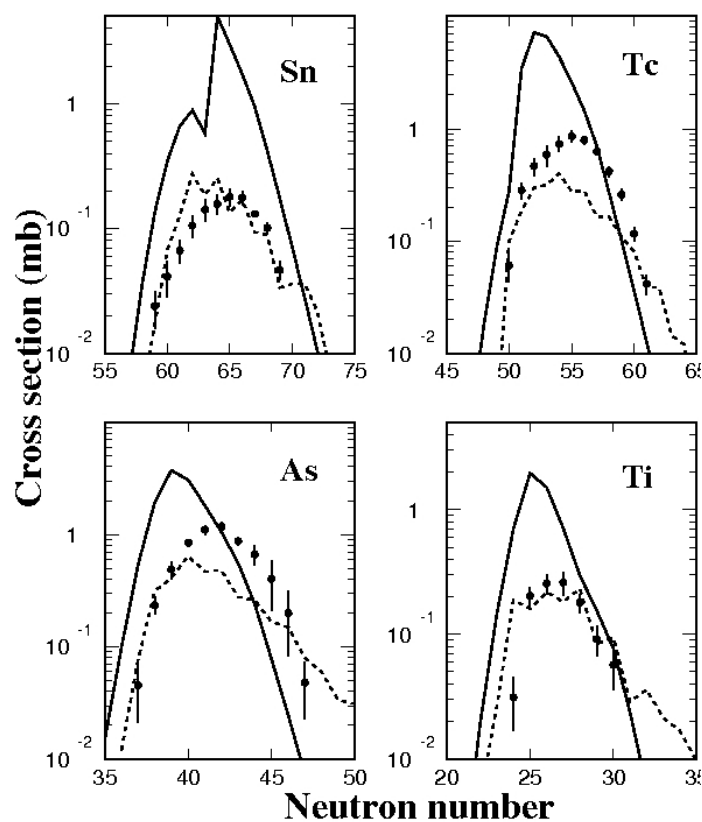
—  $\Gamma_f$ : dynamical model for fission



J. Benlliure et al., PRC 74 (2006) 014609

# Pre-fragment de-excitation: fission

## Isotopic distribution of fission yields



$^{197}\text{Au}(800 \text{ A MeV})+p$

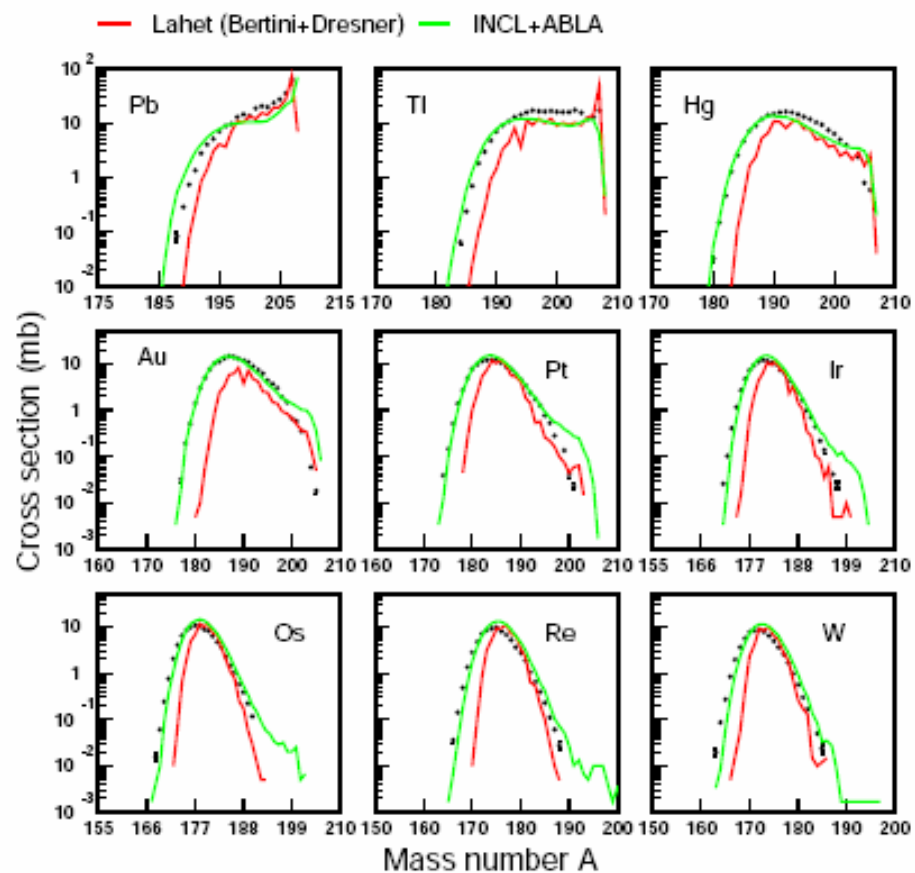
--- LAHET (Bertini+Dresner)

— R. Silberberg et al. Astr. Phys. J. 501 (1998) 911

J. Benlliure et al., NPA 683 (2001) 513

# Pre-fragment de-excitation: statistical evaporation

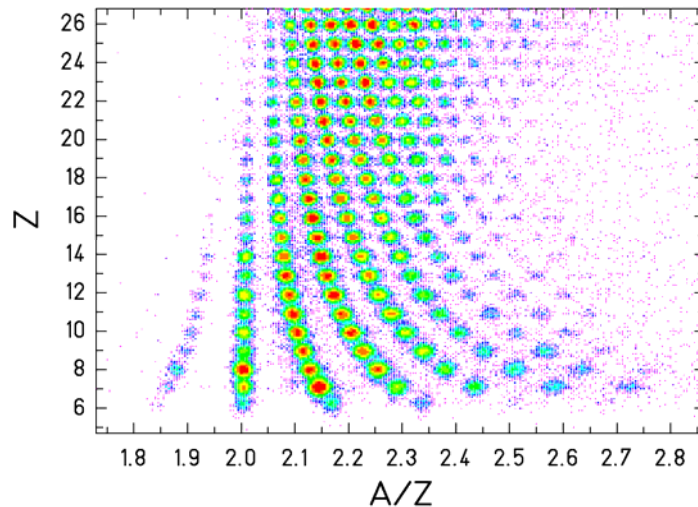
Fission probability:  $\Gamma_f/\Gamma_n$



F. Rejmund et al., NPA 683 (2001) 540

# Pre-fragment de-excitation: statistical evaporation

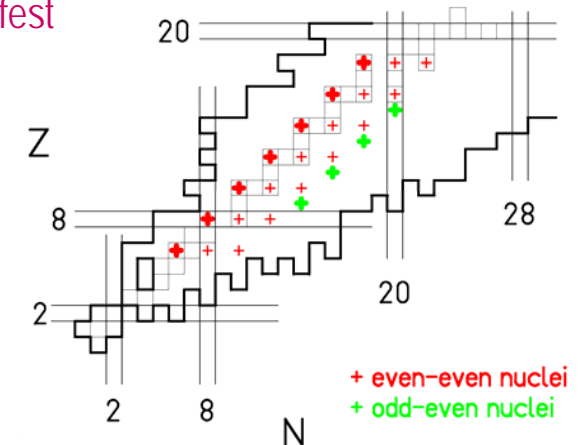
## Even-odd staggering



New complex structures manifest in the isotopic distribution of reaction residues

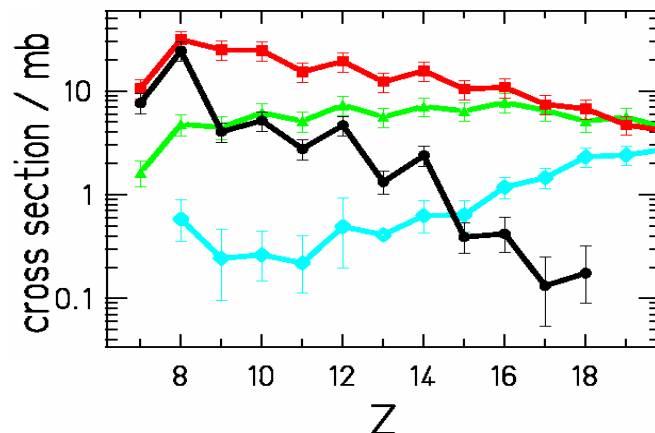
M.V. Ricciardi et al.,  
Nucl. Phys. A 733 (2004) 299

## Nuclei with enhanced production

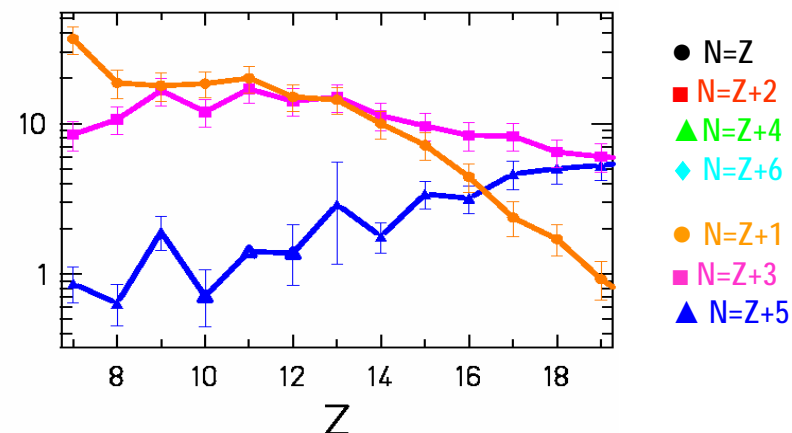


$N-Z = \text{constant}$

Even-mass nuclei



Odd-mass nuclei

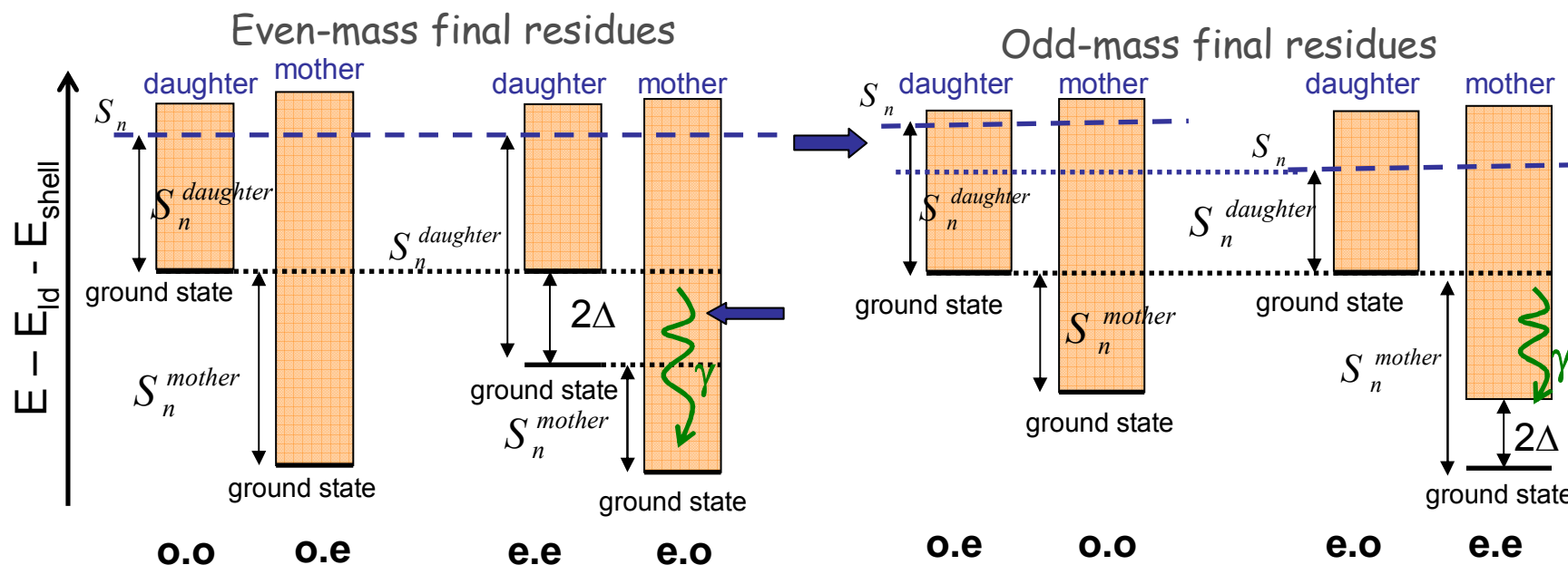




# Pre-fragment de-excitation: statistical evaporation

## Even-odd staggering

The final yields are governed by the number of bound states in both, the daughter and the mother nuclei, which are defined by level densities, ground state masses and separation energies.

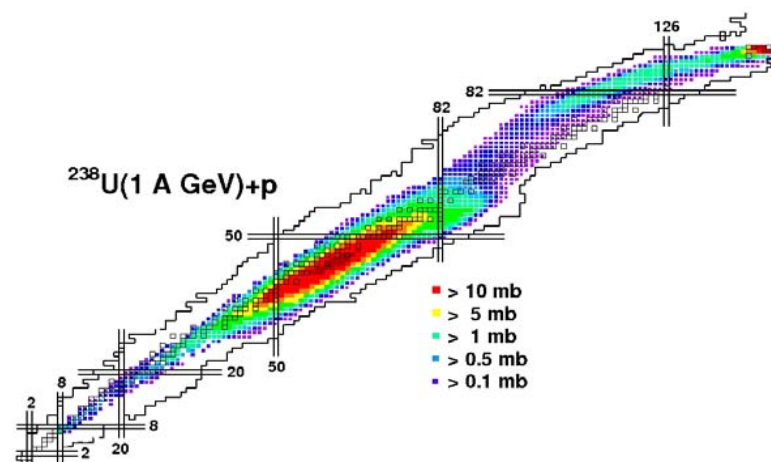
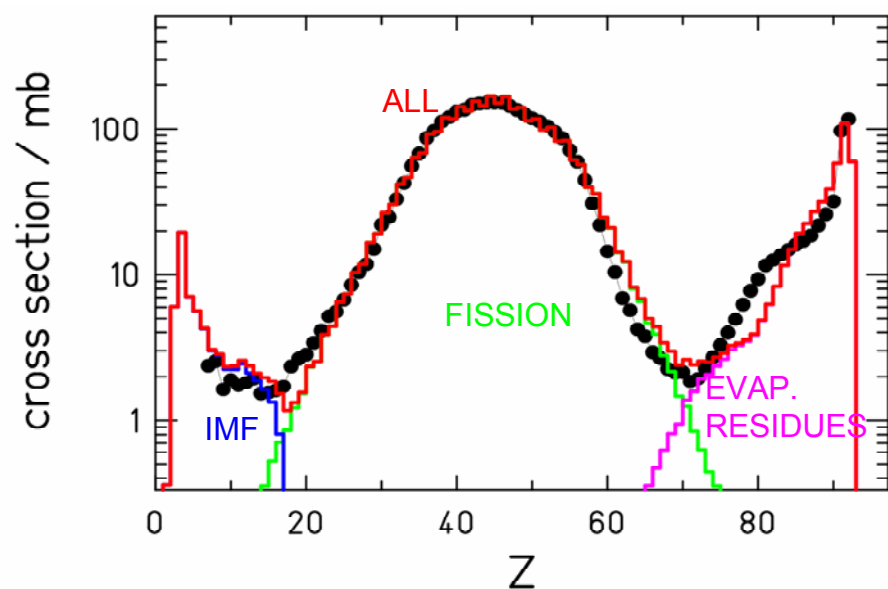


- ✓ Even-mass residues with even-Z are more probable
- ✓ Odd-mass residues with odd-Z are also more probable
- ✓ Even-odd staggering decreases with the mass (g emission)

# Pre-fragment de-excitation: intermediate-mass fragments

Fission probability:  $\Gamma_f/\Gamma_n$

$^{1238}\text{U}(1 \text{ A GeV}) + p$



M.V. Ricciardi et al., PRC 73 (2006) 014607

# Summary

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- ✓ A large data set on residual nuclei produced in spallation reactions have been obtained at GSI
  - 14 reactions have been investigated using five projectiles ( $^{238}\text{U}$ ,  $^{208}\text{Pb}$ ,  $^{197}\text{Au}$ ,  $^{136}\text{Xe}$  and  $^{56}\text{Fe}$ ) cryogenic proton and deuterium targets and different projectile energies
  - More than 7000 cross sections have been determined with an accuracy between 5 and 30%
  
- ✓ The sensitivity of these data to different aspects of the modelization of spallation reactions has been investigated
  - Residual nuclei close in neutron and atomic number to the projectile, in particular charge-exchange reactions, probe the intra-nuclear cascade phase
  - The comparison between fissile and less fissile systems helps in characterising the neutron/fission competition during the evaporation phase
  - The emission of intermediate-mass fragments or the even-odd staggering in the cross provide also information on the evaporation phase

## Collaborators

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P. Armbruster<sup>a</sup>, **L. Audouin**<sup>b</sup>, J. Benlliure<sup>a,c</sup>, M. Bernás<sup>b</sup>, A. Boudard<sup>d</sup>, **E. Casarejos**<sup>c</sup>,  
 S. Czajkowski<sup>e</sup>, T. Enqvist<sup>a</sup>, **B. Fernández**<sup>d</sup>, **M. Fernández**<sup>c</sup>, L. Giot<sup>a</sup>, A. Kelic<sup>a</sup>, R. Legrain<sup>d</sup>,  
 S. Leray<sup>d</sup>, **B. Mustapha**<sup>b</sup>, **P. Napolitani**<sup>a,b</sup>, C. Paradela<sup>b,c</sup>, **J. Pereira**<sup>c</sup>, M. Pravikoff<sup>e</sup>,  
 F. Rejmund<sup>a,b</sup>, K.-H. Schmidt<sup>a</sup>, C. Stéphan<sup>b</sup>, **J. Taieb**<sup>a,b</sup>, L. Tassan-Got<sup>b</sup>, **C. Villagrasa**<sup>d</sup>,  
 C. Volant<sup>d</sup>, W. Wlazlo<sup>d</sup>

- a) Gesellschaft für Schwerionenforschung, D-64291, Germany
- b) Institut de Physique Nucléaire, F-91406 Orsay cedex, France
- c) Universidade de Santiago de Compostela, E-15782 Santiago de Compostela, Spain
- d) DAPNIA/SPhN, CEA/Saclay, F-91191 Gif sur Yvette cedex, France
- e) CENBG, F-33175 Gradignan cedex, France

## Publications list

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### $^{238}\text{U}(1 \text{ A GeV})+p$

- J. Taieb et al., Nucl. Phys. A 724 (2003) 413
- M. Bernas et al., Nucl. Phys. A 725 (2003) 213
- M. Bernas et al., Nucl. Phys. A 765 (2006) 197
- M.V. Ricciardi et al., Nucl. Phys. A 701 (2002) 156
- P. Armbruster et al., Phys. Rev. Lett. 93 (2004) 212701

### $^{238}\text{U}(1 \text{ A GeV})+d$

- J. Benlliure et al., Phys. Rev. C 74 (2006) 014609
- E. Casarejos et al., Phys. Rev. C 74 (2006) 044612
- J. Pereira et al., Phys. Rev. C 75 (2006) 014602
- J. Pereira et al., Phys. Rev. C 75 (2007) 044604

### $^{208}\text{Pb}(1 \text{ A GeV})+p$

- W. Wlazlo et al., Phys. Rev. Lett. 84 (2000) 5736
- T. Enqvist et al., Nucl. Phys. A 686 (2001) 481

### $^{208}\text{Pb}(1 \text{ A GeV})+d$

- T. Enqvist et al., Nucl. Phys. A 703 (2002) 435

### $^{208}\text{Pb}(500 \text{ A MeV})+p$

- L. Audouin et al., Nucl. Phys. A 768 (2006) 1
- B. Fernandez et al., Nucl. Phys. A 747 (2005) 227

### $^{197}\text{Au}(800 \text{ A MeV})+p$

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### $^{136}\text{Xe}(1 \text{ A GeV})+p$

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### $^{56}\text{Fe}(0.3-0.5-0.75-1-1.5 \text{ A GeV})+p$

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