

# Applications of Monte Carlo method in Spallation Physics

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## Introduction of spallation reaction mechanism

### Physics Models

Intra-nuclear cascade model

Pre-equilibrium (exciton model)

Evaporation (Generalized Evaporation Model)

Fission model (Fong's Model)

## Realization of the physics models in real problem

Define Geometry

Ionization loss

Tracing till stop/exit

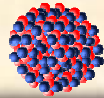
# Intra-Nuclear Cascade model

## What are the inputs we have?

Projectile: 

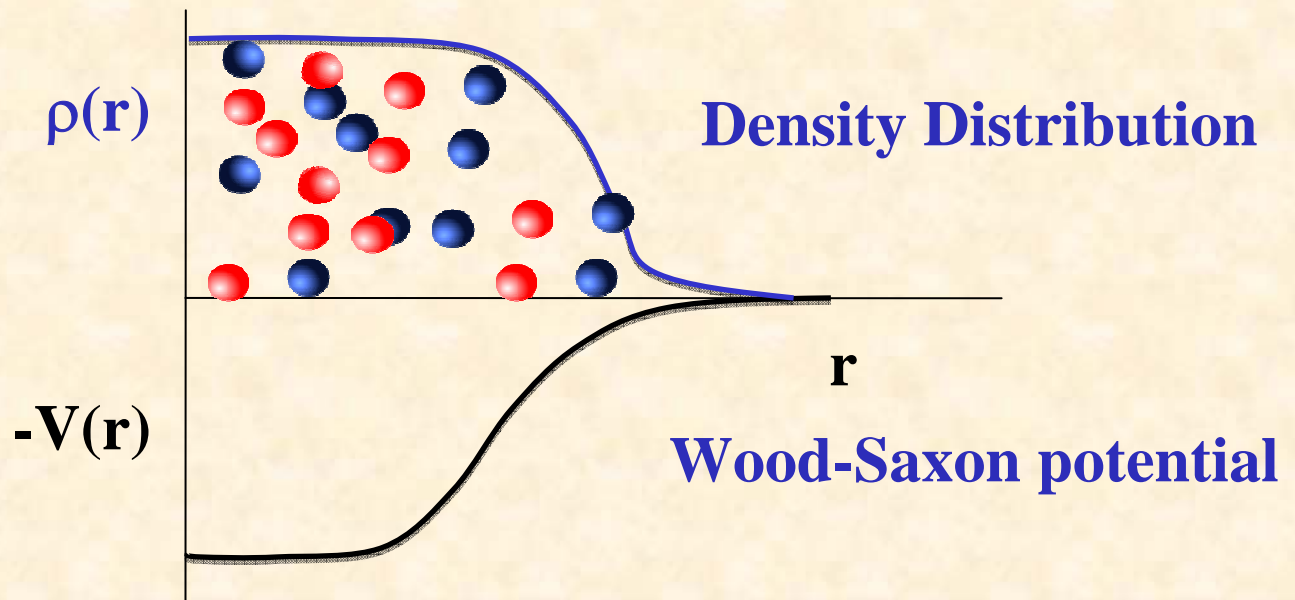
Charge, mass, energy/momentum

Target:



Charge, mass, nucleon density distribution

Each nucleon is  
assigned  
position &  
momentum  
Using Random  
Numbers



$$\left\{ \begin{array}{l} \rho(r) = \frac{\rho_0}{1 + \exp\left(\frac{r-r_0}{a}\right)} \\ \text{where } r_0 = 1.07A^{1/3} \text{ fm} \\ a = 0.545 \text{ fm} \quad \text{For } A > 10 \\ \rho(r) = \rho_0 \exp\left(-\frac{r^2}{R^2}\right) \quad \text{For } A \leq 10 \end{array} \right.$$

$$\left\{ \begin{array}{l} P_F(r) = \left(\frac{3\pi^2 \rho(r)}{2}\right)^{1/3} \\ E_F(r) = \hbar^2 \frac{(3\pi^2 \rho(r))^{2/3}}{2m_N} \end{array} \right.$$

$$\left\{ \begin{array}{l} V \equiv V_N = E_F + \text{Binding energy} \\ V_\pi = 25 \text{ MeV} \end{array} \right.$$

## Quasi free scattering

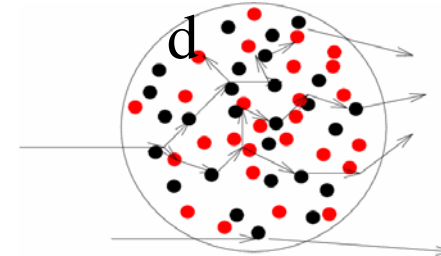
$$\lambda \ll d$$

$$\lambda \ll \Lambda$$

$\lambda$ =de-Broglie wavelength

$d$ =distance between two nucleon

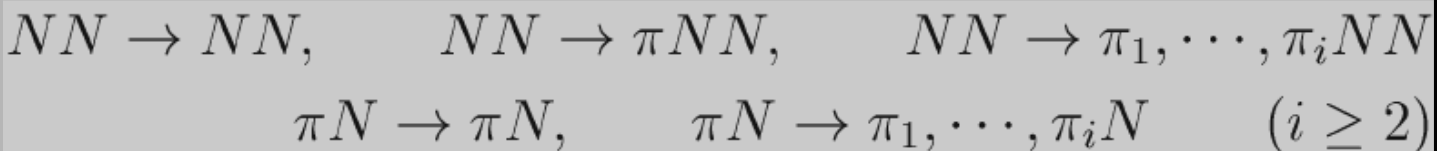
$\Lambda$ =mean free path inside nucleus



## Drawback of this theory

It is not self consistent theory

It is based on experimental knowledge



## Reactions

$$\left\{ \begin{aligned}
 \cos(\theta) &= 2\xi^{1/2} \left[ \sum_{n=0}^N a_n \xi^n + \left(1 - \sum_{n=0}^N a_n\right) \xi^{N+1} \right] - 1 \\
 a_n &= \sum_{k=0}^N a_{nk} E^k \\
 N=3, M=3
 \end{aligned} \right.$$

**Angular distribution**

**Cross-section**

$p + p = p + p$	Isotropic $E < 0.46$ GeV
$p + p = p + p$	$0.46 < E < 2.8$ GeV
$p + p = p + p$	$2.8 < E < 10.0$ GeV
$p + n = p + n$	$E < 0.97$ GeV
$\pi^+ + p = \pi^+ + p$	$E < 80.0$ MeV
$\pi^+ + p = \pi^+ + p$	$80 < E < 300.0$ MeV
$\pi^+ + p = \pi^+ + p$	$0.3 < E < 1.0$ GeV
$\pi^+ + p = \pi^+ + p$	$1.0 < E < 2.4$ GeV

# Pre-equilibrium model (Exciton model)

**Cut off energy (7 MeV) is the criteria to close INC**

n, p, d, t, <sup>3</sup>He, and <sup>4</sup>He emission

**Probability of emission is calculated as given below**

$$\Gamma_j(p, h, E) = \int_{V_j^c}^{E-B_j} \lambda_c^j(p, h, E, T) dT,$$

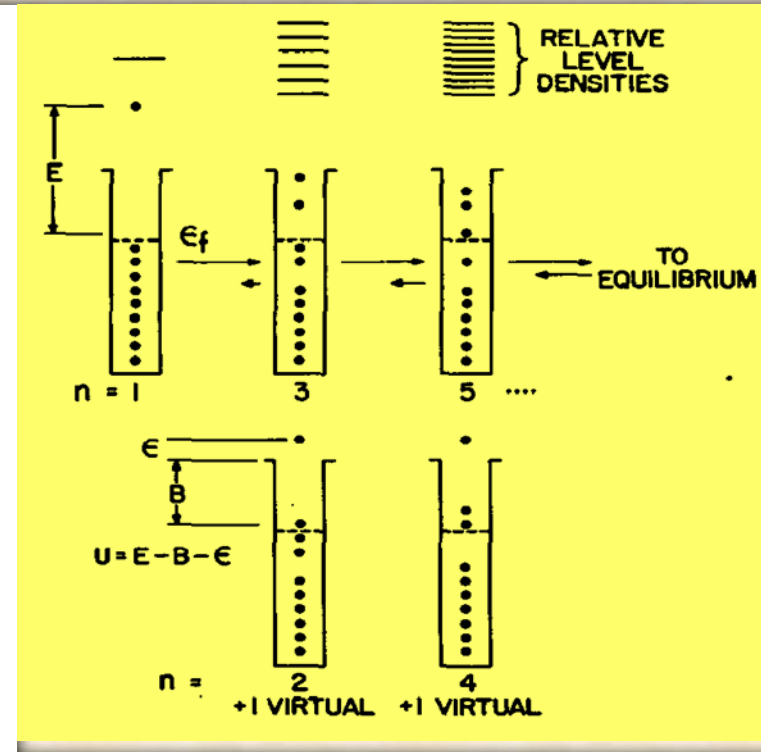
$$\lambda_c^j(p, h, E, T) = \frac{2s_j + 1}{\pi^2 \hbar^3} \mu_j \mathfrak{R}_j(p, h) \frac{\omega(p-1, h, E-B_j-T)}{\omega(p, h, E)} T \sigma_{inv}(T)$$

p=particle, h=hole, n=p+h is exciton

number, s=spin,

$\sigma_{inv}$ =cross-section, E=excitation

energy, B=binding energy



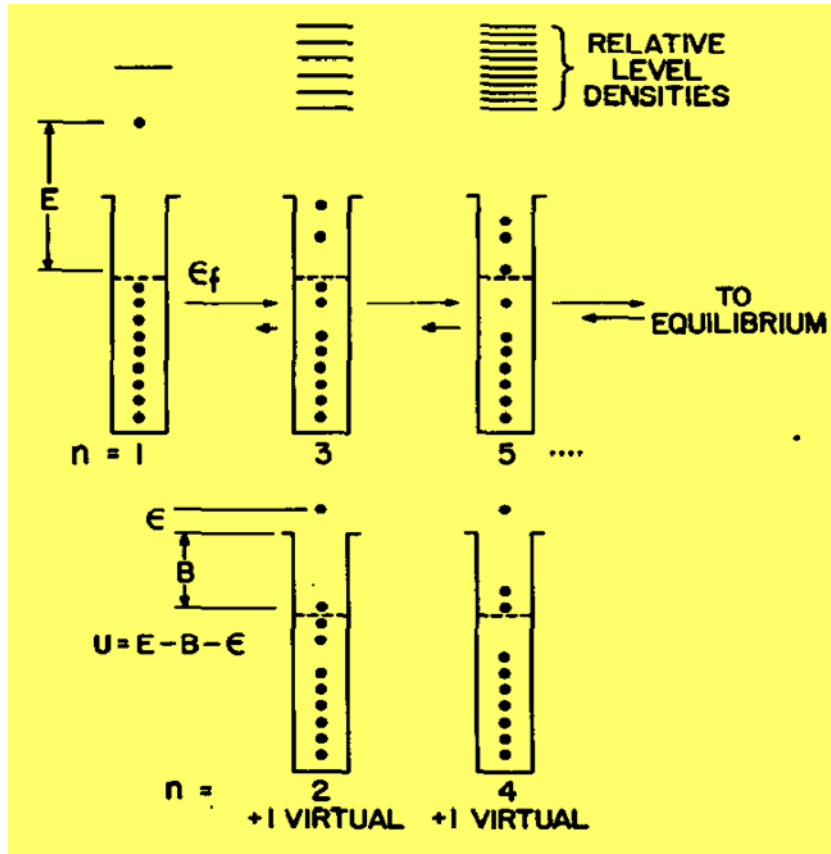
**Normalize p, d, t, <sup>3</sup>He, and <sup>4</sup>He emission probability to 1**

**Generate random number**

**Select the probable one**

# Evaporation model

## How do we reach equilibrium



$$P_j(\epsilon)d\epsilon = g_j\sigma_{inv}(\epsilon)\frac{\rho_d(E - Q - \epsilon)}{\rho_i(E)}\epsilon d\epsilon$$

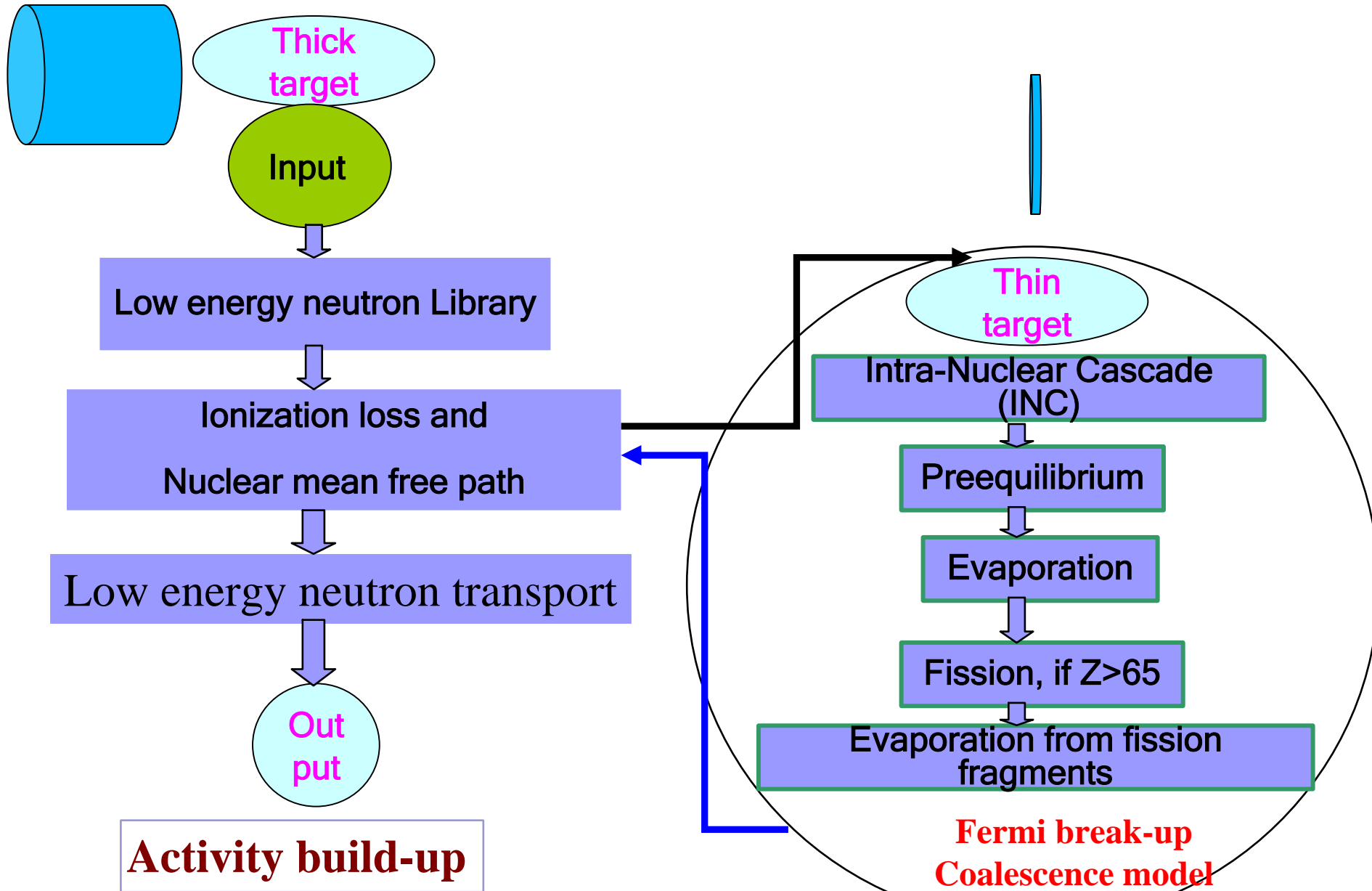
$Z_j$	Ejectiles							
0	n							
1	p	d	t					
2	$^3\text{He}$	$^4\text{He}$	$^6\text{He}$	$^8\text{He}$				
3	$^6\text{Li}$	$^7\text{Li}$	$^8\text{Li}$	$^9\text{Li}$				
4	$^7\text{Be}$	$^9\text{Be}$	$^{10}\text{Be}$	$^{11}\text{Be}$	$^{12}\text{Be}$			
5	$^8\text{B}$	$^{10}\text{B}$	$^{11}\text{B}$	$^{12}\text{B}$	$^{13}\text{B}$			
6	$^{10}\text{C}$	$^{11}\text{C}$	$^{12}\text{C}$	$^{13}\text{C}$	$^{14}\text{C}$	$^{15}\text{C}$	$^{16}\text{C}$	
7	$^{12}\text{N}$	$^{13}\text{N}$	$^{14}\text{N}$	$^{15}\text{N}$	$^{16}\text{N}$	$^{17}\text{N}$		
8	$^{14}\text{O}$	$^{15}\text{O}$	$^{16}\text{O}$	$^{17}\text{O}$	$^{18}\text{O}$	$^{19}\text{O}$	$^{20}\text{O}$	
9	$^{17}\text{F}$	$^{18}\text{F}$	$^{19}\text{F}$	$^{20}\text{F}$	$^{21}\text{F}$			
10	$^{18}\text{Ne}$	$^{19}\text{Ne}$	$^{20}\text{Ne}$	$^{21}\text{Ne}$	$^{22}\text{Ne}$	$^{23}\text{Ne}$	$^{24}\text{Ne}$	
11	$^{21}\text{Na}$	$^{22}\text{Na}$	$^{23}\text{Na}$	$^{24}\text{Na}$	$^{25}\text{Na}$			
12	$^{22}\text{Mg}$	$^{23}\text{Mg}$	$^{24}\text{Mg}$	$^{25}\text{Mg}$	$^{26}\text{Mg}$	$^{27}\text{Mg}$	$^{28}\text{Mg}$	

$$\lambda_+(n_{eq}, E) = \lambda_-(n_{eq}, E) \quad n_{eq} \simeq \sqrt{2gE}$$

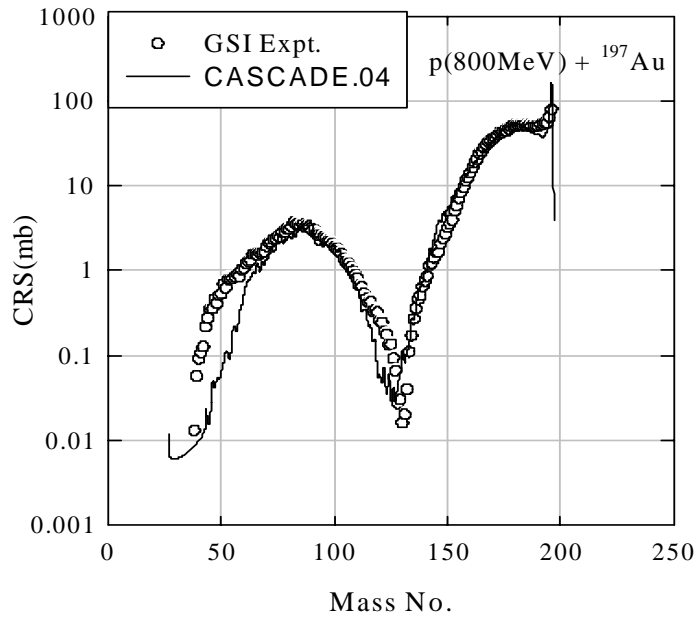
$$\rho(E) = \frac{c_1 \exp(2\sqrt{a(E - \delta)})}{a^{1/4}(E - \delta)^{5/4}}$$

$$a(A_d, Z_d, E) = A_d(0.134 - 1.2110^{-04} A_d)(1 + \frac{S}{E}(1 - \exp(-0.061E)))$$

# CASCADE.04 general scheme



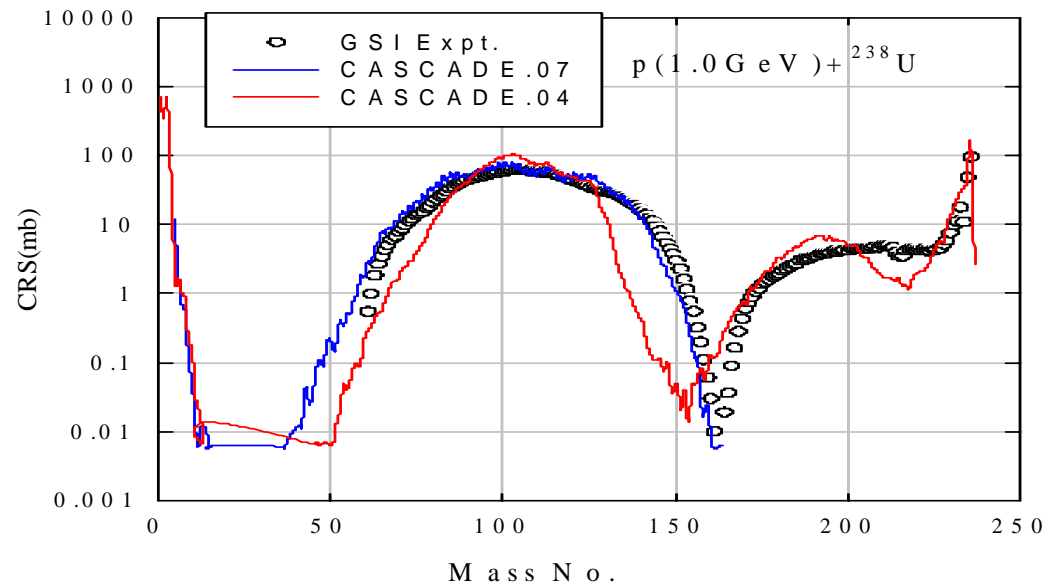
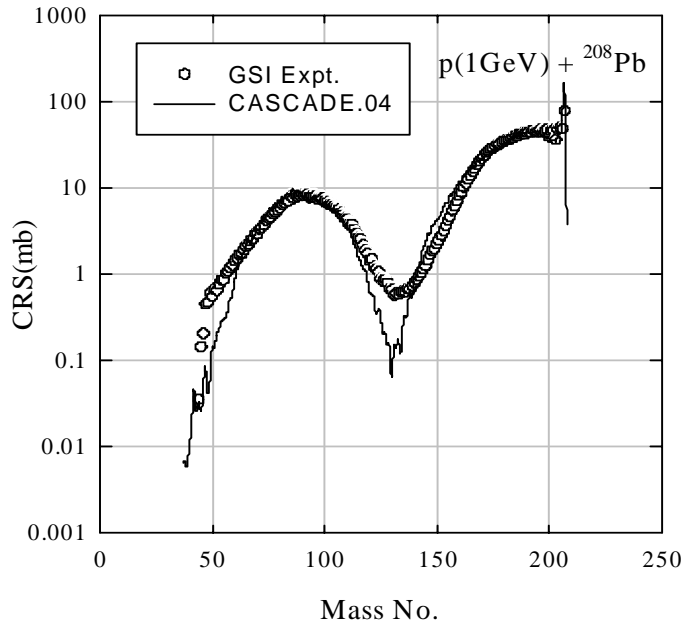
# Results, Benchmark



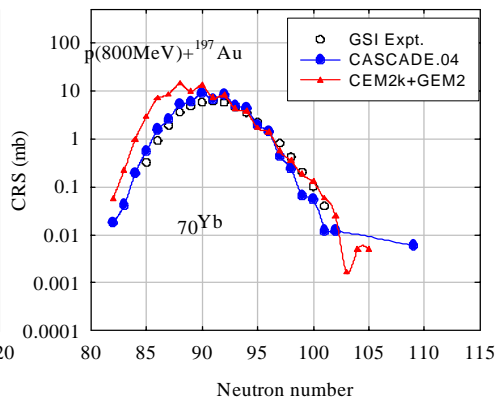
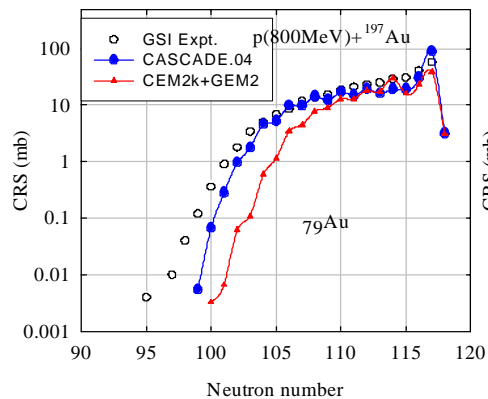
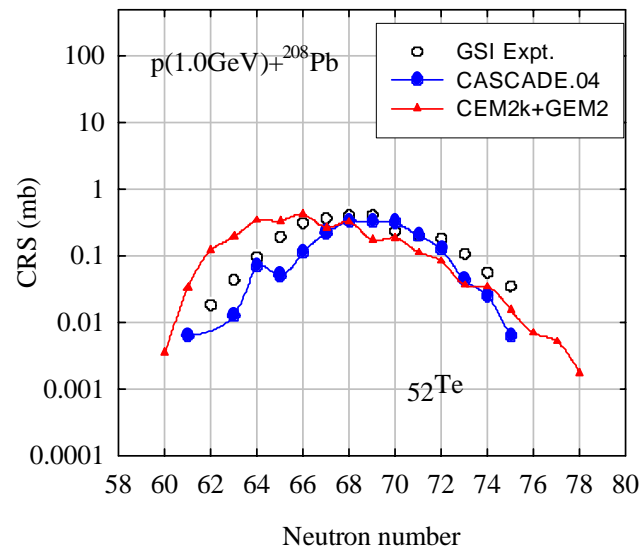
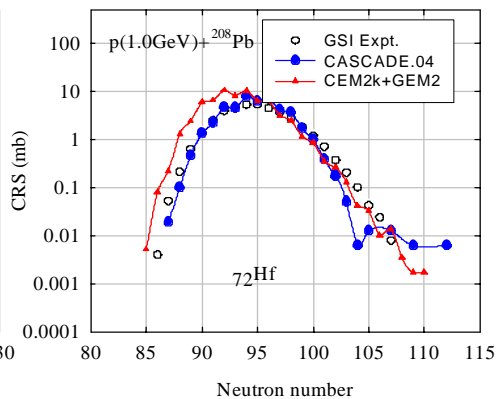
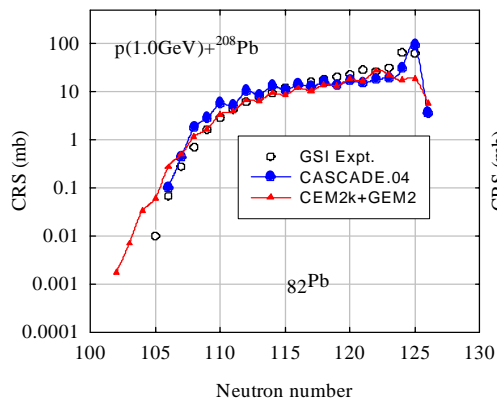
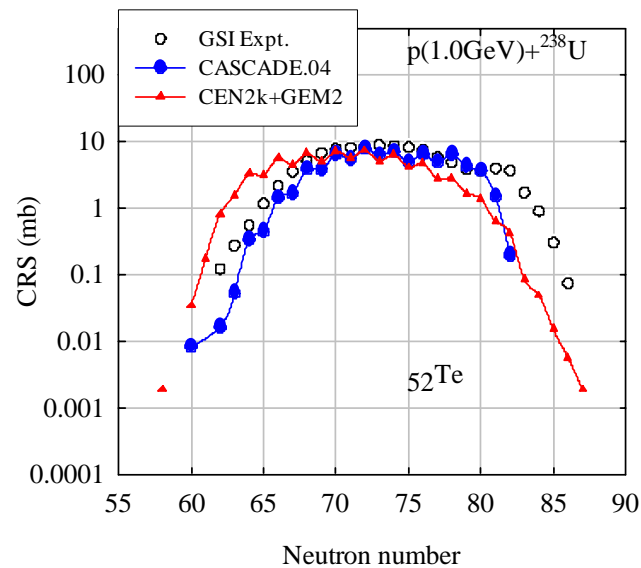
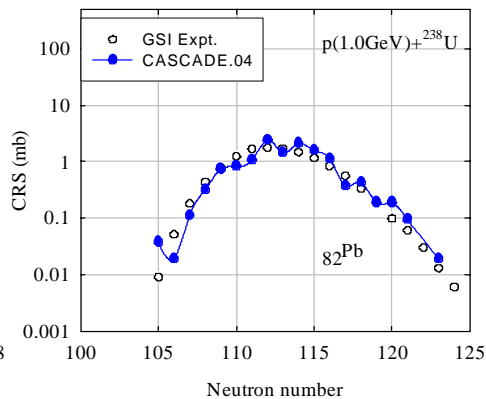
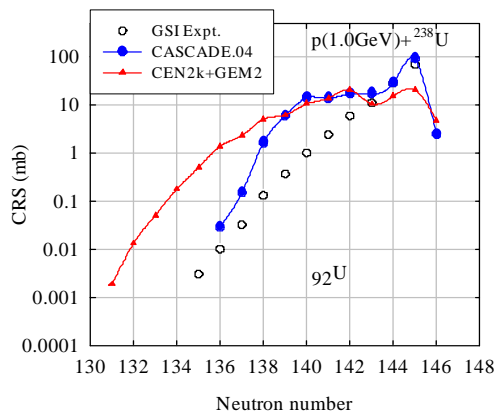
**Mass Distributions**  
**Isotope distribution**  
**Excitation function**

**$n, p, d, t, {}^3\text{He}, {}^4\text{He}, p, \alpha$**

**Thick target simulation**

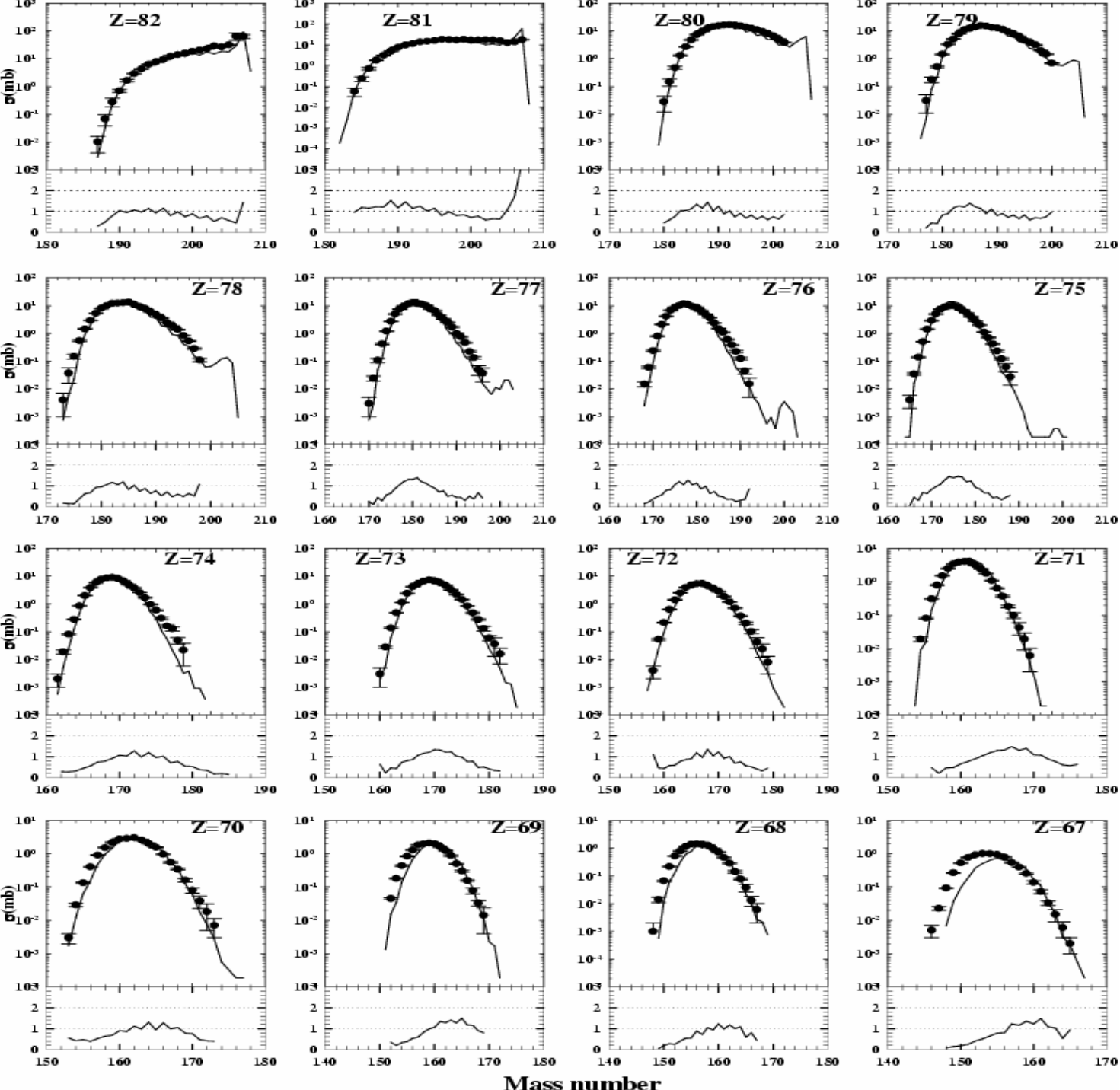


# Spallation Evaporation and Fission Residues

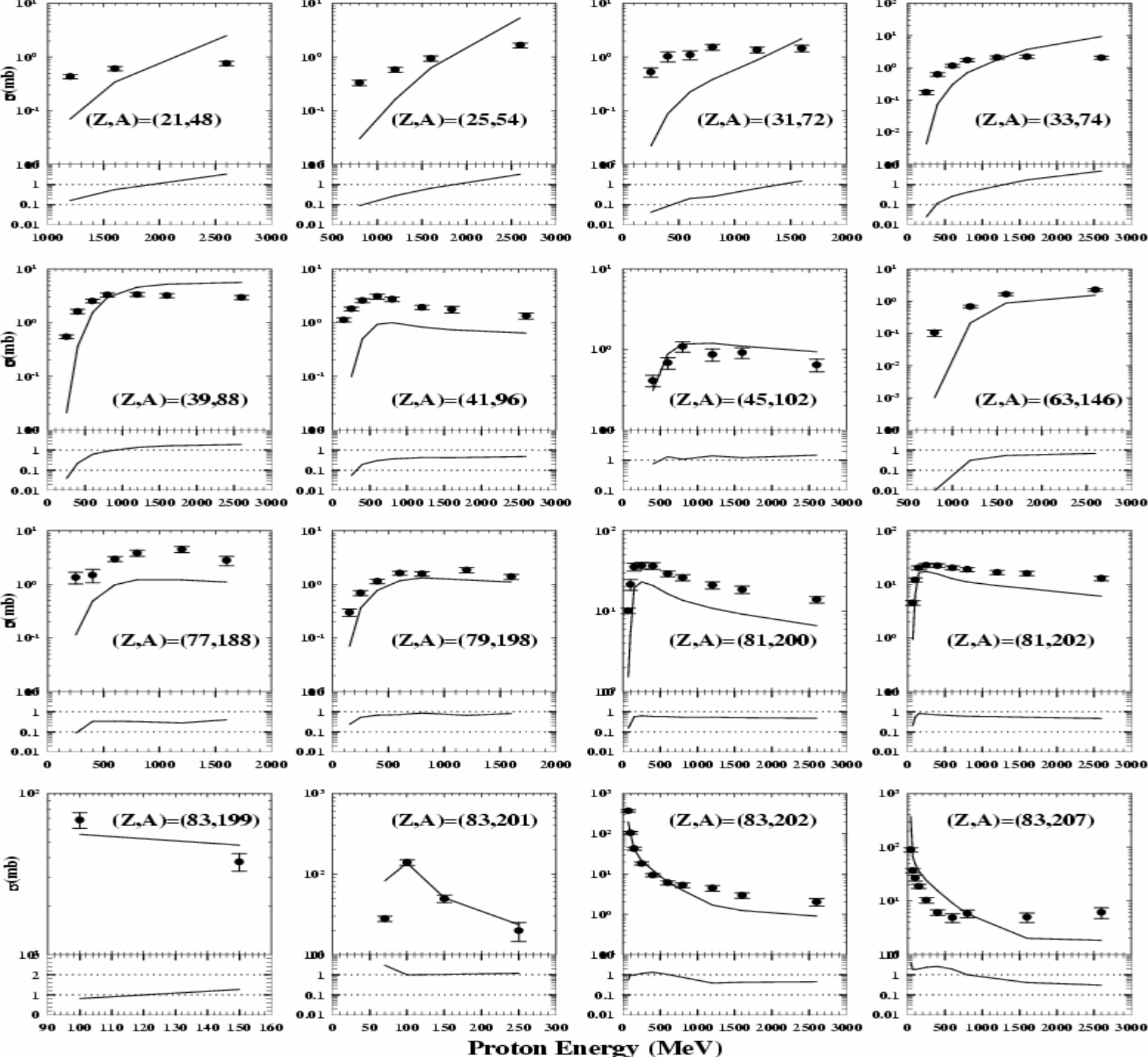


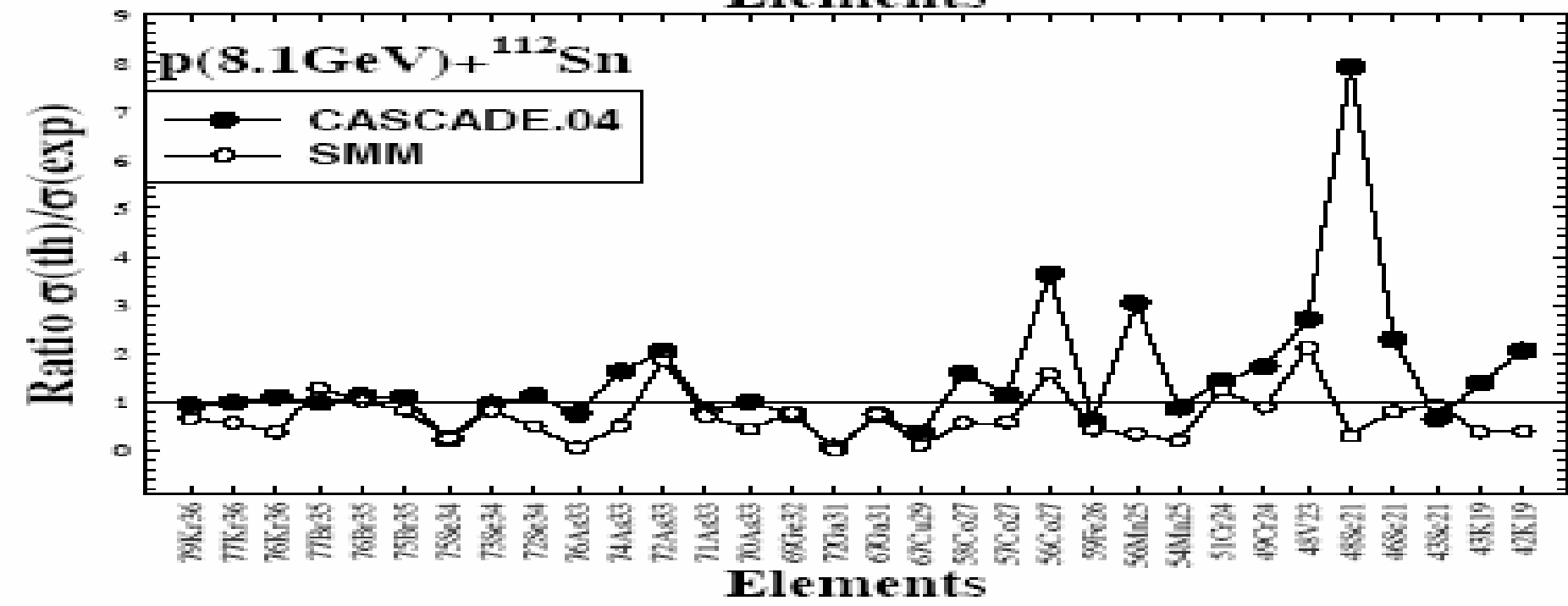
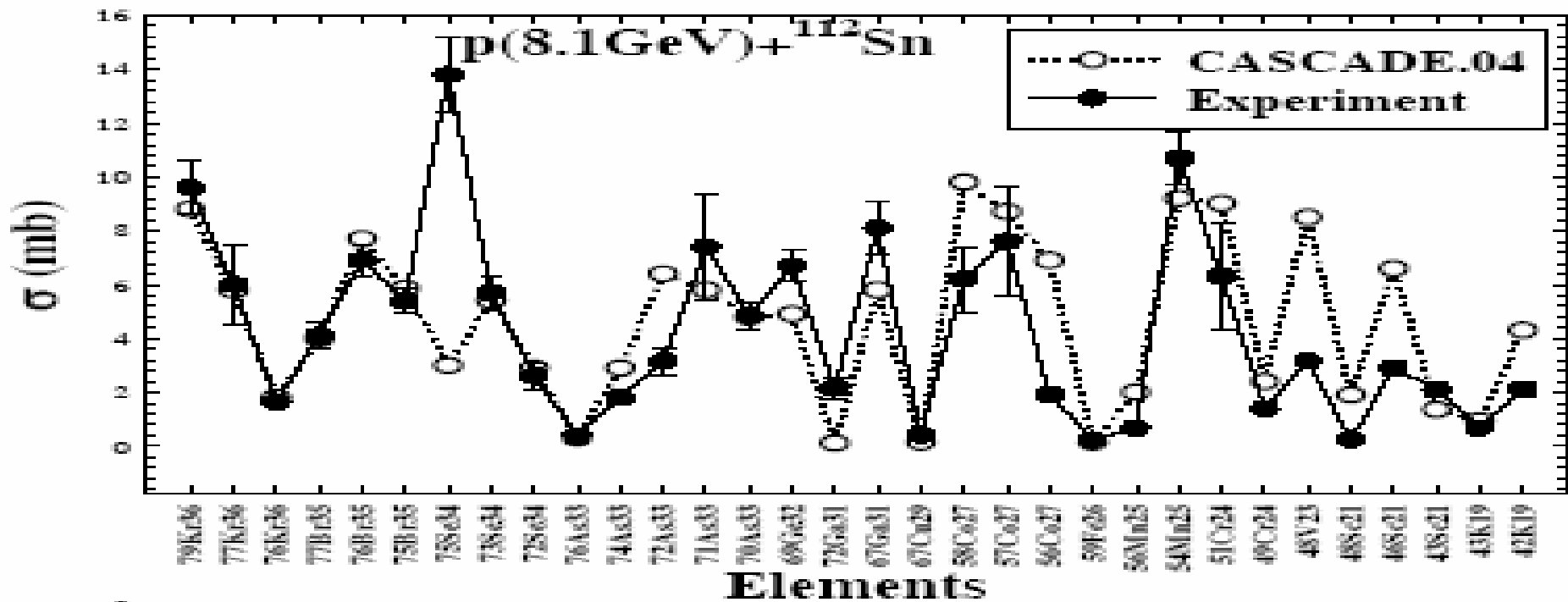


Different  
Isotopes  
From  
 $p(1\text{GeV})+\text{Pb208}$   
system

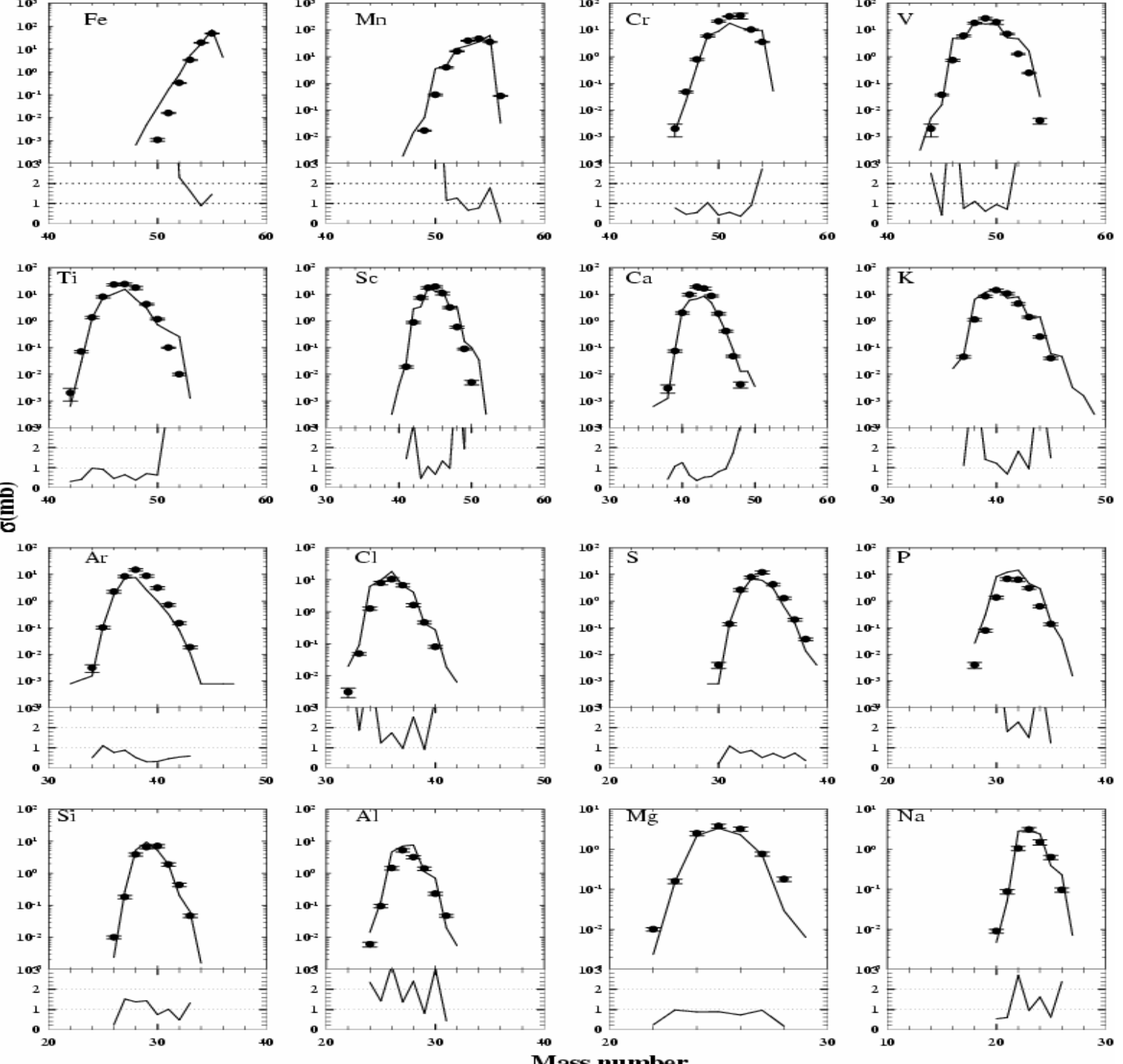


Cross-section  
For  
p+208Pb

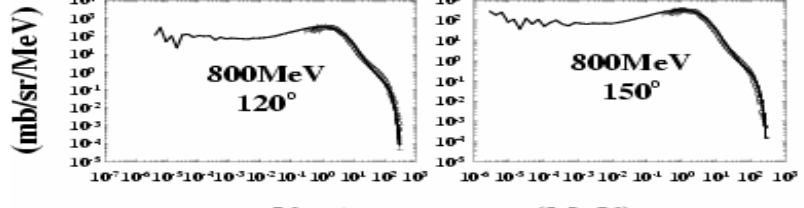
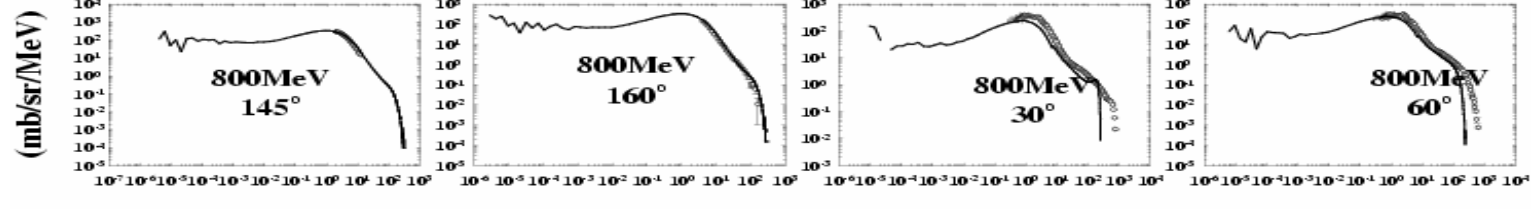
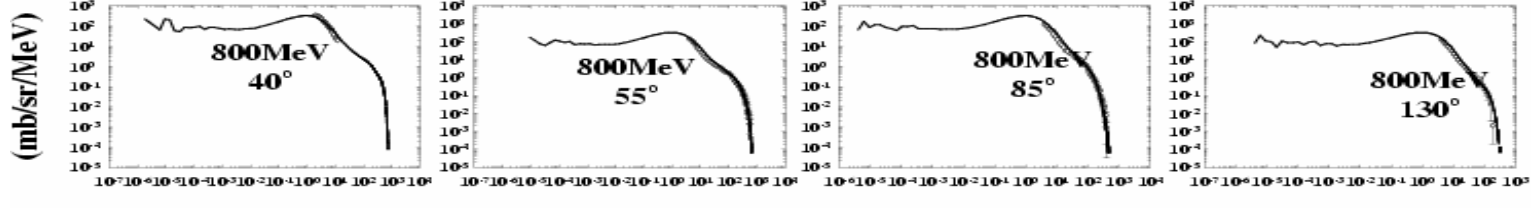
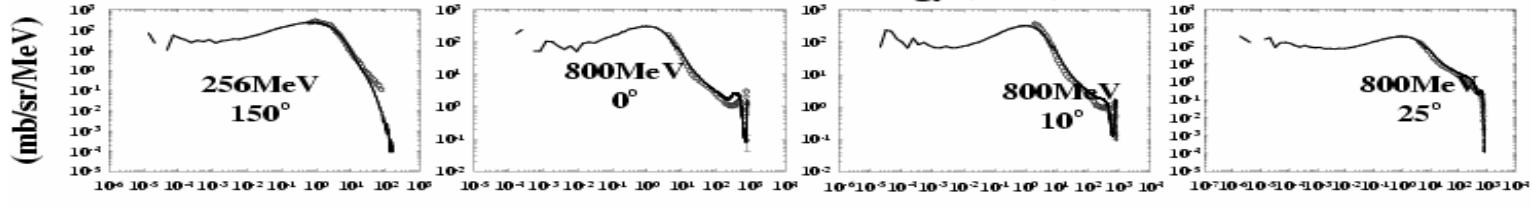
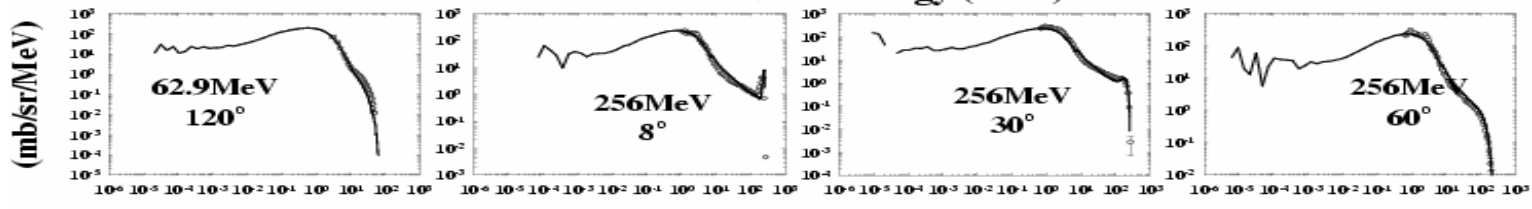
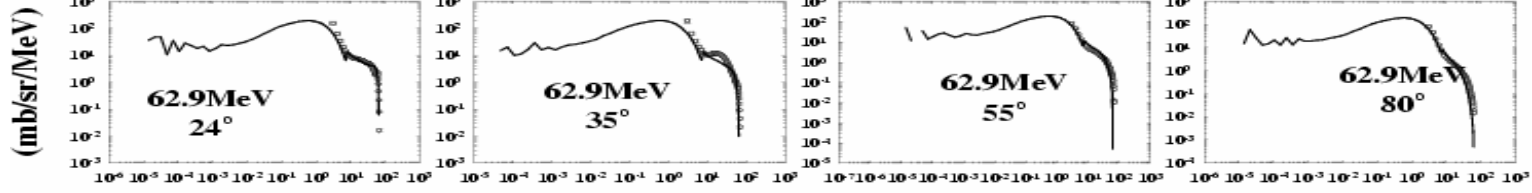




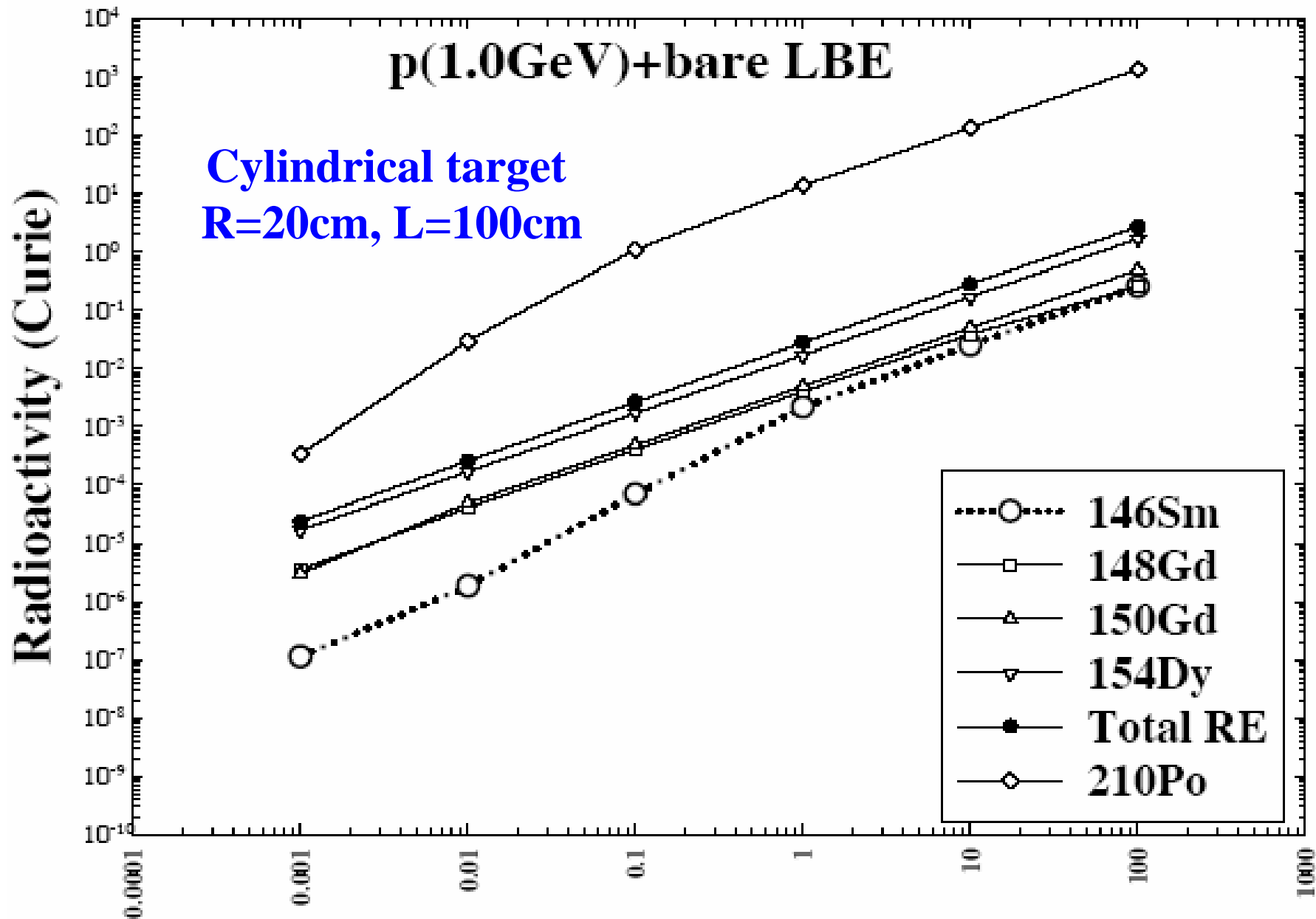
Different  
Isotopes  
From  
p(1GeV)+Fe56  
system



Double  
Differential  
Neutron  
Production  
Cross-  
section  
For p+Pb208  
system



# Alpha radio-activity in LBE due to Rare earth and $^{210}\text{Po}$



## **Thick target simulation**

### **Pre-defined geometries:**

**Spherical, cylindrical, conical, hexagonal, elliptical, hemi-sphere, hemi-elliptical, cubic ..**

### **Low energy data library**

**26-group data library**

**ENDFVII.0 is implemented for Pb<sup>208</sup> more to be done**

**Ionization/Stopping power calculation is implemented up to 100GeV**

**Coupled with burnup code ☺**

# **Thick target simulation Results**

**Heat deposition due to primary and secondaries**

**Neutron yield, Angular /energy spectra, spatial and radial flux distribution**

**Isotope buildup**

**Burnup,  $k_{\text{eff}}$ ?**

**Biasing:**

**Weight cutoff, energy cutoff, geometry splitting and exponential method**