

Neutron induced resonance reactions

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I	R	F	U

Neutron-nucleus reactions

Reaction:	• X + a \rightarrow Y + b • X(a,b)Y • X(a,b)
Examples of equivalent notations:	$ \begin{array}{c} ^{10}B + {}^{1}n \rightarrow {}^{7}Li + {}^{4}He \\ ^{10}B + n \rightarrow {}^{7}Li + \alpha \end{array} $

Reaction cross section σ , expressed in barns, $1 b = 10^{-28} m^2$

¹⁰B(n,α)

Neutron induced nuclear reactions:

- elastic scattering (n,n)
- inelastic scattering (n,n')
- capture (n,γ)
- fission (n,f)
- particle emission (n,α), (n,p), (n,xn)

Total cross section σ_{tot} : sum of all reactions

Neutron-nucleus reactions

Reaction:

• X + a
$$\rightarrow$$
 Y + b
• X(a,b)Y



Cross section:

function of the kinetic energy of the particle a

$$\sigma(E_a) = \int \int rac{d^2 \sigma(E_a, E_b, \Omega)}{dE_b d\Omega} dE_b d\Omega$$

Differential cross section:

function of the kinetic energy of the particle a and function of the kinetic energy **or** the angle of the particle **b**

Double differential cross section:

function of the kinetic energy of the particle a and function of the kinetic energy **and** the angle of the particle **b**

$$rac{d\sigma(E_a, E_b)}{dE_b} = rac{d\sigma(E_a, \Omega)}{d\Omega}$$

 $rac{d^2\sigma(E_a,E_b,\Omega)}{dE_bd\Omega}$



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Interference of $\sigma_{\text{potential}}$ and σ_{n}

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shell model representation:

configuration of nucleons in their potential

level scheme representation:





shell model representation:

configuration of nucleons in their potential

level scheme representation:





shell model representation:

configuration of nucleons in their potential

level scheme representation:





shell model representation:

configuration of nucleons in their potential

level scheme representation:





Decay of a nuclear state





Conservation of probability density:

$$\sigma(\Omega) = \frac{r^2 j_{\text{out}}(r, \Omega)}{j_{\text{inc}}}$$

Solve Schrödinger equation of system to get cross sections. Shape of wave functions of in- and outgoing particles are known, potential is unknown. Two approaches:

- calculate potential (optical model calculations, smooth cross section)
- use eigenstates (R-matrix, resonances)

R-matrix formalism

partial incoming wave functions: \mathcal{I}_c partial outgoing wave functions: $\mathcal{O}_{c'}$ related by collision matrix: $U_{cc'}$

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cross section:
$$\sigma_{cc'} = \pi \lambda_c^2 |\delta_{c'c} - U_{c'c}|^2$$



Find the wave functions



External region: easy, solve Schrödinger equation

central force, separate radial and angular parts. solution: solve Schrödinger equation of relative motion:

- Coulomb functions

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• special case of neutron particles (neutrons): fonctions de Bessel

 $\psi(r,\theta,\phi) = R(r)\Theta(\theta)\Phi(\phi)$

Internal region: **very difficult**, Schrödinger equation cannot be solved directly solution: expand the wave function as a linear combination of its eigenstates. using the R-matrix:

$$R_{cc'} = \sum_{\lambda} \frac{\gamma_{\lambda c} \gamma_{\lambda c'}}{E_{\lambda} - E}$$







The R-matrix formalism

- The R-matrix formalism is adapted to describe compound nucleus reactions.
- Typically used for neutron-induced reactions at low energy (E_n<10 MeV, resonance region).
- The resonance parameters are properties of the excited nuclear levels:

- in the resolved resonance region (RRR), to each level (resonance) corresponds a set of parameters:

$E, J^{\pi}, \Gamma_n, \Gamma_{\gamma}$

- in the unresolved resonance region (URR) average parameters are used:

 $< D_{\ell} >, < \Gamma_n^{\ell} >, < \Gamma_{\gamma}^{\ell} >$



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Resonance parameters

- A same set of resonance parameters is used to produce all resonant reactions,
- at low energies mainly elastic scattering and capture (and fission).

 $\sigma_{r,t} = \sigma_{r,t}$ (resonance parameters)

- In a measurement, one does not measure a cross section, but a reaction yield or
- transmission factor.

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$$Y_r = (1 - e^{-n\sigma_t})\frac{\sigma_r}{\sigma_t} \qquad 0 < Y_r < 1$$
$$T = e^{-n\sigma_t} \qquad 0 < T < 1$$

- The measured reaction yield is not equally sensitive to all parameters, additional
- constraints can be necessary to extract RP from measurement.

Neutron-nucleus reactions

R-matrix resonance description

• fine structure (resonances)

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- highly fluctuating cross sections
- resonance parametrization
- low energy, few channels

Optical model calculations

- gross structure
- average cross sections
- optical model potential
- high energy, many channels



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Compound nucleus reactions







Statistical model

The nucleus in the vicinity of S_n is described by the Gaussian Orthogonal Ensemble (GOE)

The matrix elements are random variables with a Gaussian distribution.

- Consequences:
 - The partial width have a Porter-Thomas distribution.
 - The spacing of levels with the same J^π have approximately a Wigner distribution.



Distribution of the spacing of two consecutive levels

 (\mathbf{e})

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 (\mathbf{e}) IRFU Known nuclei 120 ₣ proton number Z stable neutron number N









Level spacing D₀



Neutron separation energy

 $\gamma \alpha$

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Neutron separation energy





Fission of ²³⁵U+n and ²³⁸U+n



^u Measurement of (n.xn) by gamma-ray spectroscopy



example: 182W(n,3n)180W



Simulated gamma-ray spectrum



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Moderation of neutrons

Maxwell-Boltzmann velocity distribution: $\sim v^2 \exp(-rac{mv^2}{2k_BT})$ dndv $v_{\rm max} = \sqrt{2k_BT/m}$ $E_{\rm max} = \frac{1}{2}mv^2 = k_BT$

thermal neutrons:

$$v_{
m max} = 2200 \text{ m/s} \text{ (def.)}$$

 $E_{
m max} = 25.3 \text{ meV}$
 $T = \frac{1}{2}mv^2/k_B = 293.6 \text{ K}$







Evaluated nuclear data libraries

Libraries

- JEFF Europe
- JENDL Japon
- ENDF/B US
- BROND Russia
- CENDL China

Common format: FNDF-6

Contents:

Data for particle-induced reactions (neutrons, protons, gamma, other) but also radioactive decay data

Data are indentified by "materials" (isotopes, isomeric states, (compounds)) 16**O**· mat = 825 ex. natV∙ mat = 2300

 $^{242m}Am; mat = 9547$



Files for a material

from report ENDF-102

1 General information

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- 2 Resonance parameter data
- 3 Reaction cross sections
- 4 Angular distributions for emitted particles
- 5 Energy distributions for emitted particles
- 6 Energy-angle distributions for emitted particles
- 7 Thermal neutron scattering law data
- 8 Radioactivity and fission-product yield data
- 9 Multiplicities for radioactive nuclide production
- 10 Cross sections for photon production
- 12 Multiplicities for photon production
- 13 Cross sections for photon production
- 14 Angular distributions for photon production
- 15 Energy distributions for photon production
- 23 Photo-atomic interaction cross sections
- 27 Atomic form factors or scattering functions for photo-atomic interactions
- 30 Data Covariances obtained from parameter covariances and sensitivities
- 31 Data covariances for nubar
- 32 Data covariances for resonance parameters
- 33 Data covariances for reaction cross sections
- 34 Data covariances for angular distributions
- 35 Data covariances for energy distributions
- 39 Data covariances for radionuclide production yields
- 40 Data covariances for radionuclide production cross sections



Example: part of an evaluated data file



Neutron Capture Gamma-Ray Detection



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Activation

- cross sections integrated over known neutron spectrum
- applicable to some nuclei only
- no time of flight

Level population spectroscopy

- applicable to some nuclei only
- feasible with HPGe detectors,

• Total energy detection

- $\epsilon_c {\sim} E_x$, requires weighting function
- neutron insensitive detector example: C₆D₆ liquid scintillator

Total absorption detection

- requires Ω = 4 π , efficiency 100%
- capture/fission discrimination in possible, example BaF₂ total absorption calorimeter











Kinetic energy of the neutron by time-of-flight

$$E_n = E_{tot} - mc^2 = c^2 p^2 + m^2 c^4 - mc^2 = mc^2 (\gamma - 1) \qquad \gamma = (1 - v^2/c^2)^{-1/2}$$
$$E_n = \frac{1}{2}mv^2 = \alpha^2 \cdot \frac{L^2}{t^2}$$



The resolution can be expressed equivalenty in time, distance and energy:

$$R_t(\delta t)d\delta t = R_L(\delta L)d\delta L = R_E(\delta E)d\delta E$$

















Further Reading

Books/Papers

IRFU

- K. S. Krane, Introductory Nuclear Physics, Wiley & Sons, (1988).
- G. F. Knoll, Radiation Detection and Measurement, Wiley & Sons, (2000).
- P. Reus, Précis de neutronique, EDP Sciences, (2003).
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- A. M. Lane, R. G. Thomas, "R-matrix theory of nuclear reactions", Rev. Mod. Phys. 30 (1958) 257.
- G. Wallerstein, et al., "Synthesis of the elements in stars: forty years of progress", *Rev. Mod. Phys.* **69** (1997) 995.

Web sites

www.nea.fr www.nndc.bnl.gov wwwiaea.org www.cern.ch/ntof www.irmm.jrc.be



Conclusion

- Neutron induced reactions are important nuclear data necessary for a wide range of fields ranging from nuclear structure and astrophysics to advanced nuclear technology applications.
- The R-matrix formalism is adapted to describe compound nucleus reactions at low energy (E_n<10 MeV, resonance region).
- Resolved resonances need to be measured accurately, they cannot be predicted by nuclear models.



Rapport de branchement ²⁰⁹Bi + n





L'origine des déchets nucléaires



Réduire la radiotoxicité: la transmutation en complément de stockage



Clefs CEA 46 (2002)

Composition des déchets

produits de fission

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transmutation par capture de neutrons dans flux de neutrons thermique

actinides mineurs

transmutation par fission induite par neutrons dans flux de neutrons rapide

Réduire la radiotoxicité des déchets: le cylce du thorium

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 $-\Delta$ IRFU Réduire la radiotoxicité des déchets: la transmutation (n,γ) (n,γ) 100**T**c* ⁹⁹Tc 129 130 * β⁻ (2x10⁵ y) β⁻ (1.6x10⁷ y) ¹²⁹Xe ⁹⁹Ru γ γ ¹⁰⁰Tc 130

β⁻ (15.8 s)

¹⁰⁰Ru

 β^{-} (12 h)

¹³⁰Xe



Resolution

n_TOF





